Mathematical Problem-Solving Processes of Students with Special Needs: A Cognitive Strategy Instruction Model 'Solve It!'

Ufuk Özkubat¹*, Alpaslan Karabulut², Emine Rüya Özmen³

Abstract

Being a cognitive strategy instruction model called 'Solve It!' involves cognitive and metacognitive elements. The model was developed by Montague (1992) as one of the process-based teaching strategies. The purpose of 'Solve It!' strategy is to teach the following seven cognitive strategy steps: read, paraphrase, visualize, hypothesize, predict, calculate, and check. Each cognitive strategy step has the following three metacognitive steps: ask, say, and check. 'Solve It!' strategy has been used to teach students with special needs on how to solve word problems.

Introduction

Mathematics is defined as a symbolic language in which people can share their thoughts about the amount of something with each other (Miller, Butler, & Lee, 1998; Rivera, 1997). It is also considered a universal language throughout the world. Mathematics includes counting, measurement, arithmetic, computation, geometry, and algebra with the ability to think about situations related to a given quantity (Cawley, Parmar, Yan, & Miller, 1998). The following four fields were identified by National Council of Teachers of Mathematics (2000) as the basic mathematics fields: problem solving, reasoning, communication, and interaction with the real world. By defining basic mathematics components, the association considers problem solving as an important component of mathematics (Parmar & Cawley, 1997; Rivera, 1997). Although there are many definitions on the concept of problem solving, it is generally defined as a process that usually includes problem solving, combining, and analyzing skills (Cawley & Miller, 1986). Additionally, problem solving includes one and/or more than one step (Fuchs et al., 2004), and requires the differentiation of the calculations to be used in the solution process (Carpenter et al., 1993). The concept of problem solving may also contain information that is rarely unrelated or distracting (Passolunghi, Marzocchi, & Fiorillo, 2005).

Many models on the problem-solving process have been developed since 1945 (Krawec, 2010). Among them, Polya (1957), Mayer (1985), and Montague (1992) have been cited by several studies in the relevant literature using mathematical problem-solving models (Karabulut & Özkubat, 2019). The first mathematical problem-solving model was defined by George Polya in 1945. Polya's (1957) four basic steps proposed to solve mathematics problems are as follows: understanding the problem, planning, applying the plan, and controlling (backview). Another mathematical problem-solving model was developed by Mayer (1985). His model consists of two basic stages as follows: describing and solving the problem. Each step consists of four steps and two sub-steps (Krawec, 2010). These sub-steps are converting, merging, planning, and executing. The two problem-solving models have been considered important but are not described as 'innovative' in today's world (Sweeney, 2010). It is stated that in effective problem solving, the underlying power is metacognition defined as successfully completing a task and keeping track of him/herself by being aware of his/her own thought processes with the control of his/her own performance (De Corte, Greer, & Verschaffel, 1996). The problem solvers using metacognition strategies can plan effectively and monitor their own performance in the solution process (Montague & Applagate, 1993). In the context of this study, with the addition of metacognition strategies in the problem-solving process, problem solving was observed as a skill that includes not only cognitive processes but also the metacognitive processes. In this respect, Montague's problem-solving model provides a combination of cognitive and metacognitive strategies.

Montague (1991) stated that the model of effective problem solving in mathematics emerged as a result of her research on which the relevant effective variables in problem solving were examined. Those variables can be listed as follows: the usual problem solving, a solution of a mathematical problem, self-regulation, and successful problem solving (Montague, 1991). In this context, Montague (1991) examined the cognitive and metacognitive knowledge of problem solving, and the problem-solving processes of twice exceptional students, who have the combination of being gifted with superior ability and learning difficulties. In light of the study findings, cognitive and metacognitive strategies, and operations used by students who are proficient in problem solving were included in Montague's problem-solving model (Montague, Applegate, & Marquard, 1993). Montague problem-solving skills require the use of cognitive and metacognitive strategies and procedures (Montague, 1992). Montague (1992) defined the seven cognitive strategies and calculations to solve a prob-

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The 'Solve It!' strategy consists of a few steps and each step includes self-instruction, self-questioning, and self-monitoring strategies (e.g., say, ask, check). In other words, the 'Solve It!' strategy is a strategy that aims to teach the seven cognitive strategy steps, and three metacognitive strategy steps within each cognitive strategy step. In this strategy, students are taught to read the problem carefully, express the problem with their own words, analyze the information, develop a plan, solve the problem, and control the solution (Reid & Lienemann, 2006). In this context, the strategy of 'say, ask, check' that involves the cognitive and metacognitive processes and strategies to solve a problem is presented in Table 1.

Students learn seven cognitive strategies and processes to solve mathematical problems effectively with the help of the first letters of cognitive strategies through the strategy of 'Solve It!': read, paraphrase, visualize, hypothesize, estimate, compute, and check (RPV-HECC). Accurate realization of these cognitive processes is made possible by using the correct cognitive strategies (Montague, 1992). In the process of problem solving, cognitive strategy should be used to enable the cognitive process called 'understanding' to read a problem. Whether a problem is correctly comprehended by the students or not can be realized using 'paraphrasing the problem' cognitive strategy, and the use of 'conversion' cognitive process. Similarly, the use of the cognitive strategy 'calculation' needs to be applied in the cognitive process called 'computing' for a problem. While the metacognitive strategies are listed as self-instruction, self-questioning, and self-monitoring; the metacognitive processes are defined as the knowledge of strategy, the use, and control of it. In the model, the metacognitive strategies are not memorized with the help of a reminder, but they are only used to monitor students' own problem-solving practices (Montague, 1992). The cognitive and metacognitive strategies and processes are illustrated in Figure 1.

The 'Solve It!' strategy was first published as a book to support the curriculum of mathematics in 2003 (Montague et al., 2014). However, related studies were conducted long before 2003 (Montague, 1984; Montague, 1992; Montague & Bos, 1986). These studies claimed that 'Solve It!' strategy improved students' problem-solving performance by using different research designs such as experimental designs, single subject experimental designs, semi-experimental designs, and random clustering designs. The first study to test the effectiveness of the 'Solve It!' strategy was conducted by Montague and Bos (1986). The 'Solve It!' strategy was applied to six fourth-grade high school students with limited mathematical skills. The findings of the study using a multiple baseline design across individuals from single-subject experimental designs revealed that all participants' problem-solving performance were developed and that they were able to generalize their strategies to different and more difficult problems. Besides being the first study, the study was also important because it specified the cognitive strategy steps in the 'Solve It!' strategy. As a matter of fact, Montague (1984) mentioned eight cognitive strategy steps in the problem-solving process in her thesis. This strategy step is the 'state the problem' step that this study does not have in the current model. Following this research, the cognitive strategy steps remained valid, and the number of cognitive strategy steps taken in the 'Solve It!' strategy has been determined as seven. In the second study, Montague (1992) examined the effectiveness of the following two components: teaching cognitive and metacognitive strategies in the problem-solving process. Six middle school students with learning disabilities participated in the research. The intervention was completed in two phases. In the first stage, half of the participants participated in cognitive strategy teaching, while the other half participated in metacognitive strategy teaching. In the second stage, the participants participated in both practices. The research findings revealed that students who were taught cognitive strategies quickly went to the stage of mastery. In addition, problem-solving performance of all students involved in the study was developed in one-, two-, and three-step mathematical problems.

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Figure 1. Montague Mathematical Problem-Solving Model

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test and post-test results, the intervention group students started to use more strategies than the comparison group students. The average achieving group students compared to those with learning disabilities were reported to use different and more strategies in the problem-solving process. After the implementation, all students in the intervention group showed significant improvement compared to their peers in the comparison group. Moreover, Montague et al. (2011) examined the effect of 'Solve It!' interventions on the problem-solving performance of 7th grade students. The findings revealed that the mathematical performance of low and average level students with learning difficulties in the intervention program increased more than those of their peers in the comparison group. Moreover, Montague et al. (2014) examined the effect of 'Solve It!' interventions on the problem-solving performance of 7th grade students. The students who participated in the study were divided into the following three groups: low level, average level, and students with learning difficulties. They were examined in intervention and comparison groups according to their average mathematical performance and socioeconomic status. The group of participants consisted of 86 students with learning difficulties and 973 students with low and average achieving. Students who were in the intervention group participated in the following teaching stages: activating the pre-knowledge

<table>
<thead>
<tr>
<th>Cognitive strategy and the steps of the operation</th>
<th>The metacognitive strategy <code>say, ask, check</code></th>
<th>Examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>Read (for understanding)</td>
<td>The aim of say (self-instruction): The student reads the question carefully before implementing an operation.</td>
<td>Say: I will read the question, and if do not understand it, I will read it till I do.</td>
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<tr>
<td></td>
<td>The aim of ask (self-questioning): Has the student fully understood the question which has been directed to him/her?</td>
<td>Ask: Now that I have read the question, have I fully understood it?</td>
</tr>
<tr>
<td></td>
<td>The aim of check (self-monitoring): If the student has understood the question, he/she can start solving it.</td>
<td>Check: I have understood the problem. Now I can proceed.</td>
</tr>
<tr>
<td>Paraphrase (your own words)</td>
<td>The aim of say (self-instruction): To state that he/she has understood, the student paraphrases.</td>
<td>Say: I will underline the words that are related to the problem. I will paraphrase the question.</td>
</tr>
<tr>
<td></td>
<td>The aim of ask (self-questioning): Does the student have the ability to the question being asked to him/her?</td>
<td>Ask: Have I underlined the most important features or words in the problem?</td>
</tr>
<tr>
<td></td>
<td>The aim of check (self-monitoring): Make sure that highlighted keywords are relevant.</td>
<td>Check: I have found the necessary words and features they will help me solve the problem.</td>
</tr>
<tr>
<td>Visualize (a picture of a diagram)</td>
<td>The aim of say (self-instruction): Students draw to reinforce their understanding of the problem.</td>
<td>Say: I will draw a diagram of the problem.</td>
</tr>
<tr>
<td></td>
<td>The aim of ask (self-questioning): Is there any compatibility between the problem and drawing?</td>
<td>Ask: Do my drawings represent the problem?</td>
</tr>
<tr>
<td></td>
<td>The aim of check (self-monitoring): The drawing includes visual key concepts related to the mathematics problem.</td>
<td>Check: The drawing contains the basic parts of the problem.</td>
</tr>
<tr>
<td>Hypothesize (a plan to solve the problem)</td>
<td>The aim of say (self-instruction): Student creates a plan for solving the problem.</td>
<td>Say: I am going to make a plan to solve the problem.</td>
</tr>
<tr>
<td></td>
<td>The aim of ask (self-questioning): Which plan helps a student solve the problem?</td>
<td>Ask: What about the first step in this plan? What about the next step in the plan?</td>
</tr>
<tr>
<td></td>
<td>The aim of check (self-monitoring): The plan is suitable for solving this problem.</td>
<td>Check: My plan has the necessary steps to solve this problem.</td>
</tr>
<tr>
<td>Estimate (predict the answer)</td>
<td>The aim of say (self-instruction): Student evaluates value for estimating the answer or uses other strategies.</td>
<td>Say: I will guess what the correct answer of the problem is.</td>
</tr>
<tr>
<td></td>
<td>The aim of ask (self-questioning): Which prediction strategy does the student use to predict the answer?</td>
<td>Ask: In my estimation, which numbers can be used to solve the problem?</td>
</tr>
<tr>
<td></td>
<td>The aim of check (self-monitoring): All of the important problem information was used to estimate the correct answer.</td>
<td>Check: I have not missed any important information in my estimation.</td>
</tr>
<tr>
<td>Compute (do the arithmetic)</td>
<td>The aim of say (self-instruction): Student will be able to follow the plan to calculate the solution of the problem.</td>
<td>Say: Do the operations in the right order.</td>
</tr>
<tr>
<td></td>
<td>The aim of ask (self-questioning): Is the answer consistent with the prediction made?</td>
<td>Ask: How many steps are needed? Are the operations in the right order?</td>
</tr>
<tr>
<td></td>
<td>The aim of check (self-monitoring): The steps in the plan were followed and completed in the correct order.</td>
<td>Check: I have done all the work in the correct order to solve the problem.</td>
</tr>
<tr>
<td>Check (make sure everything is correct)</td>
<td>The aim of say (self-instruction): Student reviews the calculation steps to verify the answer.</td>
<td>Say: I will review the steps of the calculation.</td>
</tr>
<tr>
<td></td>
<td>The aim of ask (self-questioning): Did the student check all the steps to solve the problem and were all the calculations correct?</td>
<td>Ask: Have I reviewed every step in my answer and checked my work?</td>
</tr>
<tr>
<td></td>
<td>The aim of check (self-monitoring): The problem solution seems to be done correctly.</td>
<td>Check: I have done all the steps in the correct order to solve the problem. If I have not done, I will check the previous steps, I will ask for help when I need to.</td>
</tr>
</tbody>
</table>
for the implementation of the strategies and procedures required for problem solving, discussing the strategy, explaining the strategy, and describing how these strategies will help the improvement of the problem-solving skills, using the strategy appropriately with examples, using self-regulation strategies independently to follow their performance up three times a week for eight months until the problem-solving process was completed. The findings showed that the performance of the students in the intervention group increased compared to the performance of the comparison group, and especially the low achieving students’ performance differed significantly compared to the peers in the comparison group.

Research on students with learning disabilities also revealed that the ‘Solve It!’ strategy was used to improve students’ problem-solving performance and it was found as an effective strategy (Daniel, 2003; Krawec et al., 2013; Montague, 1984; Montague, 1992; Montague et al., 2014; Montague & Bos, 1986; Montague et al., 2011). Research showed that the ‘Solve It!’ strategy could be taught by clear expressions by following the generalization stages, being a model, voiced thinking, implementing guided and independent practices. It was also emphasized that cognitive and metacognitive strategies applied in problem-solving processes improve the mathematical skills of students with learning disabilities.

Studies have indicated that students develop problem-solving skills and generalize the learned strategy to other disciplines by systematically presenting and following the strategies of teaching steps (Smith & Alley, 1981). Some studies showed that process-based teaching is not only effective in helping students with different types of problems (Bennet, 1982) but also effective in improving students’ abilities to express problems and self-instruction to develop problem-solving skills (Case & Harris, 1988). Based on these findings, it is safe to say that the ‘Solve It!’ strategy teaches students how to implement the problem-solving process and the strategies it includes because it is a process-based problem-solving strategy and designed to teach the metacognitive activities associated with each cognitive process (Montague et al., 2014). The results about the effectiveness of studies examining students with learning disabilities showed that the ‘Solve It!’ strategy should be implemented on the students with disabilities, such as autism spectrum disorder (Whitby, 2012), intellectual disabilities (Chung & Tam, 2005; Karabulut, 2015; Karabulut & Özmen, 2018), and spina bifida (Coughlin & Montague, 2011) to enable them to improve their problem-solving performance. Stating that the number of students with autism spectrum disorders increased faster than all other disabled groups, Whitby (2012) maintained that there is a need for effective teaching strategies that can be applied to students with autism spectrum disorders and analyzed the effectiveness of the ‘Solve It!’ problem strategy in solving math problems.

Three middle school students with autism spectrum disorders were included in the study in which multiple baselines were used across participants design. As a result of the ‘Solve It!’ strategy, the problem-solving performance of the three students examined by this study increased. In this respect, Whitby (2012) asserted that ‘Solve It!’ strategy was an effective intervention in the development of problem-solving processes for students with autism spectrum disorder. Additionally, Chung and Tam (2005) applied Montague’s strategy (1992) by adapting the cognitive strategy teaching routines in their study with 30 students with mental disorders. In the study, the strategy teaching components developed by Montague (1992) (i.e., say, ask, and check) were adapted to the cognitive strategy teaching in Table 1. The students in the study were divided into three groups: traditional teaching, teaching via examples, and cognitive strategy teaching. It was revealed that the students in the cognitive teaching group made more progress than the students in other groups. Furthermore, Coughlin and Montague (2011) examined the effectiveness of the ‘Solve It!’ strategy to improve the math problem-solving performance of three students with spina bifida. The study used multiple baselines across individuals and included two steps of intervention. One-step mathematical problems were used in the first stage, while two-step mathematical problems were used in the second stage. According to findings, it appears that problem-solving performance of all participants have developed. Recent studies of Karabulut (2015) and Karabulut and Özmen (2018) aimed to examine the effect of the ‘Solve It!’ strategy on the problem-solving performance of students with mild intellectual disabilities. It was observed that students changed their use, and control of their problem-solving strategies and information qualitatively; in addition, they were able to generalize the strategies they used to solve different types of problems and maintain the generalizations.

Studies on students with spina bifida, autism spectrum disorders, and intellectual disabilities revealed that the ‘Solve It!’ strategy is an effective strategy on (Chung & Tam, 2005; Coughlin & Montague, 2011; Whitby, 2012). Poor organizational skills, such as planning, remembering previous knowledge, and self-control, which are associated with the autism spectrum disorder, affect their problem-solving performance (Happe, Booth, Charlton, & Hughes, 2006). Similarly, students with intellectual disabilities are limited in solving problems by understanding and using mathematical concepts because of their inefficient strategy repertoires (Xin & Jitendra, 1999). The low level of attention and inability to decide on the proper computing types of students with spina bifida have a negative effect on their performance in their problem-solving processes (Burmeister et al., 2005). In light of these findings, it would be safe to say that the ‘Solve It!’ strategy provides support to these students on how to interpret a math problem, how to analyze given information, how to develop a logical solution plan to solve a problem, and how to evaluate alternative solutions.

Only limited studies have examined the effects of intervention programs applied to support the problem-solving performance of students with special needs in Turkey (Baki, 2014; Karabulut, 2015; Karabulut & Özmen, 2018; Karabulut, Yılmaz, Özak, & Karabulut, 2015; Köl & Yılmaz, 2018; Özoys, 2005; Özsoy, 2017; Tuncer, 2009; Tufan & Akyut, 2018). In addition, there are no studies on identifying problem-solving processes of students with special (Özkubat, 2019; Özkubat & Özmen, 2018). The literature in Turkey on the ‘Solve It!’ strategy revealed that there are only two studies that aim to support the problem-solving performance of the students (Karabulut, 2015; Karabulut & Özmen, 2018). Therefore, a realization phase was reached on the importance of examining the studies related to the use of ‘Solve It!’ strategy, which is a mathematical intervention for students with learning disabilities, autism spectrum disorder, mental and physical disabilities in the international literature. Hence, planning the study, developing appropriate intervention programs and using scientific evidence in Turkey will be possible. This teaching strategy is only applied to mentally disabled students in Turkey; however, it is believed that this research will guide the use of this strategy to cover other types of disabilities, such as learning difficulties and autism spectrum disorders. In addition, this study will shed light on future studies by bringing a different perspective to the studies aiming to conduct on the ‘Solve It!’ strategy. In this respect, this study aimed to examine the studies using the ‘Solve It!’ strategy in terms of a number of variables.

Methodology

This study covers the research articles and dissertations published in journals using the applications of problem-solving interventions using the cognitive strategy teaching model ‘Solve It!’ including cognitive and metacognitive elements. This part of the study presented the necessary information about the criteria for inclusion of the articles and theses in this study, the literature review, coding of the articles and theses, descriptive analysis process, and the reliability of the coders.
Criteria for Inclusion

For the inclusion and non-inclusion of the articles and theses in this study, the following basic selection criteria were determined: a) The research group should include students with special needs, b) the study should include the intervention of the 'Solve It!' problem-solving strategy as an independent variable and, c) the study should be published in a national or international peer-reviewed journal. Criteria for the inclusion of the theses are as follows: a) The participant group of the theses should consist of students with special needs, b) the theses should include the intervention of the 'Solve It!' problem-solving strategy as an independent variable and, c) the theses should be master's theses and/or doctorate dissertations. Studies that did not provide the findings of special needs students after the intervention strategies were not included in this study.

Search Procedures

First of all, EBSCOhost, Education Research Complete, Education Resources Information Center (ERIC), Web of Science, Psychological Abstracts Index (PsycINFO), ULAKBIM National Databases (UVT), ProQuest Dissertations & Theses Global, Google, and Google Scholar search engines were used to determine the articles. The search was performed by entering keywords in specified search engines. The keywords were typed in Turkish and English. The following keywords were used: The 'Solve It!' math problem solving, math intervention, cognitive strategy instruction, math instruction, computation, and algebra, arithmetic. As a result of the scanning with the aforementioned keywords, 48 studies were obtained. Titles, summaries, and keywords of the studies were analyzed, and six chapters were obtained by eliminating book sections, reports. In addition to this step, the articles containing problem-solving interventions were included in the following key journals between 1990 and 2018: Exceptional Children, Learning Disabilities Quarterly, Journal of Learning Disabilities, Learning Disabilities Research & Practice, Remedial & Special Education, and Journal of Special Education.

Secondly, the keywords used in determining the articles and theses were searched using the ProQuest Digital Databases search engine in Turkish and English. As a result of the literature review, two more studies were included. Both studies were doctoral dissertations. In the third and final steps, the aforementioned keywords were searched through the Council of Higher Education’s National Thesis Center website to identify the graduate theses examining the 'Solve It!' strategy in Turkey; thus, one more study was included. Theses with electronic access were obtained from the Internet, and those with no electronic access were acquired from the libraries of the universities. The data were collected, and search filters were applied according to the Prisma Flow Diagram represented in Figure 2.

Article Coding and Reliability

The selection of articles and theses was made by considering the basic selection criteria for inclusion of articles and theses. First, a form has been created by taking the basic selection criteria into consideration. The first author read and examined 70% of the articles and theses in detail, while the second author read and examined 30% of them. They were then recorded in the assigned form. The review process was conducted by the first and second authors. As a result of the review, a total of 12 papers (nine articles and three dissertations) published in seven different journals that fit the pre-decided criteria were reached. Articles and theses included in the scope of the study are shown in the references part with (*). The reliability among coders in the study was calculated using the following formula: “Consen sus / [Consensus + disagreement] x 100” by comparing the 25% of the research results and data obtained by the first and second researchers.

Descriptive Analysis Process

The articles and theses were examined in accordance with the research review form developed by the researchers to evaluate the data at hand, a) the number of participants, b) class and age, c) gender, d) diagnosis of participants, e) target skill, f) research pattern, g) environment of the ap-

![Figure 2. Flow Diagram (The PRISMA Statement)](image-url)

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The effectiveness of the 'Solve It!' strategy, one-step problems (easy problems that can be solved in only one step), two-step problems (medium-level problems that can be solved in two steps), three-step problems (difficult problems that can be solved in three steps) was investigated in this study.

The Environments of Intervention

As can be seen in Table 3, the intervention environment of the research, the environment was distributed evenly. It appears that 27% of the studies (n= 3) were applied in support rooms, 27% of them were administered in education classrooms, and 27% of them were conducted in training support rooms initially and then in regular education classrooms. Besides, the intervention in two of the studies (19%), was performed in an empty classroom in the school.

Research Designs

Single-subject experimental patterns (n= 7, [58%]) and other experimental designs (n= 5, [42%]) were used by the reviewed studies. As for the research findings in terms of single-subject experimental designs, it appears that multiple baseline designs were used in four studies (33%) and multiple probe designs were used in three studies (25%). As for other experimental designs, it appears that the cluster-randomized design was used in two studies (17%), the pretest-posttest design was used in two studies (17%), and the cross-subject design was used in one study (8%).

Table 3. The Environments of the Intervention and Information about Designs Used

<table>
<thead>
<tr>
<th>Variables</th>
<th>f</th>
<th>%</th>
</tr>
</thead>
<tbody>
<tr>
<td>Single-subject experimental designs</td>
<td>Multiple baseline design</td>
<td>4</td>
</tr>
<tr>
<td></td>
<td>Multiple probe design</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>Total</td>
<td>7</td>
</tr>
<tr>
<td>Experimental designs</td>
<td>Cluster randomized design</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td>Pretest-posttest design</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td>Cross subjects design</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>Total</td>
<td>5</td>
</tr>
<tr>
<td>Environments</td>
<td>Support room</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>Support room/ Education classroom</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>Empty classroom</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>Total</td>
<td>12</td>
</tr>
</tbody>
</table>

The Results of Effectiveness

The examination of the visual graphics and written findings of 12 studies revealed that the 'Solve It!' strategy was effective in the acquisition of the targeted skills. The findings of the examination of the graphs of single-subject experimental designs in which the 'Solve It!' strategy was discussed showed that the curves at the starting level had an increase slope in the intervention phases. In other experimental designs, it was revealed that when the 'Solve It!' strategy was applied as a result of statistical operations, it had an effect on the acquisition of target behaviors.

Reliability

The inter-coder reliability among coders for the descriptive analysis process was 92% and ranged between 96.30- 96.60.

Discussion

This research aimed to examine the studies using the 'Solve It!' strategy by different variables. The examination of the reviewed studies revealed the following three basic findings: First, it is effective to use the 'Solve It!' strategy for the problem-solving abilities of students with learning disabilities, autism spectrum disorders, spina bifida, and intellectual disabilities. Second, the strategy has the potential to lead to progress in the problem-solving abilities of students with and without disabilities. Finally, more studies should be conducted for the purpose of supporting the problem-solving skills of students with special needs.

The findings of the diagnostic variables, in line with the descriptive analysis findings, revealed that the majority of the participants with special needs were students with learning...
disabilities. The limitations of the students with learning dis-
babilities in the field of mathematics skills are considered as
one of the main problems in the literature (Miller & Mercer,
1992). To solve such problems, students need to read the problem, decide what to do, solve the problem, and check the logic of their answers (Mont-
tague, Wager, & Morgan, 2000). Similarly, in the 'Solve It!' strategy, students are able to understand the mathematical problems, analyze the information given in the problem, de-
velop strategies to solve the problem, and evaluate the solutions (Montague, Wager, & Morgan, 2000). Therefore, it
would be safe to say that the 'Solve It!' strategy improves the students' problem-solving performance.

The processes are complex and sequential in problem-solv-
ing stages. In other words, the right solution requires the
correct implementation of the previous step makes this
process difficult for students with special needs (Jitendra et
al., 2009). Likewise, in this research the 'Solve It!' strategy in-
cludes the following steps: how to solve the problem, how to
interpret the problem with their own sentences, how to ana-
yze the information, how to develop a plan, how to solve
the problem, and how to check the solution (Montague et
al., 2014; Montague et al., 2011; Krawec et al., 2013). These
steps are sequential with each other (Reid & Lienemann,
2006). In addition, the teaching of metacognitive strategies is
associated with each cognitive process. Thus, students
learn to manage the process by using these strategies.

Solving math problems is considered a difficult skill for many
students because of the complexity of the problem-solving
processes (Jonassen, 2003; Schurter, 2002). The examina-
tion of the problem-solving teaching practices revealed that
the sequential steps that students have to take to solve the
problem are used and these steps do not cover the whole
problem-solving process all the time (Montague, 1992). Al-
though the stages representing this process show the stu-
dents the way to solve the problems, some steps are not
taken in practice and the metacognitive strategies which are
used to get self-monitoring and self-evaluation conducted
during the problem-solving process are not discussed thor-
oughly. It is not enough to know these stages to be a good
problem solver, especially for students with difficulties in
learning and managing their own learning processes, and
for those with limitations in their cognitive processes. So
as to say, the 'Solve It!' strategy enables students to learn the
problem-solving process through the steps involving the
entire process and the strategies to be used in these steps.
The purpose of the cognitive strategy teaching is to teach students to think and act like good problem solvers or
strategic learners (Montague, 2008). The cognitive routines
used in this teaching technique are conveyed to students
through loud thinking models, enabling the students' stra-
gy applications to be independent thanks to the appropri-
ate support, and immediate feedback on student's perfor-
ance provided through student and teacher interaction
(Güzel-Özmen, 2008). Students with special needs feel the
need to organize their own thinking processes (Krawec et
al., 2013; Montague et al., 2011; Montague et al., 2014). In
this context, one of the important components of the 'Solve
It!' strategy is supporters that can be expressed as proce-
dural facilitators (Chung & Tam, 2005; Montague, 2008).
The master problem solver's application of the strategy steps by
thinking loudly serves as a bridge between the students' exis-
ting skills and knowledge and their intended target
(Güzel-Özmen, 2006). The support provided at the begin-
ing of the strategy education is gradually withdrawn, and
finally, the student is able to implement the strategy inde-
dependently (Chung & Tam, 2005). Another important concept
in the 'Solve It!' strategy is the visualization strategies. The
visual strategies presented by students with special needs,
by organizing and presenting problem-solving steps to pro-
vide information about the problem due to the difficulties in
coordinating the working memory, are of great benefit
in solving the problem (Geary, 2004; Hughes et al., 2003).
Accordingly, visualization in the 'Solve It!' strategy increas-
es the students' understanding of the problem by bringing
various information together in the problem (Ives, 2007; Jit-
tendra et al., 2009; Van Garderen, 2007). In addition to the
fact that the visualization of the problems enables students
to solve the problems (Ives, 2007; Van Gardener, 2007), it
is also stated that this ensures that the information will be
stored and thus accelerate the processing of information by
identifying the problem (Kokinov et al., 2011). Short term memory problems of the students with special needs include
the problem of bringing information back to their minds immediately after hearing or seeing information
while the working memory problems arise from grouping
information and cognitive processing faults, such as coding
(Chung & Tam, 2005; Swanson & Jerman, 2006). In light of
this information, it can be stated that students with learning dis-
abilities can facilitate their math problem-solving processes by using the problem visualization strategy and supporting
their memories. Many students with special needs face fail-
ure in the field of mathematics (Jonassen, 2003). Therefore,
they can develop negative attitudes toward learning math-
ematics and the attitude toward mathematics is also supports the students in developing positive percep-
tions about problem solving through their implementation of
the strategies in the 'Solve It!' strategy. Indeed, studies
using the 'Solve It!' strategy (Daniel, 2003; Montague, 1992;
Whitby, 2009) revealed that there is a relationship between the
increase in the number of problem solving and the in-
crease in the performance of the applying the strategy, and
the attitude. It has been found that different teaching strat-
egies develop the attitude toward mathematics and math-
ematics problem-solving approaches positively. It was also
stated that there is a relationship between problem-solving
performance of students with learning disabilities, and the
difficulty level of the problem (Bryan, Bryant, & Hammill,
2000; Powell, 2011).

When faced with difficult problems, students with learning
disabilities are not able to organize the information in
their minds because they are limited in understanding the
language used in the problem. Also, the multi-staged prob-
lems cause more confusion to these students in the prob-
lem-solving process (Powell et al., 2008). Research findings
regarding target strategy teaching revealed that the problems used in relat-
ed studies are the same problems included in the 'Solve It!' strategy. The problems used in the 'Solve It!' strategy range
from easy to difficult (one, two, three-stepped) in terms of
difficulties and the number of operations needed. In ac-
cordance with this information, students' problem-solving
strategies can be developed by arranging the problems to be
used in this intervention group of students with learning
difficulties wisely (Hunt and Vasquez, 2014). In light of
this information, it can be stated that the difficulties of the prob-
lems within the 'Solve It!' strategy, and the number of trans-
actions listed from easy to difficult (one, two, three steps)
are an important variable for the effective implementation
of this strategy (Karabulut & Özmen, 2018).

The participating groups of the study included students with learning disabilities, intellectual disabilities, autism
spectrum disorders, spina bifida, and typical development
al patterns. The effectiveness of 'Solve It!' strategy applied
in these studies has been evaluated (Chung & Tam, 2005;
Coughlin & Montague, 2011; Daniel, 2003; Karabulut, 2015;
Karabulut & Özmen, 2018; Krawec et al., 1984; Montague,
1992; Montague et al., 2011; Montague et al., 2013; Mont-
ague et al., 2014; Montague & Bos, 1986; Whitby, 2012).
It was found that students with and without special needs
made improvement. The intervention group showed rela-
...
tively positive developments over the control group in several reviewed articles. This means that many of the students benefited from the intervention. It also revealed that their peers with usual developmental patterns benefited from the strategies as well, even though it was prepared for the students with special needs. Based on the findings of this research, this research makes suggestions for practice and further research. First, the studies revealed that students with special needs succeeded in solving problems by applying appropriate interventions. In this context, experts working with students with special needs should get involved in professional development programs about the problem-solving stages as well as cognitive and metacognitive strategies with which students can successfully implement the problem-solution strategies. Second, it appears that 12 studies used the ‘Solve It!’ strategy to develop the problem-solving skills of students with special needs. Hence, students with special needs should be the subjects of the studies examining the ‘Solve It!’ strategy to support their problem-solving skills. In this context, future studies can test the effect of each of cognitive and metacognitive strategy element within the ‘Solve It!’ strategy and examine the effects of this strategy on problem-solving performance of the students with special needs. Thus, some programs can be prepared to solve the problems. Third, the ‘Solve It!’ strategy can be recommended not only for students with special needs, but also for their peers with similar development disorders because it has the potential to increase their problem-solving performance.

References


*Krawec, J., Huang, J. Montague M., Kressler B.& Alba A. M.*


* See Table 4.
### Table 4. Research Properties

<table>
<thead>
<tr>
<th>Research and aim</th>
<th>Participants</th>
<th>Grade and age level</th>
<th>Diagnosis</th>
<th>Target skills</th>
<th>Research designs</th>
<th>Intervention environment</th>
<th>Generalization and follow up</th>
<th>Reliability</th>
<th>Results</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chung and Tam (2005)</td>
<td>22 Male 8 Female</td>
<td>GL: 9-10 AL: 15-17</td>
<td>ID</td>
<td>Mathematical problems including two steps addition and subtraction</td>
<td>Cross subjects experimental design</td>
<td>Empty room in school</td>
<td>G: - F: + RO: + AR: -</td>
<td>Students who were trained in cognitive strategy teaching solved more problems than other groups correctly.</td>
<td></td>
</tr>
<tr>
<td>Coughlin and Montague (2011)</td>
<td>3 Male 1 Female</td>
<td>GL: 6, 7, 8 AL: 11-13</td>
<td>SB</td>
<td>One and two-step mathematical problems in the Solve It! program</td>
<td>Multiple baseline across individuals design</td>
<td>Support room</td>
<td>G: - F: + RO: + AR: +</td>
<td>The mathematical problem-solving skills of all participants in the study increased significantly.</td>
<td></td>
</tr>
<tr>
<td>Karabulut and Ozmen (2018)</td>
<td>1 male 2 female</td>
<td>GL: 5 AL: 11-12</td>
<td>ID</td>
<td>Substitution problems involving one-step addition and subtraction</td>
<td>A multiple probe design across subjects</td>
<td>Empty classroom in the school</td>
<td>G: F: RO: + AR: +</td>
<td>Solve It! strategy was identified as effective in the solution of change problems involving a gradual addition and subtraction process.</td>
<td></td>
</tr>
<tr>
<td>Montague (1992)</td>
<td>3 Male 3 Female</td>
<td>GL: 6, 7, 8 AL: 12-14</td>
<td>LD</td>
<td>One, two and three-step mathematical problems with exact and decimal numbers</td>
<td>A multiple probe design across subjects</td>
<td>Support room</td>
<td>G: F: RO: + AR: +</td>
<td>It is stated that the model in which cognitive and metacognitive strategies were taught together in solving mathematical problems was more effective than the models in which the strategies were handled separately and teaching cognitive and metacognitive strategies improved the performance of the students in solving mathematical problems.</td>
<td></td>
</tr>
<tr>
<td>Research and aim</td>
<td>Participants</td>
<td>Grade and age level</td>
<td>Diagnosis</td>
<td>Target skills</td>
<td>Research designs</td>
<td>Intervention environment</td>
<td>Generalization and follow up</td>
<td>Reliability</td>
<td>Results</td>
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</tr>
<tr>
<td>Montague, Enders and Dietz (2011)</td>
<td>359 Male 420 Female</td>
<td>GL: 8 AL: -</td>
<td>LD, TD</td>
<td>Mathematical problems with exact and decimal numbers</td>
<td>Cluster randomized design</td>
<td>Education classroom</td>
<td>G:+ F:+</td>
<td>RO: +AR: +</td>
<td>Students who participated in the intervention in all talent groups received higher points.</td>
</tr>
<tr>
<td>Whitby (2012)</td>
<td>2 male 1 female</td>
<td>GL: 7,8 AL: 13-14</td>
<td>ASD</td>
<td>One and two-step mathematical problems in the Solve It program</td>
<td>A multiple baseline across participants</td>
<td>Support room and education classroom</td>
<td>G:+ F:+</td>
<td>RO: +AR: +</td>
<td>It is stated that all of the three students who participated in the study improved their performance in solving mathematical problems.</td>
</tr>
</tbody>
</table>