Exploring In-Service Mathematics Teachers’ Perceived Professional Development Needs Related to the Strands of Mathematical Proficiency (SMP)

Areej Isam Barham

1 Qatar University, QATAR

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Abstract
The National Research Council developed the concept of mathematical proficiency as being described by five strands: conceptual understanding, procedural fluency, strategic competency, adaptive reasoning, and productive disposition. The purpose of this study is to explore in-service mathematics teachers’ perceptions of professional development needs related to the five strands of mathematical proficiency and to investigate the effect of teachers’ demographic factors on their perceived needs. Participants included 342 teachers with varying qualifications and years of experience teaching at multiple grade levels (elementary, preparatory, and secondary) in Qatar’s government schools. The study uses a 35-item questionnaire to evaluate teachers’ professional development needs within the five strands.

Keywords: in-service mathematics teachers, professional development needs, strands of mathematical proficiency

INTRODUCTION
Over the past few decades, there has been a worldwide increase in the need for teachers’ professional development (TPD) (Loucks-Horsley & Matsumoto, 1999; Villegas-Reimers, 2003; Conference Board of the Mathematical Sciences, 2012). The reason for this increase in TPD is based on the idea that the teacher is a vital person in the teaching and learning process, one who provides information, explains concepts and skills, gives examples, assesses student ability, and provides feedback to support the learning process. Therefore, teachers are the key factor in improving instruction and student learning in the mathematics classroom (Hiebert et al., 1997).

Rowan, Correnti, and Miller (2002) suggest that teachers who know content and practice effective teaching strategies positively affect their students’ learning. This requires classroom teachers to possess pedagogical content knowledge (Shulman, 1987). Villegas-Reimers (2003) suggests teachers use this to construct their conceptual map, which encompasses how to teach, use different instructional strategies, and provide representations to facilitate student learning and create a positive learning environment. More importantly, TPD is one of the basic elements that aid teachers in building new pedagogical content knowledge and developing their expertise and practice in their classes, ultimately leading to enhanced student learning (Ball, Thames, & Phelps, 2008; Kaiser et al., 2017; Wood et al., 2011).

Bednarz, Fiorentini, and Haung (2011) identified seven principles for professional development standards based on the National Research Council (2001) and the National Staff Development Council (1995). One key principle of TPD is to consider teachers as the starting point by investigating their understanding of mathematics and then building upon that understanding. Shriki and Lavy (2011) addressed the importance of conducting professional development programs that meet teachers’ needs so that they will be more eager to attend such programs and the TPD will maximize its impact on teachers’ development. Mundy (2005) pointed out the importance of using research-based methods to explore teachers’ needs, while other researchers mention the need for teachers not only to possess mathematics content knowledge but also to develop effective ways of teaching that help students master mathematics learning (Ball et al., 2008; Hill & Ball, 2004).
Contribution to the literature

- Although mathematical teaching competencies were examined in previous studies, reflecting the SMP to some extent, this current study aims to explore teachers’ needs related to all five strands of mathematical proficiency (SMP).
- Based on the study’s analysis, teachers prefer to attend tailored programs prioritizing productive disposition, adaptive reasoning, conceptual understanding, strategic competence, and procedural fluency.
- The developed research instrument demonstrated high validity and reliability across the SMP. Researchers can use this instrument to explore teachers’ perceptions of their professional development needs or develop it for use as a qualitative research tool to examine mathematics teachers’ needs.

Mathematics is commonly viewed as an essential subject throughout the duration of most students’ school lives. As a result of the efforts of mathematicians and curriculum developers during the twentieth century, the concept of Mathematical Proficiency has emerged, as described by the five strands developed by the National Research Council (NRC, 2001), for example. According to the NRC (2001), these strands of mathematical proficiency (SMP) comprise all aspects required for any student to learn mathematics successfully. The five SMP are conceptual understanding, procedural fluency, strategic competency, adaptive reasoning, and productive disposition. One of the most important aspects of this concept is that “the five strands are interwoven and interdependent in the development of proficiency in mathematics” (NRC, 2001, p. 116). The purpose of this study is to explore in-service mathematics teachers’ perceptions of professional development needs related to the five strands of mathematical proficiency, as well as identify how the teachers’ demographic factors affect these perceived needs. The five SMP will serve to frame the current study. They will inform the design of the research instrument, as well as the data collection, analysis, and interpretation processes involved in the current study. The following section reviews the literature to give background information and to build a credible theoretical context by defining the strands of mathematical proficiency and relating them to the professional instructional needs of teachers.

LITERATURE REVIEW

There is a rich body of literature in the area of mathematical proficiency, covering many different perspectives. In the current study, two aspects are examined to help in designing and conducting this research. The first body concentrates on identifying the SMP and instructional strategies and tools that help teachers provide effective mathematics instruction related to the SMP. The second body addresses studies on the needs of mathematics teachers and reviews literature on the role of teachers’ demographic factors that may affect their needs.

The Strands of Mathematical Proficiency

Researchers and educators in the field of mathematics education have developed the concept of successful mathematics learning, leading to the concept of mathematical proficiency. A review of the literature demonstrates that mathematics teachers must acquire teaching skills that enable them to assist their students in learning and using the strands of mathematical proficiency. The following portion of the surveyed literature provides a review of previous research that addresses the identification of SMP and related studies that focus on required teaching skills related to these strands.

The first strand of mathematical proficiency is conceptual understanding. This strand represents students’ understanding of mathematical concepts, operations, and relations. The National Research Council (2001) and the National Council of Teachers of Mathematics (2000) argued that for students to achieve this strand, teachers need to acquire basic knowledge and specific teaching skills to help build conceptual understanding for students. Teachers’ pedagogical capacities in using multiple representations, making connections between mathematical ideas, and developing mathematical communication skills are essential abilities for developing a student’s conceptual understanding (NCTM, 2000; NRC, 2001). Shriki and Patkin (2016) addressed the importance of teachers knowing how to develop a student’s ability to represent their mathematical ideas. Davis and Simmt (2006) addressed the need for mathematics teachers to know how concepts are presented and elaborated through the curriculum. They also pointed out that finding vocabulary, images, and algorithms play an important role in developing student understanding of mathematical concepts. Hence, teachers must be adept at ‘translating’ among available symbol systems and recognizing when they are engaging in such translations.

The second component is procedural fluency, which reflects students’ ability to carry out mathematics procedures in an accurate, appropriate, efficient, and flexible way (NRC, 2001). This strand requires careful instruction to help students achieve different
computational skills, either by using paper and pencil, conducting mental operations, using calculators or computers, or even giving estimated solutions (Fuson, 1990; Hiebert et al., 1997). The National Research Council (2001) identified the use of concrete models and practice drill exercises as effective ways to help students develop mathematical algorithms and skills.

The third strand is strategic competence that demonstrates a student’s ability to formulate, represent, and solve mathematical problems. This strand requires that teachers possess the professional skills needed to develop student ability in solving challenges such as word problems related to specific mathematical knowledge and developing problem-solving strategies and techniques (NRC, 2001). Developing a student’s strategic competence requires careful instruction because it requires students to formulate specific mathematical problems and acquire different skills in representing the problem via methods of numerical, symbolic, verbal, or graphical representation (Schoenfeld, 1988). This step reflects students’ understanding of the problem and helps them develop appropriate techniques for a solution. Expert problem solvers can form mental representations, detect mathematical relationships, and develop novel solution techniques such as diagram creation, methods of trial and error, table construction, list creation, logical reasoning, pattern finding, or working retrospectively in a flexible way (NCTM, 2000; Common Core State Standards Initiative [CCSSI], 2010; Australian Curriculum and Assessment Reporting Authority [ACARA], 2014).

The fourth component is adaptive reasoning. This component represents a student’s capacity to engage in logical thought, reflection, explanation, and justification. Shriki and Patkin (2016) point out that teachers need basic teaching skills to develop students’ capabilities of presenting mathematical arguments and justifications, improving their mathematical thinking skills, and furthering their reflective abilities. The adaptive reasoning strand can flourish when teachers employ their teaching skills in a number of ways, including conducting mathematical proofs, estimating and predicting, finding analogical correspondences that represent powerful reasoning mechanisms, and applying intuitive, inductive, and deductive thinking (NRC, 2001).

The fifth strand is productive disposition, which refers to the tendency to make sense in mathematics, to believe that it is useful and valuable, and to see oneself as an effective learner and doer of mathematics (NRC, 2001). Several researchers have addressed the importance of teacher ability in building positive attitudes towards mathematics learning (Fang, 2012; Shriki & Lavy, 2011; Shriki & Patkin, 2016).

One important feature of the SMP is that all the strands are aligned with one another: conceptual understanding, procedural fluency, strategic competence, and adaptive reasoning are integrated elements. Once these strands are developed, students become confident of their ability to complete mathematical tasks, understand the value of mathematics, recognize mathematical structure, and build positive attitudes towards mathematics. As a result, a productive disposition is formed (NRC, 2001).

Based on the above description of each strand of mathematical proficiency and its related required teaching skills, the research instrument was developed by constructing the items of the questionnaire and distributing them among the five SMP within the data analysis process.

Mathematics Teachers’ Needs and Some Related Factors

The review of the literature revealed a complex range of issues that reflect the needs of mathematics teachers and indicate that these needs are varied in different domains. Teachers’ needs related to mathematical proficiency in general were addressed in a number of studies (Fang, 2012; Superfine & Li, 2014) and investigated as they related to each strand of mathematical proficiency in others (Evans, 2012, 2014; Polly, 2011; Shriki & Lavy, 2011; Steele & Rogers, 2012). In order to present previous research focused on mathematics teachers’ needs in a clear way, the collected studies were reviewed and classified according to themes related to the SMP.

Some studies have addressed teachers’ need to acquire different teaching skills or knowledge that may enhance students’ conceptual understanding (Fang, 2012; Superfine & Li, 2014; Polly, 2011; Shriki & Lavy, 2011). More specifically, Fang (2012) explored the needs of high school mathematics teachers regarding mathematics professional literacy through quantitative and qualitative research. Results showed there is a need to develop teachers’ skills in using mathematical language and symbols, developing spatial visualization, and acquiring knowledge of common core mathematical concepts and ideas that indicate needs related to conceptual understanding. According to Polly (2011), who examined the impact of the development of technological pedagogical content knowledge of two mathematics teachers after their participation in a learner-centered professional development project, technology may not necessarily assist in this. Although the project concentrated on the use of technology in the mathematics classroom, results of the professional development demonstrated that students’ conceptual understanding in mathematics was not improved. This indicates that there is still a need to develop teaching skills to enhance students’ conceptual understanding. In relation to this strand, Shriki and Lavy (2011) investigated the perceptions of 138 mathematics teachers regarding their needs for professional development with consideration given to the effect of years of teaching...
experience as one of the factors that may affect teacher needs. Results of the study found that the most relevant needs were teacher’s development of their mathematical knowledge and the acquisition of knowledge that can help them lead their students towards the understanding of mathematical concepts. Furthermore, Shriki and Lavy (2011) demonstrated that the second most relevant need was knowledge on student learning; teachers must know how students understand mathematics, how they perceive various concepts, and how they construct their mathematical knowledge. Similar findings were reported by Superfine and Li (2014), who designed and implemented a model for the professional development for mathematics teachers who teach content courses through a two-year project. The topics of the project’s workshops incorporated six dimensions based on the analysis of teacher and educator practices and needs of teachers. Mapping between the representation and the formulating and revising of mathematical definitions were two of the dimensions that reflect teachers’ needs in acquiring skills related to conceptual understanding.

Other studies explored teachers’ needs for the development of skills related to mathematical literacy. In turn, this demonstrated teachers’ need for their students to acquire procedural fluency (Fang, 2012; Evans 2012; Superfine & Li, 2014). In particular, Fang (2012) demonstrated that teachers’ skill in performing mathematical operations is one of the most important needs. Evans (2012) found that middle and high school mathematics teachers have poor literacy skills. In relation to this strand, Superfine and Li (2014) demonstrated pre-service elementary teachers’ needs in analysis of student errors, as well as performing multiplication and division operations on fractions.

Other researchers highlighted the need for teachers to master skills that could develop their students’ problems-solving skills, which may match their needs related to strategic competence (Evans, 2012, 2014; Fang, 2012; Superfine & Li, 2014). Fang’s (2012) results demonstrated that the competencies of problem solving and applying multiple strategies to solve different kinds of mathematical problems match the strategic competence strand and are the most important skills. Evans (2012) found that middle and high school mathematics teachers who participated in an alternative certificate program had significant improvement in their problem-solving abilities. However, the study also found that although there was improvement in problem-solving abilities, these skills were still generally weak because of teachers’ failure to start on a problem, poor literacy skills, and a lack of time or effort working on their mathematical problems. In another study, Evans (2014) argued that one of the best ways to help students acquire better content understanding is by providing them with the opportunity to learn through problem solving and inquiry learning, which both include critical thinking.

Various studies have suggested there is a need for teachers to develop their students’ adaptive reasoning skills, such as higher-level thinking skills (Polly, 2011) and the ability to overcome difficulties associated with mathematical justifications and proofs (Superfine & Li, 2014). In the same domain, additional research (Barham and Al-Khateeb, 2012) found that pre-service mathematics teachers have intermediate abilities in induction, reasoning and mathematical proof, and poor thinking skills in modeling, estimation, criticism, guessing, symbols expression and justification. Fang’s study (2012) demonstrated that there was a need for developing teacher competencies in abstracting and generalizing. The researchers (Steele & Rogers, 2012) conducted a study to explore the relationship between mathematical knowledge for teaching and teaching practice in reasoning and proofing. The study used a qualitative research approach by conducting observations and clinical assessments for two secondary mathematics teachers who had varying degrees of experience, prior knowledge, and school settings. Despite these differences, the results indicated that using Mathematics Knowledge for Teaching (MKT) for examining and assessing classroom practice provides a deeper and more innovative framework for the investigation. Findings of the study also found that student levels of ability to communicate mathematical knowledge is a key mediating factor between MKT and the opportunity to learn. In the same study, Steele and Rogers (2012) found that teachers have difficulties with proofs and they often prefer to follow empirical arguments rather than deductive proofs, as they view the former as easier than the latter.

Of equal importance is the teacher’s need to interact with his or her students (Shriki & Lavy, 2011) to build positive attitudes towards the learning of mathematics; these may reflect productive disposition (Fang, 2012). In the same domain, Shriki and Patkin (2016) examined elementary mathematics teachers’ perceptions of their professional needs and examined whether a teacher’s needs changed based on their academic qualifications and the age group taught. The study sample was composed of 84 teachers who were interviewed and responded to a questionnaire. Results showed that the main needs are strengthening teacher knowledge and ability to deal with emotional aspects that relate to students’ learning of mathematics. The same results are supported by Fang (2012), who showed that teachers’ needs in building confidence in teaching mathematics and establishing positive attitudes towards mathematics learning in their classrooms reflect needs related to productive disposition.

Although a variety of mathematical teaching competencies were examined in previous studies that reflect the SMP to some extent, the innovation of this current study is that it aims to explore teachers’ needs
related to all five strands of mathematical proficiency (SMP).

Some studies reviewed here also addressed the effect of teachers’ characteristics, such as teaching experience, educational background, and age group taught on perceptions of teachers’ needs. Fang (2012) examined the role of demographic data such as educational background and teaching experience. Results of the study demonstrated that although demographic variables have little or no effect on teachers’ needs in terms of rating perceived importance, teaching experience has a significant effect on teacher’s needs in terms of perceived level of mastery in specific domains. In the same context, Shriki and Lavy (2011) found that perceived needs differ based on years of teaching experience. Their findings showed that new teachers perceived needs in developing their knowledge to gain self-confidence, whereas more experienced teachers perceived needs in developing teaching skills to influence student learning. The study also showed that highly experienced teachers perceived needs in developing their knowledge to satisfy their curiosity. In another study, the role of teacher qualifications and grade level taught were explored by Shriki and Patkin (2016). Results of the study demonstrated that more experienced teachers perceived fewer professional needs. Findings of the study also showed low significance of teachers’ academic education and age group taught. In the same context, Evans (2014) pointed out that teachers with less experience were not well prepared in the content and pedagogy required to teach mathematics successfully when compared with experienced teachers.

Overall, review of the literature showed that mathematics teachers’ needs at various grade levels have been well investigated. Previous studies have examined teachers’ needs at the elementary level (Shriki & Patkin, 2016), the secondary level (Evans, 2012, 2014; Fang, 2012; Steele & Rogers, 2012), and the university level (Superfine & Li, 2014). This current study considers the grade level taught (primary, preparatory, and secondary) as one of the factors to be examined in exploring whether teachers’ needs differ.

In light of these previous studies, the current study aims to explore the effect of teachers’ demographic factors, such as qualifications, grade level taught, and years of teaching experience on their perceived needs.

Background and Rationale

The State of Qatar is a developing country. Despite a massive educational reform program instituted over the last 13 years, students have shown low levels of achievement on international mathematics tests such as TIMSS (2011, 2015), National Center for Education Statistics (2012, 2016), and PISA (2012). In 2008, following several years of comprehensive planning and analysis, the state of Qatar articulated long-term national goals and values in the Qatar National Vision 2030 (General Secretariat for Development Planning, 2008). To achieve these purposes, the National Strategy concentrates on plans, programs, and projects that Qatar should pursue in 14 sectors, including the Education and Training Sector (Supreme Education Council, 2014). In light of the Qatar National Vision 2030 and in the hope of supporting teachers’ professionalization in mathematical proficiency and mathematics education in general, this study aims to explore in-service mathematics teachers’ perception of professional development needs related to the SMP and investigate the effect of teachers’ demographic factors on their perceived needs. Applying such research is of significant importance as part of the assessment of teachers’ professional development (TPD) needs, with special consideration of the five (SMP): conceptual understanding, procedural fluency, strategic competency, adaptive reasoning, and productive disposition. Results of the study will inform researchers, mathematicians, and educators about current needs and direct them to future professional development programs that meet teachers’ needs. In turn, this may improve their instructional practices and indirectly enhance students’ learning. The study provides a theoretical framework for designing a valid and reliable research instrument for measuring and identifying teachers’ needs related to the SMP. The study also investigates the effect of teachers’ demographic factors that may affect their perceived needs. Results and recommendations of the study will guide researchers toward future studies in terms of significant strands and factors.

Research Questions

The study aimed to answer the following two questions:

1. To what extent do in-service mathematics teachers perceive their professional development needs related to the strands of mathematics proficiency?
2. Are there any statistically significant differences in perceptions of teachers’ needs related to the effect of teacher’s qualifications, grade level taught, and years of teaching experience?

METHODOLOGY AND METHODS

Research Design

The study used a quantitative research design using a survey method. A descriptive survey research design was implemented that involved collection of quantitative data to answer the two key research questions. The survey design suited the current study, as the accessible population consisted of a total of 1184 in-service mathematics teachers. The sample of the study consisted of 342 teachers who were selected randomly.
and represented 28.89% of all government school teachers currently teaching mathematics. This survey design (questionnaire) enables quantitative descriptions to represent perceptions and views in a population by studying a sample selected within the population (Creswell, 2014).

**Instruments**

To explore to what extent in-service mathematics teachers perceive their professional development needs related to the SMP, a survey questionnaire was developed by the researcher. The researcher used a comprehensive review of the literature to inform the design of the questionnaire. Following are some examples related to the five SMP: Item a20 reads “Teaching by using multiple mathematical representations,” and item a27 states “Developing students’ ability in forming connections between relations in mathematics.” These items were designed based on NRC (2001) and NCTM (2000), which assert that teachers’ pedagogical knowledge on using multiple mathematical representations and making connections between mathematical ideas are essential skills for developing students’ conceptual understanding. Item a14, “Developing students’ skills in identifying appropriate procedures,” and item a19, “Teaching mental operations and strategies,” were constructed based on work by Fuson (1990) and Hiebert et al. (1997), who argued that procedural fluency requires careful instruction to help students achieve different computational skills either by using pencil and paper, conducting mental operations, using calculators or computers, or even giving estimated solutions. Item a10, “Developing students’ skills in representing mathematical problems,” and item a17, “Developing students’ skills in problem-solving strategies,” were designed based on CCSSI (2010) and ACARA (2014), which mentioned that strategic competence requires careful instruction to help students form mental representations, detect mathematical relationships, and develop novel solutions and techniques in a flexible way. Regarding adaptive reasoning, item a11, “Identifying mathematical thinking skills,” was designed based on Shriki and Patkin (2016), who pointed out that teachers should achieve basic teaching skills for developing students’ mathematical thinking ability. In addition, item a32, “Enhancing mathematical proof for students,” was built based on the NRC (2001), which asserted that teachers are responsible for developing the adaptive reasoning strand for their students by developing their teaching skills in conducting mathematical proofs. Items related to productive disposition, such as a24, “Enhancing students’ belief in one’s own efficacy,” were also designed based on the NRC (2001), which argued that productive disposition refers to the tendency to make sense in mathematics and to see oneself as an effective learner and doer of mathematics. Item a28, “Building positive attitudes towards mathematics,” was designed based on Fang (2012) and Shriki and Lavy (2011), who addressed the importance of teachers’ abilities to build positive attitudes and emotional aspects towards mathematics learning. The questionnaire consisted of two sections. The first section included demographic information such as gender, grade level taught, teachers’ qualifications, and years of teaching experience. The second section consisted of 35 Likert scale items. The 35 items were rated as follows: 4 = most relevant to my needs, 3 = relevant to my needs, 2 = fairly relevant to my needs, 1 = less relevant to my needs, 0 = not relevant to my needs. Questionnaire items were classified into five domains to measure mathematics teachers’ needs related to the SMP. Table 1 shows the distribution of items in the strands of mathematical proficiency (SMP).

**Validity and Reliability of the Instrument**

**Validity of the research instrument**

The first process was the translation of the questionnaire into Arabic. To ensure the equivalent meaning of the items, translation and back translation were conducted by two experts who are bilingual in Arabic and English. The back-translation process was performed by an independent person who did not see the original version before translating the instrument back to the first language. The researcher then compared the translated and original versions, found where points were not fully aligned, and made changes to reconcile the versions. A second round of translation by the independent person then took place, with this process continuing until the versions were nearly identical. For construct validity, four experts in the area of mathematics education were consulted and asked to provide explicit notes like, “keep as is,” “keep with these changes …,” or “omit because ….” Accordingly, the references were used to support the validation process and went beyond Cronbach’s alpha, also supporting the construct validation and the back-translation processes. Thus, constructive validity was met. Based on the data gained from the pilot study, the correlation between each of the items against the entire scale (n=35, N=342) was calculated and then items with significant correlations at p < 0.01 were selected. Results showed that the questionnaire items’ correlations ranged...
Table 2. Item correlations with the whole scale and item correlations with the strands

<table>
<thead>
<tr>
<th>Items</th>
<th>SMP</th>
<th>Item correlations with the whole scale</th>
<th>Item correlations with the strands</th>
</tr>
</thead>
<tbody>
<tr>
<td>a7</td>
<td>Conceptual understanding</td>
<td>.797**</td>
<td>.813**</td>
</tr>
<tr>
<td>a13</td>
<td>Procedural fluency</td>
<td>.828**</td>
<td>.865**</td>
</tr>
<tr>
<td>a21</td>
<td>Strategic competence</td>
<td>.828**</td>
<td>.850**</td>
</tr>
<tr>
<td>a82</td>
<td>Adaptive reasoning</td>
<td>.834**</td>
<td>.875**</td>
</tr>
</tbody>
</table>

**. Correlation is significant at the 0.01 level (2-tailed).

between 0.656 and 0.848 with the whole scale and ranged between 0.716 and 0.875 with the strands. For example, the item correlation for a7 was 0.797 with the whole scale and 0.813 within its related strand (conceptual understanding). The item correlation for a24 was 0.834 with the whole scale and 0.875 with its related strand (productive disposition). Table 2 shows some examples of item correlation with its related strand and with the whole scale.

In addition, correlations between the strands of mathematical proficiency were calculated, and the results showed positive correlations among them. The value of (r) ranged between 0.817 and 0.963. For example, the correlation between strategic competence and productive disposition was 0.817, while the correlation between procedural fluency and the whole scale was 0.963.

Previous values of (r) demonstrate that the questionnaire has good validity.

Reliability of the research instrument

The statistical reliability of the instrument was calculated using Cronbach’s alpha coefficient of internal consistency both for the questionnaire as a whole and separately for the five strands. The analyses produced a 0.98 alpha coefficient value for the whole questionnaire, 0.939 value for conceptual understanding, 0.915 value for procedural fluency, 0.908 value for both strategic competence and adaptive reasoning, and 0.873 value for productive disposition, which indicated a satisfactory level of reliability (Robinson, Shaver, & Wrightsman, 1991). The high-value alpha coefficients suggest that the instrument is suitable to measure mathematics teachers’ perceptions of professional development needs related to the SMP.

Participants and Data Collection

The research was conducted during the second semester of the 2015-2016 academic year. The questionnaire was distributed to over 29 governmental primary, preparatory, and secondary schools in Qatar. Participants were 342 teachers (92 male, 250 female) across primary (133), preparatory (62), and secondary (147) stages in Qatari government schools. Qualifications varied from bachelor’s degrees (279) to higher diplomas (48) to master’s or Ph.D. level (14). Experience ranged from 1-3 years (26), 4-6 years (76), 7-11 years (88), 12-18 years (79), to more than 18 years (72).

Mathematics teachers in the participating schools were asked to volunteer to participate in the study. Teachers were also informed about the purpose of the study, asked to respond to the questionnaire, and assured of confidentiality.

Data Analysis

The study followed a quantitative research approach. Descriptive statistics were utilized via Statistical Packages for Social Sciences (SPSS 15.0). To answer the first research question, means, standard deviations, percentages, and t-tests were used for pre-defined values to identify in-service mathematics teachers’ professional development needs related to the SMP.

A comparison was made between the mean score of the responses on the items of the questionnaire, the five strands of mathematical proficiency, and for the whole scale. Additionally, t-values were calculated to examine if there were statistically significant differences regarding teachers’ needs compared with a predetermined average value (= 2) that lies in the middle of the scale; this is because the scale was a Likert-type scale ranging from 0 to 4. Teachers’ responses were classified based on a descriptive rubric (Table 3) which was presented at the beginning of the questionnaire to guide participants in how to respond to the questionnaire items, and to specify operationally their professional development needs related to the SMP.

The top 3 box scores were also used to better understand and analyze the scale questions by calculating the sum of percentages for the three highest rating points on the scale.

In addition, means, standard deviations, and Analysis of Variance (ANOVA) were calculated to examine if there were any statistically significant differences in teachers’ perceptions regarding their needs related to the SMP in favor of the effect of teacher’s qualifications, grade level taught, and years of teaching experience.

RESULTS

Findings Related to the First Research Question

The first question of the study examined to what extent in-service mathematics teachers perceive their professional development needs related to the SMP. As shown in Table 4, the overall mean score for the scale
Table 3. Descriptive rubric of teachers’ professional development needs related to the SMP

<table>
<thead>
<tr>
<th>Teachers’ PD Needs</th>
<th>Description</th>
<th>Scale</th>
</tr>
</thead>
<tbody>
<tr>
<td>Most relevant to my needs</td>
<td>Means that you have no information about this subject/topic and cannot apply it in the teaching of mathematics.</td>
<td>4</td>
</tr>
<tr>
<td>Relevant to my needs</td>
<td>Means that you know little information about this subject but you cannot apply it in the teaching of mathematics.</td>
<td>3</td>
</tr>
<tr>
<td>Fairly relevant to my needs</td>
<td>Means that you have some information about this subject and have limited experience in its application in the teaching of mathematics.</td>
<td>2</td>
</tr>
<tr>
<td>Less relevant to my needs</td>
<td>Means that you have good knowledge about this subject and good experience in its applications in the teaching of mathematics.</td>
<td>1</td>
</tr>
<tr>
<td>Not relevant to my needs</td>
<td>Means that you have wide knowledge about this subject and wide experience and skills to apply it in the teaching of mathematics effectively.</td>
<td>0</td>
</tr>
</tbody>
</table>

Table 4. Means, standard deviations and t-tests of teachers’ perceptions regarding their needs

<table>
<thead>
<tr>
<th>One-Sample Statistics</th>
<th>N</th>
<th>Mean</th>
<th>Std. deviation</th>
<th>Std. error mean</th>
<th>T</th>
<th>df</th>
<th>Sig. (two-tailed)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Conceptual understanding</td>
<td>341</td>
<td>2.49</td>
<td>0.970</td>
<td>0.053</td>
<td>9.37</td>
<td>340</td>
<td>0.000</td>
</tr>
<tr>
<td>Procedural fluency</td>
<td>342</td>
<td>2.45</td>
<td>0.993</td>
<td>0.054</td>
<td>8.42</td>
<td>341</td>
<td>0.000</td>
</tr>
<tr>
<td>Strategic competence</td>
<td>342</td>
<td>2.47</td>
<td>1.021</td>
<td>0.055</td>
<td>8.54</td>
<td>341</td>
<td>0.000</td>
</tr>
<tr>
<td>Adaptive reasoning</td>
<td>342</td>
<td>2.56</td>
<td>0.934</td>
<td>0.051</td>
<td>11.10</td>
<td>341</td>
<td>0.000</td>
</tr>
<tr>
<td>Productive disposition</td>
<td>341</td>
<td>2.60</td>
<td>1.083</td>
<td>0.059</td>
<td>10.32</td>
<td>340</td>
<td>0.000</td>
</tr>
<tr>
<td>Mathematical proficiency</td>
<td>341</td>
<td>2.52</td>
<td>0.953</td>
<td>0.052</td>
<td>10.05</td>
<td>340</td>
<td>0.000</td>
</tr>
</tbody>
</table>

was 2.52, suggesting that relevant professional development needs were significantly related to the SMP as a whole and to all the strands of mathematical proficiency in particular.

Results also showed that productive disposition had the highest mean (2.60), followed by adaptive reasoning (2.56) and conceptual understanding (2.49), while the mean score for strategic competence was 2.47, followed by the lowest mean (2.45) for procedural fluency.

The weighted means for the items of the questionnaire were calculated and classified as follows to specify mathematics teachers’ needs. Since the scale was a Likert-type that ranged from 0 to 4 through 5 classifications, the range for each classification was calculated by dividing 4 by 5 (equal to 0.80). The limits for each classification were calculated starting from 0.0, adding 0.80 sequentially, and ending in 4. Hence, the first classification ranged from 0.00 to 0.80, the second classification ranged between 0.81 and 1.60, and so on. This procedure formed the five classifications. Therefore, the weighted mean of teachers’ responses to the items of the questionnaire were classified based on these limits sequentially as follows: not relevant (0.0-0.80), less relevant (0.81-1.60), fairly relevant (1.61-2.40), relevant (2.41-3.20), and most relevant (3.21-4.00).

Table 5 presents the findings demonstrating teachers’ responses towards the items of the questionnaire, reflecting their perceptions on professional development needs related to the SMP.

The results of this study showed that mathematics teachers perceived a need for professional development in all items related to productive disposition and adaptive reasoning, such as “Enhancing students’ belief in one’s own efficacy” and “Enhancing mathematical proof for students.” In addition, they have professional development needs for most of the items belonging to conceptual understanding, such as “Teaching by using multiple mathematical representations,” and strategic competence. From the perception of mathematics teachers, needs were also fairly relevant for procedural fluency items such as “Enhancing students’ skills in carrying out procedures accurately.”

To provide more detail, we reported the survey results in a more informative way by using the top 3 box scores. Table 6 presents the top 3 box scores results by calculating the sum of percentages for the top three highest rating points on the scale, which reflects the percentage of teachers who responded to the items of the questionnaire with “most relevant to my needs,” “relevant to my needs” or “fairly relevant to my needs”. In addition, Table 6 indicates the ranking of the items of the questionnaire and sorts them relative to the five SMP.

The 35 items are ranked from 1 to 20 (see the far left column of Table 6, where the items with the same percentage have the same rank), according to the importance that the respondents attributed to them. Previous analyses (using mean scores and standard deviation) demonstrated that the teachers’ professional development needs were related to all five SMP, with productive disposition receiving the highest mean score, followed by adaptive reasoning, conceptual understanding, and strategic competence, with the lowest mean for procedural fluency. Table 6 gives more in-depth insights regarding teachers’ perceptions of the extent to which they need professional development based on their knowledge and experiences that are represented by the items of the questionnaire in relation to each strand of mathematical proficiency.

Based on the descriptive rubric of the rating scale presented in Table 3, the results in Table 6 reflect the
percentage of respondents who perceived that either they have no information about the item’s subject/topic and cannot apply it in the teaching of mathematics, or they have little information about this subject but they cannot apply it in the teaching of mathematics, or they have some information about this subject but have limited experience in its application in the teaching of mathematics. In brief, the results of the top 3 box scores show the percentage of perceived professional development needs as demonstrated by the respondents.

The top six items in Table 6 represent the most essential perceived needs, as demonstrated by 50% or more of the respondents. Item a3 “developing inductive reasoning for students” was ranked first, which relates to the “adaptive reasoning” domain (57% of the respondents ranked it as “most relevant to my needs”, “relevant to my needs” or “fairly relevant to my needs”). At the same time, item a28 “Enhancing mathematical proof for students”, which is also associated with the same domain, was ranked fourth. In addition, Table 6 reveals that more than half of the respondents (56%) perceived professional development needs for “using conceptual maps in teaching mathematics” (a31), and half of them (50%) perceived professional development needs for “teaching by using multiple mathematical representations” (a20), both associated with the “conceptual understanding” domain. Additional essential needs for more than half of the respondents (55%) are associated with the “procedural fluency” domain, with perceived needs for “enhancing students’ procedural fluency in mathematical operations” (a18), and “productive disposition” domain corresponding to 51% of respondents’ needs, with perceived needs for “enhancing students’ belief in diligence in learning mathematics” (a34).

Table 6 also gives a clear insight into the teachers' perceived professional development needs related to the “productive disposition” domain, where all items associated with this strand are ranked in the first top 9, such as “building positive attitudes towards mathematics” (a28), which was ranked seventh (49%), “enhancing students’ habitual inclination to see mathematics as sensible,
Barham / Teachers’ PD Needs Related to SMP

Table 6. Top 3 box scores results of teachers’ responses to the items of the questionnaire, sorted by ranking and SMP domains

<table>
<thead>
<tr>
<th>Ranking</th>
<th>Items</th>
<th>SMP Domain</th>
<th>Top 3 Box Scores %</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>a3: Developing inductive reasoning for students</td>
<td>AR</td>
<td>57</td>
</tr>
<tr>
<td>2</td>
<td>a31: Using conceptual maps in teaching mathematics</td>
<td>CU</td>
<td>56</td>
</tr>
<tr>
<td>3</td>
<td>a18: Enhancing students’ procedural fluency in mathematical operations</td>
<td>PF</td>
<td>55</td>
</tr>
<tr>
<td>4</td>
<td>a32: Enhancing mathematical proof for students</td>
<td>AR</td>
<td>52</td>
</tr>
<tr>
<td>5</td>
<td>a34: Enhancing students’ belief in diligence in learning mathematics</td>
<td>PD</td>
<td>51</td>
</tr>
<tr>
<td>6</td>
<td>a20: Teaching by using multiple mathematical representations</td>
<td>CU</td>
<td>50</td>
</tr>
<tr>
<td>7</td>
<td>a28: Building positive attitudes towards mathematics</td>
<td>PD</td>
<td>49</td>
</tr>
<tr>
<td>8</td>
<td>a16: Teaching to amend alternative concepts</td>
<td>CU</td>
<td>48</td>
</tr>
<tr>
<td>a5:</td>
<td>Developing students’ ability in formulating word problems</td>
<td>SC</td>
<td>48</td>
</tr>
<tr>
<td>a19:</td>
<td>Teaching mental operations and strategies</td>
<td>PF</td>
<td>48</td>
</tr>
<tr>
<td>a22:</td>
<td>Enhancing students’ habitual inclination to see mathematics as sensible, useful, and worthwhile</td>
<td>PD</td>
<td>48</td>
</tr>
<tr>
<td>9</td>
<td>a24: Enhancing students’ belief in one’s own efficacy</td>
<td>PD</td>
<td>47</td>
</tr>
<tr>
<td>a30:</td>
<td>Making connections between mathematical concepts and procedures to reach mathematical generalizations</td>
<td>CU</td>
<td>47</td>
</tr>
<tr>
<td>10</td>
<td>a2: Applying specific strategies for teaching mathematical concepts</td>
<td>CU</td>
<td>46</td>
</tr>
<tr>
<td>a17:</td>
<td>Developing students’ skills in problem solving strategies</td>
<td>SC</td>
<td>46</td>
</tr>
<tr>
<td>a21:</td>
<td>Enhancing students’ skills in problem solving</td>
<td>SC</td>
<td>46</td>
</tr>
<tr>
<td>a6:</td>
<td>Developing logical thinking for students</td>
<td>AR</td>
<td>46</td>
</tr>
<tr>
<td>a9:</td>
<td>Developing deductive reasoning for students</td>
<td>AR</td>
<td>46</td>
</tr>
<tr>
<td>a29:</td>
<td>Modelling mathematical problems in daily life situations</td>
<td>AR</td>
<td>45</td>
</tr>
<tr>
<td>11</td>
<td>a33: Enhancing students’ skills in approximation, estimation, and prediction</td>
<td>AR</td>
<td>45</td>
</tr>
<tr>
<td>a35:</td>
<td>Teaching mathematical patterns</td>
<td>AR</td>
<td>45</td>
</tr>
<tr>
<td>12</td>
<td>a26: Teaching mathematical concepts via problem solving</td>
<td>CU</td>
<td>44</td>
</tr>
<tr>
<td>a27:</td>
<td>Developing students’ ability in forming connections between relations in mathematics</td>
<td>CU</td>
<td>44</td>
</tr>
<tr>
<td>a10:</td>
<td>Developing students’ skills in representing mathematical problems</td>
<td>SC</td>
<td>44</td>
</tr>
<tr>
<td>13</td>
<td>a25: Measuring student acquisition of mathematical concepts</td>
<td>CU</td>
<td>43</td>
</tr>
<tr>
<td>14</td>
<td>a11: Identifying mathematical thinking skills</td>
<td>AR</td>
<td>42</td>
</tr>
<tr>
<td>14</td>
<td>a14: Developing students’ skills in identifying appropriate procedures</td>
<td>PF</td>
<td>42</td>
</tr>
<tr>
<td>a23:</td>
<td>Enhancing students’ skills in carrying out procedures accurately</td>
<td>PF</td>
<td>42</td>
</tr>
<tr>
<td>15</td>
<td>a7: Developing conceptual understanding for students</td>
<td>CU</td>
<td>40</td>
</tr>
<tr>
<td>a12:</td>
<td>Teaching problem solving strategies</td>
<td>SC</td>
<td>40</td>
</tr>
<tr>
<td>16</td>
<td>a13: Developing students’ competencies in carrying out procedures flexibly in mathematical exercises</td>
<td>PF</td>
<td>39</td>
</tr>
<tr>
<td>17</td>
<td>a8: Developing students’ comprehension of mathematical operations</td>
<td>CU</td>
<td>37</td>
</tr>
<tr>
<td>18</td>
<td>a4: Identifying algorithms and skills included in the mathematical content</td>
<td>PF</td>
<td>34</td>
</tr>
<tr>
<td>19</td>
<td>a15: Teaching problem solving techniques (steps)</td>
<td>SC</td>
<td>33</td>
</tr>
<tr>
<td>20</td>
<td>a1: Identifying the mathematical concepts included in the mathematical content</td>
<td>CU</td>
<td>25</td>
</tr>
</tbody>
</table>


useful, and worthwhile” (a22), ranked eighth (48%), and “enhancing students’ belief in one’s own efficacy” (a24), ranked ninth (47%).

Comparing items associated with “conceptual understanding” domain, Table 6 shows that some items have a lower ranking in the first top10, such as “teaching to amend alternative concepts” ranked eighth (a16, 48%), “making connections between mathematical concepts and procedures to reach mathematical generalizations” ranked ninth (a30, 47%), and “applying specific strategies for teaching mathematical concepts” ranked tenth (a2, 46%). At the same time, some items related to the same domain of “conceptual understanding” have a very low ranking, such as “developing conceptual understanding for students”, which is ranked fifteenth (a7, 40%), and “developing students’ comprehension of mathematical operations”, which is ranked seventeenth (a8, 37%). Moreover, the last item, in the same domain of “conceptual understanding”, shows that a lower percentage of teachers (25%) perceived professional development needs for developing their skills in “identifying the mathematical concepts included in the mathematical content” (a1).

In addition, Table 6 demonstrates that although some items related to the “adaptive reasoning” domain had higher percentage of perceived needs as demonstrated by the respondents (a3, a32), the majority of the items related to the same domain had a middle-ranking, in that some were ranked tenth (46%), such as “developing logical thinking for students” (a6), “developing deductive reasoning for students” (a9), and “modeling mathematical problems in daily life situations” (a29), and others were ranked eleventh (45%), such as “enhancing students’ skills in approximation, estimation, and prediction” (a33) and “teaching mathematical patterns” (a35).

For the “strategic competence” domain, Table 6 reflects a variety of the respondents’ needs, ranking eighth, such as “developing students’ ability in formulating word problems” (a5, 48%) and tenth (46%), such as “developing students’ skills in problem solving strategies” (a17), and “enhancing students’ skills in problem solving” (a21). In contrast, another item received a low ranking
(nineteenth place), whereby only 35% of the respondents perceived professional development needs for “teaching problem solving techniques (steps)” that related to the same domain.

Table 6 reveals that most items related to the “procedural fluency” domain have the lowest ranking, representing fewer perceived needs for “developing students’ competencies in carrying out procedures flexibly in mathematical exercises” (a13, 39%), which was ranked sixteenth, and for “identifying algorithms and skills included in the mathematical content” (a4, 34%), ranked eighteenth.

Findings Related to the Second Research Question

The second research question explored whether there were statistically significant differences in perceptions of mathematics teachers’ professional development needs related to the SMP, specifically with regard to the effect of demographic variables such as the teacher’s qualifications, grade level taught, and years of teaching experience.

To examine if there are statistically significant differences related to the effect of the grade level taught, a one-way analysis of variance (ANOVA) was utilized. Mathematics teachers were grouped according to the grade level taught (primary, preparatory, and secondary). The one-way ANOVA revealed no statistically significant differences related to grade level taught for each SMP in particular or for mathematical proficiency as a whole. For example, for conceptual understanding, the one-way ANOVA revealed no statistically significant difference: $F(2, 338) = 0.890, p = 0.412$. In addition, for total mathematical proficiency, the one-way ANOVA revealed no statistically significant difference: $F(2, 338) = 0.637, p = 0.530$. This result suggests that teachers who teach primary, preparatory, and secondary grade levels have similar needs.

A one-way ANOVA was also utilized to examine whether there were statistically significant differences related to the effect of teacher qualifications. Mathematics teachers were grouped according to their education levels (bachelor, higher diploma, and master or PhD). The one-way ANOVA revealed there were no statistically significant differences related to teachers’ qualifications for all strands of mathematical proficiency and for mathematical proficiency as a whole. For example, for productive disposition, the one-way ANOVA revealed no statistically significant difference: $F(2, 337) = 0.80, p = 0.45$. In addition, for the total mathematical proficiency, the one-way ANOVA revealed no statistically significant difference: $F(2, 337) = 0.32, p = 0.73$. This result suggests that teachers who have baccalaureate degrees, higher diplomas, or even master-level or doctorate degrees have similar needs.

To examine if there were any statistically significant differences related to the effect of number of years of teaching experience, a one-way ANOVA was utilized. Mathematics teachers were grouped according to years of teaching experience (1-3 years, 4-6 years, 7-11 years, 12-18 years, and more than 18 years). The one-way ANOVA revealed that there were statistically significant differences with a medium effect size (0.04-0.06) related to years of teaching experience for all components of SMP: $F(4, 335) = 3.39, p = 0.01$ for conceptual understanding, $F(4, 336) = 4.938, p = 0.001$ for procedural fluency, $F(4, 336) = 4.678, p = 0.001$ for strategic competence, $F(4, 336) = 4.049, p = 0.003$ for adaptive reasoning, and $F(4, 335) = 3.609, p = 0.007$ for productive disposition. For mathematical proficiency as a whole, the finding was $F(4, 335) = 4.561, p = 0.001$. This result suggests that mathematics teachers’ needs differ based on their teaching experience.

A post hoc test (Tukey HSD) was utilized to determine exactly where the means differed. The post hoc test revealed that teachers with experience ranging from 4 to 6 years ($p = 0.003$) and from 7 to 11 years ($p = 0.012$) perceived more professional development needs, with statistically significant differences compared with other teachers with less experience (from 1 to 3 years) or with more experience (more than 18 years), for each strand in particular and for the whole SMP in general. One exception is for teachers with experience from 4 to 6 years, who perceive more needs related to conceptual understanding, with statistically significant differences ($p = 0.026$) when compared with the other groups of mathematics teachers.

The above results reveal that there were no statistically significant differences among teachers due to teachers’ qualifications or grade level taught, while statistically significant differences were found in terms of years of teaching experience. To investigate further, we used the top 3 box scores according to teachers’ qualifications, grade level taught, and years of teaching experience to explore trends or tendencies in each group. The results of the top 3 box scores show some differences regarding the percentage of perceived professional development needs as demonstrated by the respondents of different groups in some domains.

For example, item a3 “developing inductive reasoning for students” was ranked first in terms of perceived needs and relates to the “adaptive reasoning” domain. As shown in Figure 1, the results of the top 3 box scores by grade level taught revealed that the primary teachers perceived more needs (62%) compared to the other groups, with fewer perceived needs for secondary teachers (52%). For “using conceptual maps in teaching mathematics primary”, which relates to the “conceptual understanding” domain. The results show equivalent perceived needs for primary and preparatory teachers (61%), while secondary teachers perceived fewer needs (48%).

11 / 18
Figure 1 shows the equivalent perceived needs for teachers in all groups regarding “enhancing students’ belief in diligence in learning mathematics” in relation to the “productive disposition” domain. For items ranked last, the results show differences in perceived needs between the different groups. For example, as shown in Figure 1, equivalent perceived needs were found for teachers in different groups for “identifying algorithms and skills included in the mathematical content”, which relates to the “procedural fluency” domain. In the “strategic competency” domain, teachers’ needs for “teaching problem solving techniques (steps)” differed between different groups. The results show that preparatory teachers perceived fewer needs (28%) compared to other groups, with more needs found for primary teachers.

The results from the Top 3 box scores by teachers’ qualifications also showed different percentages regarding perceived needs in different groups. As shown in Figure 2, in all items related to the different domains, teachers with a master’s or Ph.D. qualification perceived fewer professional development needs. For some items, the result showed equivalent perceived needs between teachers who had a bachelor’s degree and those who had a post graduate degree, such as their needs regarding “using conceptual maps in teaching mathematics” and “teaching problem solving techniques (steps)”.

The results of the Top 3 box scores by years of teaching experience also revealed differences regarding teachers’ perceived needs in different groups. As shown in Figure 3, teachers with more experience perceived fewer needs related to the presented items in all the domains. In addition, the results showed more perceived needs for teachers who had 7-11 years’ experience for most items compared to the other groups, such as in “developing inductive reasoning for students”, which relates to the “adaptive reasoning” domain. Likewise, those with less experience also showed more perceived needs compared to the more experience groups in the “using conceptual maps in teaching mathematics”, which relates to the “conceptual understanding” domain and in the “teaching problem solving techniques (steps)”, which relates to the “strategic competence” domain.

Figure 3 also shows that teachers with 4-6 years of experience had the highest percentage (63%) of perceived needs compared to other groups for “enhancing students’ belief in diligence in learning mathematics”, relating to the “productive disposition” domain. Figure 3 also shows other findings regarding teachers’ need for “identifying algorithms and skills included in the mathematical content”, relating to the “procedural fluency” domain, whereby the highest percentage was for teachers with 1-3 years of teaching experience.

**DISCUSSION**

As the review of the literature demonstrated, there is no doubt that investigating teachers’ perceptions regarding their need for professional development related to SMP is an important issue for educators and researchers, strongly emphasizing the importance of reforming mathematics education programs. In addition, researchers and educators in the field of mathematics education have developed the concept of successful mathematics learning, leading to the concept of mathematical proficiency. Hence, this study explored mathematics teachers’ needs related to the strands of mathematical proficiency.
The results of the study found that the overall mean score for the scale was 2.52, representing relevant professional development needs with statistically significant differences related to the SMP as a whole and for all strands of mathematical proficiency. In addition, the mean score for the strands of mathematical proficiency varied between 2.45 and 2.60. Statistically significant differences were found for the different strands of mathematical proficiency, representing slight variation in mathematics teachers' perceived needs for professional development. These results support the importance of current research identifying critical domains for future professional development of mathematics teachers.

The results of the study also demonstrated that productive disposition had the highest mean score (2.60), representing the greatest need for professional development. This result resonates with Shulman (2015), who addressed one of the limitations of pedagogical content knowledge (PCK), originally conceived as being devoid of emotion, feelings, and motivation. Based on the descriptive rubric provided with the questionnaire, these results show that teachers know little about productive disposition and cannot apply strategies to...
achieve it. In particular, the results showed that teachers perceived a need to know how to enhance students’ habitual inclination to see mathematics as sensible, useful, and worthwhile. Of similar importance was their interest in enhancing students’ belief in their own efficacy, building positive attitudes towards mathematics, and enhancing student belief and diligence in learning mathematics.

This finding shows that productive disposition is the area of mathematics proficiency that requires the most attention for teachers. I suggest that one possible reason for this finding is that teaching as a profession has traditionally been concerned with instruction, but teachers themselves would like that to change; based on the findings, the first priority for teachers in this study was having mathematics make sense. This includes belief in the intrinsic value of mathematics, creating effective learners, and building positive attitudes and positive emotions towards mathematics learning. This is consistent with the work of Shriki and Lavy (2011), who addressed teachers’ need for greater interaction with their students. Studies that further support these findings (Fang, 2012; Shriki & Patkin, 2016) show that mathematics teachers need to build positive attitudes towards the learning of mathematics.

The findings of the study also indicated that the following needs were relevant to adaptive reasoning, with a mean score of 2.56. Mathematics teachers perceived needs for professional development in improving the following student skills: inductive reasoning, estimation and prediction, approximation, logical thinking, deductive reasoning, and mathematical thinking skills. Reflecting on their own activities, they focused on the following: modeling mathematical problems in daily life situations, enhancing mathematical proofs, and the teaching of mathematical patterns. This result reflects the perception that mathematics teachers see a need to develop higher-level thinking skills in their students. This may be because teachers found it difficult to enhance student capacity in engaging in logical thought, reflection, explanation, and justification. This result aligns with Shriki and Patkin (2016), who found that teachers should achieve basic teaching skills for developing students’ capability to present mathematical arguments and justification and develop mathematical thinking skills and reflective abilities. Polly (2011) gives further support to this idea, demonstrating that there is a need for teachers to develop their students’ adaptive reasoning skills, such as those demanding higher-level thinking. Fang (2012) addressed the need to enhance student ability to abstract or generalize mathematical ideas. Other researchers have cited the need to enhance the ability to overcome difficulties with mathematical proofing (Steele & Rogers, 2012; Superfine & Li, 2014).

Mathematics teachers’ needs related to conceptual understanding were ranked in the middle for professional development, with a mean score of 2.49. They perceived a need to apply these specific strategies: teaching mathematical concepts, teaching to amend alternative concepts, teaching by using multiple mathematical representations, and measuring student acquisition of mathematical concepts. The results demonstrated teachers’ needs relating to understanding how to teach mathematical concepts via problem solving and using conceptual maps in teaching mathematics. A need was identified for developing student ability in forming connections between relations in mathematics and making connections between mathematical concepts and procedures to reach conclusions. However, this sample of mathematics teachers perceived fairly relevant needs in identifying the mathematical concepts included in mathematical content, developing conceptual understanding for students, and developing student comprehension of mathematical operations. This result demonstrated that teachers have some knowledge of these areas yet limited experience in their application in the teaching of mathematics. This is consistent with other studies that addressed teachers’ need to acquire different teaching skills or knowledge that may enhance students’ conceptual understanding (Fang, 2012; Polly, 2011; Shriki & Lavy, 2011; Superfine & Li, 2014).

The fourth priority for mathematics teachers in this study was related to strategic competence, with a mean score of 2.45. This may refer to the type of strand centered more specifically on developing problem-solving skills within the curriculum. Most classes approached problem solving with relation to different topics specified in the curriculum; on the other hand, some classes addressed problem-solving strategies at the end of the unit. The results of the study demonstrated mathematics teachers’ need to develop student ability in problem-solving and associated strategies as well as representing mathematical problems. Other studies have highlighted the need for teachers to master teaching skills that help their students develop their problem-solving skills (Fang, 2012; Evans, 2012; Evans, 2014; Superfine & Li, 2014). However, teachers perceived fairly relevant needs in how to teach problem-solving techniques (steps). This may be because this skill is a mandatory part of the curriculum.

The results of the study showed that the lowest mean score was 2.45, related to procedural fluency. This may reflect teacher’s practices in the mathematics classroom, where opportunities are given to develop student skills in carrying out mathematical procedures in a flexible, accurate, efficient, and appropriate way. This subsequently gives the students more chances to practice drill exercises, helping them develop mathematical algorithms and skills.

Using the top 3 box scores to report and analyze the scale questions enabled the research findings to be more informative. Based on the descriptive rubric of the rating...
scale presented in the current study, the results offer more insights regarding teachers’ needs in terms of specific knowledge and experience. The results also revealed the top six items representing the most essential perceived needs that were demonstrated by more than half of the respondents. In the “adaptive reasoning” domain, essential needs were “developing inductive reasoning for students” and “enhancing mathematical proof for students”. For the “conceptual understanding” domain, the results showed that “using conceptual maps in teaching mathematics” and “teaching by using multiple mathematical representations” were also ranked within the top six perceived needs. The results also revealed additional essential needs for more than half of the respondents associated with the “procedural fluency” domain, including “enhancing students’ procedural fluency in mathematical operations”, and needs associated with the “productive disposition” domain, with perceived needs for “enhancing students’ belief in diligence in learning mathematics”. These results are sensitive and crucial to planning professional development programs and workshops that meet teachers’ needs. For example, for better planning of Qatari teachers’ professional development programs in the “productive disposition” domain, educators and mathematicians should be more aware regarding teachers’ needs in “building positive attitudes towards mathematics”, “enhancing students’ habitual inclination to see mathematics as sensible, useful, and worthwhile”, and “enhancing students’ belief in one’s own efficacy.”

For the “conceptual understanding” domain, the results highlighted teachers’ needs regarding knowledge and skills for “teaching to amend alternative concepts”, “making connections between mathematical concepts and procedures to reach mathematical generalizations”, and “applying specific strategies for teaching mathematical concepts”. In addition, the results of the study underlined some teaching skills related to the “adaptive reasoning” domain, such as “developing logical thinking for students”, “developing deductive reasoning for students”, and “modeling mathematical problems in daily life situations.”

The results of the study demonstrated that there were no statistically significant differences related to teachers’ qualifications. This result could be explained by the majority of participating teachers having a bachelor’s degree (81.8%). This result is supported by Fang (2012), who found no effect on teachers’ perceived needs due to their educational background. Despite this finding, using the top 3 box scores according to teachers’ qualifications revealed that teachers with high qualifications perceive fewer professional development needs. This finding could be explained by the positive effect of continuous learning for teachers.

In addition, results of the study revealed no statistically significant differences linked to grade level taught. From the researcher’s experience, one possible reason for this is that teachers at all levels may be supported by similar professional programs, with little concern for their needs or the grade level they teach. However, the research findings aligned with Shriki and Patkin (2016), who found minimal significance in perceived needs according to academic education or grade level taught. In addition, based on the results reported by the top 3 box scores regarding years of teaching experience in the current study, there are some differences regarding the percentages of the perceived professional development needs demonstrated by respondents of different groups in some domains. For example, primary teachers perceived more professional development needs for “developing inductive reasoning for students” and “using conceptual maps in teaching mathematics primary” compared to the other groups. This could be due to the type of the mathematical content taught in primary school, such as introducing primary mathematical concepts, and teachers’ awareness in developing inductive reasoning for students in the early years.

One of the most interesting findings is that statistically significant differences were found with regard to years of teaching experience. Results found that teachers who have teaching experience from 4 to 6 years and from 7 to 11 years perceived more professional development needs, with statistically significant differences compared with less-experienced colleagues (1-3 years) or even very experienced colleagues (more than 18 years). This was found across most strands of mathematical proficiency, with the exception of conceptual understanding, wherein the differences are statistically significant only for teachers with teaching experience of 4-6 years and no other groups. I suggest that this finding in general reflects that teachers in this period of experience are generally starting to identify their actual needs related to the SMP. The reason for the exception regarding teachers’ needs related to conceptual understanding could be explained because of this range of experience 4-6, where teachers become more aware of the importance of developing students’ conceptual understanding, which requires less development time compared with other strands.

For teachers with less experience, this could be because of the type of undergraduate programs they completed, the content of which has helped them to acquire knowledge and skills that match new pedagogical trends in mathematics education to capture the SMP. On the other hand, this result may indicate a lack of awareness regarding the teachers’ own professional development needs. In addition, results showed that teachers with more than 18 years of teaching experience perceived less need for professional development; this could be explained either by their rich experience in the field or because they have become less enthusiastic in participating in even more professional development programs.
CONCLUSIONS

This study investigated mathematics teachers’ perceptions of their professional development needs related to the five Stands of Mathematical Proficiency (SMP). The research instrument developed in this study demonstrated high validity and reliability across the SMP. It is recommended that researchers use this research instrument in the field of mathematics education research to explore teachers’ perceptions of their professional development needs. This research instrument could also be developed to be used as a qualitative research tool to examine mathematics teachers’ needs. In addition, there is a need to develop qualitative research studies by conducting classroom observations or interviews for more in-depth research addressing the SMP.

Accounting for a variety of variables such as qualifications, grade level taught, and number of years of experience, this study found professional development needs for mathematics teachers related to all five SMP. This study demonstrated the need for and importance of conducting professional development programs for mathematics teachers that meet their needs. Teachers will be more enthusiastic about attending such tailored programs, which will maximize the impact on their development and may lead to effective ways of teaching. In turn, this will benefit student mastery of mathematics learning.

Based on the analysis in this study, the priority of professional development needs from the point of view of mathematics teachers demonstrated the need to provide teachers with professional development programs relevant to productive disposition, followed by adaptive reasoning, conceptual understanding, and strategic competence, and ended by procedural fluency consequently. It is recommended that teachers be provided with professional developmental programs based on these priorities.

The results offer more insight into mathematics teachers’ most essential needs in terms of specific knowledge and experience within different categories. This information aids in planning professional development programs and workshops that will meet teachers’ needs.

Some results were not expected, such as there being no significant differences found with regards to grade level taught and teacher qualifications. More in-depth qualitative research is recommended to identify the effect of such factors.

One interesting finding in this study is that the number of years of experience for mathematics teachers resulted in different needs, where teachers with fewer years of experience perceived fewer needs compared with more experienced colleagues. More research is recommended to examine whether this result is due to the type of undergraduate programs teachers have attended. In particular, there should be a focus on whether their undergraduate programs helped them to acquire knowledge and skills that match new trends in mathematics education to capture the SMP, or if they simply have a relative lack of awareness of their professional development needs.

REFERENCES


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