Reflection on the Analytic Geometry Courses: The GeoGebra Software and its Effect on Creative Thinking

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Abstract Creativity has a significant role in individuals’ lives. This research aims to examine the reflection of the learning process of analytic geometry concepts through GeoGebra software and its effect upon the development of preservice mathematics teachers’ creative thinking skills. This effect is expected to make a significant contribution to the literature with the examination of creativity and its dimensions as well as the determination of GeoGebra’s role. At this point, this study designed as a mixed method research. Vectors in R² and R³ have been taught to the preservice mathematics teachers using the GeoGebra; moreover, at the beginning and at end of the implementation, the Torrance Creative Thinking Test (TCTT) has been conducted. The research group included a total of thirty preservice teachers. Research data has been collected through Torrance Creative Thinking Test Verbal A and Figural A forms, semi-structured interviews, worksheets and models created by the preservice teachers using the GeoGebra software. The qualitative and quantitative methods have been used for data analysis. Analyses have revealed that the use of the GeoGebra software has positive reflections on preservice teachers, and thus, a significant difference has been noted in favor of the post-test in all dimensions of creativity but one.

Keywords Analytic Geometry, Creativity, GeoGebra Dynamic Mathematics Software, Preservice Mathematics Teachers

1. Introduction

Mathematics is considered as one of the tools through which an individual’s creativity is ascertained. Baki [1] suggests that an increase in imagination in terms of mathematics means the improvement of the path of intuition, creativity and exploring. In Turkey, the aim is to develop creative thinking skills at all levels of education starting from elementary school to higher education [2]. There are various definitions regarding the concept of creativity in the literature. Being one of the touchstones with his studies concerning creativity, Torrance [3] defines creativity as the process of "sensing difficulties, problems, gaps in information, making guesses and hypotheses, testing these hypotheses; revising and restating them; and finally communicating the results". Some researchers suggest that creativity in mathematics is generally related to the problem solving [4].

Education is supposed to support the development of creative thinking in terms of teacher-student relationship [3] and educational environment, methods and techniques, teaching materials as well as assessment. Nevertheless, how education faculties in Turkey organize learning environment or which decisions they make with reference to the development of creative thinking skills of preservice teachers is a significant research subject as it is indispensable for learning settings to be reorganized by taking into account these factors such as being student-centered, developing problem-solving skills, making an emphasis on divergent thinking skills, psychologically safe and planning an environment for infinite learners with the aim of accelerating the development of creative thinking in schools [5]. Therefore, the potential of computer-aided software may be used in the learning settings for the development of creativity [6]. Thus, adopting an integrated learning environment with technology in mathematics classrooms seems to be an alternative way for developing creativity [7].

There are many studies on the relationship between creativity levels of preservice teachers’ and socio-demographic variables in the field [8, 9, 10, 11, 12, 13, 14]. In Özdemir and Çağmak [12], the effect of drama education on creativity of prospective classroom teachers was examined and the data in this study was gathered through “Torrance Test of Creative Thinking-Figural Form A and at the end of the course, the scores of creativity test, the students took increased to some extent in all of the dimensions of creativity test, which are “fluency”,

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an effective and proper use of the dynamic geometry software (DGS) enables students to gain several skills such as exploration and creativity [17]. One of the DGS is the GeoGebra dynamic software that embodies the features of the computer algebra systems (CAS) [18] and the ease of use and the aspects to be translated into several languages [19]. In addition, most of the analytic geometry concepts like points, lines, circles, conic sections, and vectors on the plane can be visualized via the GeoGebra software [20]. Furthermore, visualization of three-dimensional objects has been much easier thanks to the 3D window of the GeoGebra [21]. Nevertheless, another significant research topic can be considered as how these facilities of GeoGebra software reflect on the development of elementary mathematics teachers’ creativity.

The researchers of this study have observed that preservice mathematics teachers who enrolled in primary school teaching department, as lecturing analytic geometry course for a long time, depended on the formerly learned patterns without questioning. Furthermore, they are determined to encounter difficulties during the learning process. Similarly, numerous studies have concluded that students have difficulties in learning the concepts of analytic geometry [22, 23, 24, 25]. Moreover, preservice teachers fail in constructing; that is in imagining some expressions [26]. Many researchers have stated that dynamic software is beneficial for eliminating these adverse conditions [27, 28]. Therefore, the authors investigate the effect of the GeoGebra software in both developing elementary school preservice mathematics teachers’ creativity and understandings of the analytic geometry concepts.

The literature revealed various studies conducted on analytic geometry and its dimensions such as success [29, 30] or comparison of using the computer-aided software in the teaching of analytic geometry concepts with the other methods [31, 32, 33]. However, the present study tries to reveal the role of the GeoGebra dynamic software in the process by scrutinizing elementary school mathematics preservice teachers’ learning processes. When studies were examined on this issue, it is found that creativity has been measured by the Torrance Creative Thinking Test (TCTT). TCTT also has significance in the literature for the direct measurement of creativity [34]. Upon analyzing other tests that are based on creativity, it is revealed that “the a-c creative ability test” focuses only on measuring creativity, “Khatena-Torrance creative perception inventory” is used only for measuring someone’s own creativity perception, while others intended to measure creativity indirectly (quoted by [35]). On the other hand, there are numerous experimental studies in which TCTT is used to measure creativity [5, 36, 37, 38, 39]. Furthermore, the dimensions of the Torrance Creative Thinking Test are composed of fluency, flexibility and originality [36, 39, 40]. This research has examined the reflection of the learning process of the concepts regarding analytic geometry by means of the GeoGebra dynamic software and its effect on the development of preservice mathematics teachers’ creative thinking skills. In accordance with the main objective, the following questions are presented:

1. How do the elementary school mathematics preservice teachers’ learning processes of analytic geometry concepts come true in the GeoGebra dynamic software-aided learning environment?
2. How do these processes affect the development of the elementary school mathematics preservice teachers’ creative thinking skills in all dimensions?

2. Methods

This following section covers the research model, design of the research, research group, data collection, and data analysis.

2.1. Research Model

This study used a mixed method that refers to the use of qualitative and quantitative research methods or paradigms together [41]. Creswell [41] puts great emphasis on the advantage of the mixed method in such a way that researchers carry out their studies in a sufficient way by taking into consideration both qualitative and quantitative aspects.

Quantitative dimension of the study is consisted of a pre-test and a post-test group for one week experimental research design. In order to find an answer to the qualitative dimension, the GeoGebra software-aided learning environments in analytic geometry classes have been instructed to the preservice teachers within elementary school mathematics education program and the reflections of this environment have been analyzed in detail.

2.2. Design of the Research

The design of the research takes place in two stages. These stages are as follows:

2.2.1. Preparation Stage

Upon examining the related literature, students have been
found to succeed in analytic geometry concepts when a
well-organized learning environment is created. Therefore,
worksheets that will affect the learning setting were initially
prepared through analyzing various publications about
creativity and analytical geometry. Worksheets include
guidelines that require the use of the GeoGebra software by
elementary school mathematics preservice teachers during the
process of the discovery of the concepts related to the
subjects. Following the assessments carried out by two
domain experts, the required corrections have been made.
Afterwards, the implementation process has been initiated
considering the questions that will be posed by teachers.

2.2.2. Implementation Stage

At the initial phase of the implementation process, the
TCTT has been applied to the preservice teachers. Then,
two-person groups have been formed for the dynamic
software-aided learning settings. While forming groups,
harmony and level of success between the members of the
group have been taken into account, and fifteen groups have
been created. Also, another researcher has tested the
learning setting and qualitative data collection tools by
sustaining the curriculum on the same course at a different
university for a week further. A pilot study has been
performed after controlling the compatibility of the data
collection tools. The tools have been applied to the
preservice teachers.

The implementation has lasted a total of 9 weeks, and 9
worksheets have been used in this process. These courses
included vectors on the plane and on space. Pre-service
teachers have not been expected to use the GeoGebra
proficiently with regard to the instructions available in
worksheets about the use of software. The aim is to use the
software as a tool so as to acquire the required information.
For instance, preservice teachers are requested to create a
vector on screen in order to explore the relationship
between the start/end point and the coordinates of the vector
for a better understanding of the definition of vector.
Moreover, preservice teachers were also asked to take
different several vectors on the screen with a view in order
to realize that the vector is a change of location which
represents sum of these vectors taken on the screen in line
with the relationship between these vectors and their sum.
In another worksheet, preservice teachers were asked to
take two vectors and produce the cross product of these
vectors so that they can determine the relationship between
these two vectors and the cross product vector. Besides, it
has been revealed that the area of a parallelogram that is
composed of two vectors and the volume of the
parallelepiped consisted of three vectors in space with the
GeoGebra subsequently to understand the relationship
between the two vectors and their cross product vector. A
month after the implementation, the TCTT has been
reapplied to the preservice teachers to seek answers for the
research questions.

2.3. Research Group

The research has been carried out with preservice
mathematics teachers who receive education at the
department of elementary school mathematics. The sample
consisted of 30 preservice teachers from the same class.
Among the preservice teachers, 16 were female and 14 were
male. They were selected amongst those who take analytic
geometry course that was taught by one of the authors in a
public university. Thus, this research used an experimental
method without controlling any group as the courses in the
elementary mathematics education department in Turkey
are carried out as a single group due to the limited quota
except for a few universities.

Taking courses on basic ICT skills at the first grade, the
preservice mathematics teachers began interacting with the
GeoGebra in two courses (General Mathematics, Geometry).
At the second grade, the GeoGebra is used only for
presentation by the researcher when needed in Calculus I
course. In addition, they were asked to use the GeoGebra
software in their exams or to answer the presented questions.
Thus, all participants were trained in order to use the
GeoGebra and to prepare activities by using it. They already
had the skills needed to construct the situations on the
worksheets. Furthermore, their mathematics competency
level was sufficient, and they had positive attitudes towards
mathematics.

2.4. Data Collection Tools

The data collection tools employed in the study have
been presented in accordance with the qualitative and
quantitative methods as follows.

2.4.1. Quantitative Data Collection Tool

The Torrance Thinking Creative Test (TTCT) was first
introduced in 1966 and has been used in 615 researches and
more than 100 postgraduate theses [42] in order to measure
individuals’ creativeness performance in 35 different
cultures. The study has deployed the Torrance Thinking
Creative Test (TTCT) as a quantitative data collection tool.
The tool is composed of two equivalent forms including
Verbal A and B and Figural A and B in which each form has
subtests. Both forms of the TTCT test are appropriate at all
levels of education from kindergarten to university. The
Turkish adaptation of Figural and Verbal Forms of the TCTT
were created by Aslan [43]. The following test forms were
used in the present study.

The TTCT-Verbal has two parallel forms, A and B,
including the following subtests: (a) Asking Questions and
Making Guesses (subtests 1, 2 and 3) in which participants
write questions and make guesses about possible causes and
consequences of situations based on a drawing of a scene; (b)
Improvement of a Product (subtest 4); the participants list
ways to change a toy elephant so that they will have more fun
playing with it; (c) Unusual Uses (subtest 5); they list
interesting and unusual uses of a cardboard box; (d) Unusual
Questions (subtest 6); preservice teachers list interesting and unusual questions of a cardboard box; (e) Supposing (subtest 7); they are asked to list all the consequences that an improbable situation may come true [44, 45]. Fluency, originality and flexibility characteristics were assessed via the TTCT Verbal A Form.

The TTCT-Figural is consisted of two parallel forms with three subtests: (a) compose a drawing; (b) finish a drawing; and (c) compose a different drawing parting from parallel lines [45]. Also, the TTCT Figural A Form includes 18 sub-dimensions: fluency, originality, elaboration (detailing), abstractness of titles, resistance to premature closure, creative strengths list (emotional expressiveness, storytelling articultateness, movement or action, expressiveness of titles, combining of incomplete shapes, synthesis of incomplete lines, unusual visualization, internal visualization, extending or breaking boundaries, humor, richness of imagery, colorfulness of imagery and fantasy).

A form of the TCTT was conducted to preservice teachers before and after the study. 5-6 minutes were given to participants for each activity in the verbal part of the TCTT, 10 minutes for each activity that includes shapes. The implementation of the TCTT and scoring each participant's test lasted approximately 75-80 minutes.

2.4.2. Quantitative Data Collection Tool
Qualitative data include the interviews conducted with preservice teachers during the lessons, worksheets performed by groups and models prepared on the GeoGebra screen.

2.5. Data Analysis

The responses posed by elementary school mathematics preservice teachers to the TCTT Verbal – Figural A form were scored by the authors individually depending upon the principles by Torrance and Torrance Creative Thinking Test Verbal – Figural A guidelines and assessment booklet. The research data were analyzed through use of the SPSS 21.0 statistical package program. First, the study confirmed whether data provided the general requirements of the parametric tests. Normality was tested by performing skewness and kurtosis on the analysis of the data obtained in the study. Paired samples t-test was used for those between -1 and +1, while the study used non-parametric Wilcoxon test for the other activities.

Data printout and control obtained from interviews and worksheets were carried out. During writing the interview data on paper, each conversation was respectively written by interviewer-interviewee without making any correction. Then, the data analysis was finalized by bringing together all the analyses conducted by researchers independently and discussing on them. This is a significant requirement referenced in ensuring the validity of the research. In addition, codes were given to the preservice teachers as A, researcher and T1, preservice teacher 1 ...etc.

3. Results
In this section, the quantitative and qualitative data obtained from the participants were discussed separately in order to clarify two research questions.

3.1. Reflection on Course Process
This section presents several reflections of the elementary school mathematics preservice teachers that obtained through analyzing their learning processes with reference to vectors in R^2 and R^3. This presentation is supported by excerpts from interviews, statements that preservice teachers wrote on worksheets and screenshots in the GeoGebra software. Besides, codes were given to the preservice teachers in each group as T1, T2, T3, .... T30.

Taking the research findings into account, elementary school mathematics preservice teachers conducted the process of exploring better via the GeoGebra. To illustrate, T11 and T12 preservice teachers, who considered a vector as the displacement of a point, have determined the coordinates of the vector emerging with the change of the places of the points they have taken on the GeoGebra screen. Then, this group has been noted to generalize this expression as mathematical. The data for this case are as follows:

Some of the teachers, who learned the sum of the two vectors, had the opportunity to learn more about vectors together with the reasons. Illustratively, the data about T1 and T2 preservice teachers are as follows:

T1: We know the vector is a displacement. Therefore, let's add two vectors end to end. Look! How the place has changed.
T2: Yes. Total w vector has been achieved. Now, let's take five vectors and observe them by adding these vectors end to end as stated in the worksheets.
T1: We're good at memorizing the sum of two vectors. It could be five and more vectors in total. It does not change when we add more. I think we can observe much better.
Elementary school mathematics preservice teachers have been reported to make a better observation about the fact that the product of two vectors is orthogonal to both of these vectors on the three-dimensional screen of the GeoGebra. During this process, preservice teachers have observed that inner products of two vectors of vector product were always zero thanks to the dynamic feature of the software via both algebra and three-dimensional screen by changing the points. The data on this result for T17 and T18 preservice teachers are as follows:

T17: By taking three pencils after observing this, we can show the third pencil orthogonal to the two pens. But, I think that observing them here will be better.

R: Well, what can we say for inner product?

T17: Inner products are always zero, which can be observed from algebra screen. This inner product does not change when we move the points.

T18: Inner products are always zero if two vectors are orthogonal.

Later, the preservice teachers were asked to take the two vectors as parallel and intercept with each other, and to observe and interpret how the vector products of these vectors change. In this regard, most of the elementary school mathematics preservice teachers have been determined to make various assumptions at first, and then they have identified the vectors on the screen as parallel or intercepting. T23 and T24 preservice teachers’ responses are as follows:

R: How does vector product change when you get u and v vectors as parallel or intercept with each other?

T23: I think it does not change as the vector product will appear again on the three-dimension screen. Still, it will be better to observe it on the screen.

T24: Yes, I’m getting the coordinates of the vector u (2, -2.1) and the vector v (4, 4, 2). Yes, w vector becomes a zero vector. It disappears from the three-dimension screen. It was observed as the point on the two-dimensions and three dimensions.

T23: Actually, when we consider the definition of the vector product, it is a row like a determinant.
It has also been revealed that the majority of the preservice teachers had difficulty in finding vector products of two vectors in the above processes. They have noted the nonexistence of toolbar which provides this directly in the GeoGebra software. The conversation between T21 and T22 preservice teachers is presented as follows:

T21: If there was a command or icon which finds vector product direct, we wouldn’t have been obliged to write the coordinates of the vector product on the input screen.

T22: I agree. We've written the definition of the vector of the vectorial product.

3.2. The Data Regarding the Torrance Creative Thinking Test

Table 1 depicts paired sample t-test results related to the mean of the Verbal and Figural forms pre- and post-test of the elementary school mathematics preservice teachers.

Table 1. Paired Sample t-test Results Related to Preservice Teachers’ Creative Thinking Skills

<table>
<thead>
<tr>
<th>Measurement</th>
<th>N</th>
<th>X</th>
<th>SS</th>
<th>t</th>
<th>p</th>
</tr>
</thead>
<tbody>
<tr>
<td>Verbal pre</td>
<td>31</td>
<td>56.81</td>
<td>17.50</td>
<td>-7.065</td>
<td>.000</td>
</tr>
<tr>
<td>Verbal post</td>
<td>31</td>
<td>95.65</td>
<td>29.28</td>
<td>-8.509</td>
<td>.000</td>
</tr>
<tr>
<td>Figural pre</td>
<td>31</td>
<td>80.35</td>
<td>27.79</td>
<td>-8.509</td>
<td>.000</td>
</tr>
<tr>
<td>Figural post</td>
<td>31</td>
<td>139.32</td>
<td>36.17</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Upon analyzing Table 1, this difference has been found to be statistically significant in the Verbal and Figural Form A depending on the paired samples t-test results (p<.05). The research findings show that teaching analytic geometry concepts via the GeoGebra dynamic software process has a positive and significant impact on creative thinking.

Considering the preconditions of the preservice teachers’ verbal fluency, verbal originality and verbal flexibility being the activities of verbal creativeness and activities of figural creativeness such as fluency, originality, elaboration (detailing), abstractness of titles, resistance to premature closure, creative strengths list (emotional expressiveness, storytelling articulateness, movement or action, expressiveness of titles, combining of incomplete shapes, synthesis of lines, unusual visualization, internal visualization, extending or breaking boundaries, humor, richness of imagery, colorfulness of imagery and fantasy) scores, the data have been determined to be sporadic. In addition, skewness and kurtosis coefficients were taken into account in order to identify whether the data available in the preconditions distributed normally.

The mean scores obtained from each activity by the preservice teachers were calculated for the activities of verbal forms (fluency, flexibility, originality) and figural forms (originality, abstractness of titles, resistance to premature closure, movement or action, expressiveness of titles, internal visualization), all of which demonstrated normal distribution in the TCTT. The paired sample t-test was performed with the aim of determining whether there is a significant difference between the scores of pre- and post-test for each activity. Table 2 displays the findings related to pre- and post-test results of these activities, which are normally distributed.

As it can be observed in Table 2, the pre-test and post-test mean scores of preservice teachers related to verbal form fluency activity have been determined to be 28.19 and 45.81, respectively. A statistically significant difference between the mean scores of the preservice teachers has been identified in this activity (p= .00<.05). Likewise, a statistically significant difference between the mean scores of the preservice teachers in favor of the post-test has been noted in terms of the verbal forms of flexibility and originality.

Having examined the results of the figural form for originality, the mean scores of the pre-test have been found to be 11.97, while that of the post-test seems to rise up to 20.23. Research results have also revealed a significant difference in favor of the post-test (p= .00<.05). As for the results of the figural form of abstractness of titles, the mean scores of the pre-test were 7.39 while the mean score of post-test seems to increase in 12.61. It has been pointed that the difference is significant in favor of the post-test (p= .00<.05). Likewise, as to the figural forms of resistance to premature closure, movement or action, expressiveness of titles and internal visualization, a statistically significant difference has been reported in favor of the post-test (p= .00<.05).
Table 2. Paired Sample t-test Results Related to Pre-test - Post-test Mean Scores Obtained from Normally Distributed Activities

<table>
<thead>
<tr>
<th>Form/dimensions</th>
<th>X</th>
<th>N</th>
<th>SS</th>
<th>t</th>
<th>P</th>
</tr>
</thead>
<tbody>
<tr>
<td>V-fluency pre-test</td>
<td>28.19</td>
<td>31</td>
<td>8.45</td>
<td>-6.15</td>
<td>.000</td>
</tr>
<tr>
<td>V-fluency post-test</td>
<td>45.81</td>
<td>31</td>
<td>15.47</td>
<td></td>
<td></td>
</tr>
<tr>
<td>V-flexibility pre-test</td>
<td>15.48</td>
<td>31</td>
<td>4.61</td>
<td>-6.94</td>
<td>.000</td>
</tr>
<tr>
<td>V-flexibility post-test</td>
<td>23.68</td>
<td>31</td>
<td>6.21</td>
<td></td>
<td></td>
</tr>
<tr>
<td>V-originality pre-test</td>
<td>13.13</td>
<td>31</td>
<td>6.34</td>
<td>-6.31</td>
<td>.000</td>
</tr>
<tr>
<td>V-originality post-test</td>
<td>26.16</td>
<td>31</td>
<td>10.11</td>
<td></td>
<td></td>
</tr>
<tr>
<td>F-originality pre-test</td>
<td>11.97</td>
<td>31</td>
<td>6.28</td>
<td>-6.34</td>
<td>.000</td>
</tr>
<tr>
<td>F-originality post-test</td>
<td>20.23</td>
<td>31</td>
<td>6.16</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 3. Wilcoxon Signed Rank Test Results Relating to the Activities of TCTT

<table>
<thead>
<tr>
<th>Form/dimensions</th>
<th>Post test Pre test</th>
<th>N</th>
<th>Mean Rank</th>
<th>Rank Sum</th>
<th>Z</th>
<th>p</th>
</tr>
</thead>
<tbody>
<tr>
<td>F-fluency</td>
<td>Negative rank</td>
<td>3</td>
<td>8.00</td>
<td>24.00</td>
<td>-3.850</td>
<td>.000</td>
</tr>
<tr>
<td></td>
<td>Positive rank</td>
<td>23</td>
<td>14.22</td>
<td>327.00</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Equal</td>
<td>5</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>F- elaboration</td>
<td>Negative rank</td>
<td>1</td>
<td>4.50</td>
<td>4.50</td>
<td>-3.182</td>
<td>.001</td>
</tr>
<tr>
<td></td>
<td>Positive rank</td>
<td>14</td>
<td>8.25</td>
<td>115.50</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Equal</td>
<td>16</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>F- emotional expressiveness</td>
<td>Negative rank</td>
<td>3</td>
<td>4.50</td>
<td>13.50</td>
<td>-4.231</td>
<td>.000</td>
</tr>
<tr>
<td></td>
<td>Positive rank</td>
<td>24</td>
<td>15.19</td>
<td>364.50</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Equal</td>
<td>4</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>F- storytelling articulateness</td>
<td>Negative rank</td>
<td>4</td>
<td>12.75</td>
<td>51.00</td>
<td>-3.737</td>
<td>.000</td>
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<tr>
<td></td>
<td>Positive rank</td>
<td>26</td>
<td>15.92</td>
<td>414.00</td>
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<tr>
<td></td>
<td>Equal</td>
<td>1</td>
<td></td>
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<tr>
<td>F- combining of incomplete shapes</td>
<td>Negative rank</td>
<td>0</td>
<td>.00</td>
<td>.00</td>
<td>-1.000</td>
<td>.317</td>
</tr>
<tr>
<td></td>
<td>Positive rank</td>
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<td>1.00</td>
<td>1.00</td>
<td></td>
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</tr>
<tr>
<td></td>
<td>Equal</td>
<td>30</td>
<td></td>
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<tr>
<td>F- synthesis of lines</td>
<td>Negative rank</td>
<td>0</td>
<td>.00</td>
<td>.00</td>
<td>-2.384</td>
<td>.017</td>
</tr>
<tr>
<td></td>
<td>Positive rank</td>
<td>7</td>
<td>4.00</td>
<td>28.00</td>
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<tr>
<td></td>
<td>Equal</td>
<td>24</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>F- unusual visualization</td>
<td>Negative rank</td>
<td>2</td>
<td>8.00</td>
<td>16.00</td>
<td>-4.346</td>
<td>.000</td>
</tr>
<tr>
<td></td>
<td>Positive rank</td>
<td>26</td>
<td>15.00</td>
<td>390.00</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Equal</td>
<td>3</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>F- extending or breaking boundaries</td>
<td>Negative rank</td>
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<tr>
<td>F- humor</td>
<td>Negative rank</td>
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<td>13.50</td>
<td>-4.420</td>
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<td>F- richness of imagery</td>
<td>Negative rank</td>
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<td>8.50</td>
<td>17.00</td>
<td>-3.848</td>
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<td>F- colorfulness of imagery</td>
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<td>F- fantasy</td>
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The study used non-parametric Wilcoxon test for the figural forms of fluency, elaboration (detailing), emotional expressiveness, storytelling articulateness, combining of incomplete shapes, synthesis of lines, unusual visualization, extending or breaking boundaries, humor, richness of imagery, colorfulness of imagery and fantasy, which are not distributed normally. Table 3 presents Wilcoxon Signed Rank Test results relating to the activities of the TCTT.

As can be seen in Table 3, the figural form of fluency (z=-3.850; p=.00<.05) is significant by the effect of the difference between the pre-test and post-test results of the preservice teachers. Similarly, for the figural forms of elaboration (z=-1.822; p=.001<.05), emotional expressiveness (z=-2.421; p=.00<.05) and storytelling articulateness (z=-3.727; p=.00<.05) a significant difference has been noted in favor of the post-test.

There was not any significant difference between the pre-test and post-test scores of the preservice teachers for the dimension of combining of incomplete shapes (z=-1.000; p=.317>.05). In other words, it is most likely that the results of the pre-test have similar features with the post-test results. With respect to synthesis of lines (z=-2.384; p=.017<.05), a significant difference has been pointed between the pre-test and post-test scores of the preservice teachers. In a similar manner, it was revealed that there was a significant difference between the pre-test and post-test scores of the preservice teachers in favor of the post-test regarding unusual visualization (z=-4.346; p=.00<.05), extending or breaking boundaries (z=-3.364; p=.001<.05), humor (z=-4.420; p=.00<.05), richness of imagery (z=-3.848; p=.00<.05), colorfulness of imagery (z=-4.119; p=.00<.05) and fantasy (z=-3.578; p=.00<.05).

4. Conclusion and Discussion

The research results have revealed that elementary school mathematics preservice teachers magnificently observed that vector of vector product is orthogonal to both of the vectors on the three-dimensional screen of GeoGebra. Furthermore, many scientists state that the 3D screen of GeoGebra software is useful [46, 47, 48, 49]. Parallel to the research results, Arcavi and Hadas [50] and Sheffield and Cruikshank [51] have indicated that dynamic software enables students to learn by experiencing through visualization, and hence students not only make observations but they also have the ability to measure, to make comparison and to change shapes. Most of the preservice teachers have been stated to try to uncover the reasons for the results. In fact, as mentioned by González and Herbst [52] and Santos-Trigo and Cristóbal-Escalante [53], all the processes above have been realized thanks to the sense of creativeness and making deductions via dynamic software. Besides, preservice teachers who follow the instructions available in worksheets prepared via GeoGebra software have been determined to make mathematical generalizations. Similar results emerged in the study conducted by Santos-Trigo and Cristóbal-Escalante [53].

The findings related to TCTT have revealed that preservice teachers’ verbal and figural mean scores increase in favor of post-test. A statistically significant difference has been noted between pre-test and post-test for both verbal form-A and figural form-A. It may be wise to emphasize that teaching through GeoGebra software has a positive and significant impact on creative thinking. Several studies have indicated the positive impact of daily life modeling activities, constructed with GeoGebra upon students’ creativity [20, 54]. Aktümen and Yıldız [55] conducted another study that questioned the projects designed via GeoGebra by preservice teachers may ensure the development of their creativity. In their studies, Liu [56] and Idris and Nor [57] have found that technology uncovers existing, creative thinking skills of students and facilitates their development. That GeoGebra software presents different screens together may cause such a situation like this. For example, the pre-service teachers can easily observe the vector product of the vectors by changing dynamically in the graphic screen.

Torrance Creative Thinking Test Verbal- Figural Form-A has been examined for each activity, and no significant difference has been demonstrated between pre-test and post-test in terms of combining of incomplete shapes activity; whereas, in all other activities, a significant difference has been detected in favor of post-test. This is likely due to the fact that GeoGebra software does not have an effect on the activity called combining of incomplete shapes that is considered as an indicator of the ability to see relationships between unrelated elements. Otherwise, Edwards and Jones [22] have reported that GeoGebra software helps to create higher-order thinking skills. This case may derive from the use of worksheets for supporting each other in order to teach a subject in the course of analytical geometry. It is highly probable to point the relationship between them thanks to the GeoGebra software, if this case can be repeated with other independent subjects of analytical geometry.

As for fluency activity, a significant difference has been identified in favor of the post-test. Teaching through GeoGebra is likely to have a positive effect on fluency which is based upon producing a large number of ideas within a certain time constraint. A similar finding has been found by Eshrat, Asgury, Sarami and Zarekar [40] in that computer-aided education is effective on fluency activity of creativity. As to originality activity, a significant difference has been identified in favor of the post-test. In their studies, Aqda, Hamidi and Rahimi [36], Liu [56] and Eshrat, et. al. [40] have found that computer-aided education is effective on originality activity of creativity. A significant difference has also been determined in favor of post-test in terms of elaboration activity. The study carried out by Aqda, et. al. [36] has revealed the effectiveness of computer-aided
Continuous efforts are expected to be made in order to improve the lack of these skills, so it is essential that GeoGebra software be included in the education process as an important tool.

Finally, there are several reasons why GeoGebra software-aided learning settings presented to elementary school mathematics preservice teachers during analytic geometry courses cause a significant difference in favor of post-test in all activities except for one. These are as follows: the ease of use, to reflect the change simultaneously carried out on a window to the other windows and visually presenting a rich content. Aslan [58] defines creativity as “the new and original, emerging as a product based on skill or does not turn into a product yet, including specific problem-solving processes, a cognitive process by which a person uses intelligence elements originally”. This provides preservice teachers with having a positive improvement in terms of dynamic mathematics software, which is an appropriate decision. Hohenwarter, Hohenwarter, Kreisler and Lavicza [59] have stated that teachers can observe students’ creativity by allowing them to work with GeoGebra and then teachers can shape their teaching methods. In this context, putting forth potentials and deficiencies of the GeoGebra software in a similar manner at certain special cases would make a significant contribution to the literature.

REFERENCES


Reflection on the Analytic Geometry Courses: The GeoGebra Software and its Effect on Creative Thinking


