This study reviewed the statistical practices in published research articles in the "Journal of Education for Students Placed at Risk" to determine the reporting of effect sizes and structure coefficients. Of the 12 quantitative studies found in the last 3 volumes of the journal, only 3 were identified as using multiple regression analysis. Two of the three indicated use of effect size magnitudes, but the third reported only "F" and "p-" values. None of these articles gave structure coefficients. Reporting effect sizes highlights the difference between statistical and practical significance. The paper also recommends the use of "what-if" analysis when using regression. (SLD)
Multiple Regression Methodology in the *Journal of Education for Students Placed at Risk*: Effect Sizes and Structure Coefficients

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In any research study, the integrity of the research is only as strong as the weakest link. Study validity can be threatened from myriad fronts, including attacks to what is commonly called statistical conclusion validity. Statistical conclusion validity refers to the appropriate use and interpretation of the statistical methodology used in a given study (Babbie, 1992). When methods are not appropriately employed, the conclusions that can be drawn from a line of inquiry are weakened. Accordingly, the purpose of the present paper is to review the statistical practices in published research articles in the Journal of Education for Students Placed at Risk concerning two important issues in regression research.

First, as in all general linear model analyses (cf. Cohen, 1968; Knapp, 1978) and consistent with current trends in best statistical practice (Thompson, 1999; Wilkinson & American Psychological Association (APA) Task Force on Statistical Inference, 1999), the interpretation of effect sizes in regression research is critical to understanding one’s study results. Effect sizes help researchers understand the magnitude of relationships among their variables, and therefore shed light on result importance (Thompson, 1999). Effect size reporting is becoming increasingly important as researchers become aware of the limits of statistical significance testing. As the APA Task Force recommended:

It is hard to imagine a situation in which a dichotomous accept-reject decision is better than reporting an actual $p$-value or, better still, a confidence
interval... Always provide some effect-size estimate when reporting a p-value (p. 599, emphasis added).

Second, and also in all general linear model analyses, structure coefficients are critical to interpreting variable importance. Indeed, the common practice of examining only standardized weights (i.e., beta weights) in regression research can lead to erroneous conclusions (Thompson & Borrello, 1985; Courville & Thompson, 2001). Because they represent the simple bivariate correlation between a predictor variable and the latent predicted variable (i.e. Yhat), structure coefficients tell us the contribution each predictor could have made in accounting for overall effect. Structure coefficients are not adversely affected by multicollinearity (as beta weights are), and therefore overcome the so-called "bouncing beta" problem in which the beta weights can dramatically change as predictor intercorrelations fluctuate across studies. Accordingly, both beta weights and structure coefficients should almost always be interpreted in regression research.

Several studies have examined the reporting of effects and structure coefficients in research (cf. Courville & Thompson, 2001; Henson & Smith, 2000; Vacha-Haase, Nilsson, Reetz, Lance, & Thompson, 2000). In large part, and unfortunately, both effect sizes and structure coefficients are not frequently reported and interpreted in the research literature. Kirk (1996) suggested increase frequency of reporting for multiple regression articles due to the fact that statistical software often readily provide $R^2$ effects in regression output.

**Purpose**

To further examine the current status of best reporting practice, the present paper will examine the use and interpretation of structure coefficients and effect sizes in
multiple regression articles in the *Journal of Education for Students Placed at Risk*. Therefore, the present paper will extend the methodological examination to the multicultural and at-risk education literature.

Articles using multiple regression were first identified in the last three volumes of the journal. These articles were then examined and coded concerning whether the article (a) reported structure coefficients, (b) interpreted structure coefficients, (c) reported effect sizes, and (d) interpreted effect sizes. Along with this data, the paper also documents the types of effect sizes used. Examples of best and poor practice are noted and recommendations for improved reporting practice are offered.

**Method**

**Article Selection**

A total of twelve quantitative type studies were found in the last three volumes of *The Journal of Education for Students Placed At Risk*. Only three of those twelve articles were identified as using multiple regression analysis, of which this paper addresses.

**Effect Size Reporting**

Two of the three articles examined using multiple regression in *The Journal of Education for Students Placed At Risk* indicated use of effect size magnitudes. The third article only reported $F$ and $p$-values.

**Effect Size Interpretation**

Kirk (1996) identified 16 varieties of magnitude effect reporting in social science journals reviewed in one study, however only $r$, adjusted $r^2$ and $\eta^2$ were interpreted in the articles reviewed that used multiple regression in *The Journal of Education for Students Placed At Risk*. Of the two studies using effect sizes, adjusted $r^2$ was only
referenced once; eta\(^2\) was also reported in one article. The article reporting adjusted r\(^2\),
provided an interpretation of the data results in both the Results and Discussion sections;
the other article reporting eta\(^2\) provided an interpretation in the Results section only.

Structure Coefficient Reporting and Interpretation

In examining studies that used multiple regression analysis in *The Journal of
Education for Students Placed At Risk*, all of those studies were quantitative in nature,
reporting statistics such as the mean, standard deviation, \(F\), and \(p\)-values. However, none
reported or interpreted structure coefficients or beta weights.

**Reporting and Interpreting Structure Coefficients**

Reporting structure coefficients as an important measure in research studies has
yet to be found as a common method in examining and analyzing data, in the general
linear model (Courville & Thompson, 2001). However, as noted by Thompson (1992),
the reporting of beta weights and structure coefficients are both important. Thompson
(1992) further argued that “the thoughtful researcher should always interpret either (a)
both the beta weights and the structure coefficients or (b) both the beta weights and the
bivariate correlations of the predictors with Y“ (p. 14).

Unfortunately, in regression research, heavy emphasis has been placed on solely
interpreting beta weights to the exclusion of structure coefficients. For example, one
study (Courville & Thompson, 2001) noted that only three of twenty articles reviewed in
*The Journal of Counseling Psychology* between January 1990 and April 1993 reported
structure coefficients.

Since structure coefficients can help explain the predictive importance of a
predictor variable’s contribution to the overall effect, reporting these measures may help
in explaining the theoretical and practical ramifications of the results. Courville and Thompson (2001) suggested that if a general linear model analysis is used in a study where predictors are correlated, as they often are, then “when interpreting regression results, once noteworthy effects have been detected it may be best to consult the full system of results, just as we routinely would in applications of other members of the general linear model analytic family” (p. 45).

A structure coefficient is a correlation between an observed variable (e.g. predictor) and a synthetic variable (e.g. Yhat); an example structure coefficient formula for predictor X1 would be: \( r_{\text{structure}} = r_{Y \text{ with } X1/R} \) (cf. Courville & Thompson, 2001; Daniel & Onwuegbuzie, 2001). Structure coefficients are not readily obtainable for multiple regression using a statistical software package (i.e. SPSS), although it is as much a correlation analysis as Pearson’s r, and can be calculated using the statistical package (cf. Daniel & Onwuegbuzie, 2001). All researchers need to do is to save the unstandardized predicted values (i.e. Yhat) as part of the regression analysis and then correlate these Yhat scores with the observed predictors. When one squares the structure coefficient \( r_s^2 \), the result is the percentage of variance the predictor could contribute to the explained effect.

**Reporting Effect Sizes**

Reporting effect sizes alongside \( p \)-values, given the limitations of statistical significance testing, is long overdue for educational journals (Kirk, 1996). As noted by Kirk (1996), “researchers have been encouraged to supplement reports of null hypothesis tests with measures of effect magnitude” for over 70 years now.
Effect sizes can generally be grouped into two categories. Category one includes mean difference effects such as Cohen’s d, which represents the difference between experimental and control groups divided by the pooled standard deviation of both groups. Category two includes variance-accounted-for effects such as $r^2$, $\eta^2$ and adjusted $r^2$ (Snyder & Lawson, 1993).

Reporting an effect size is necessary in that statistical significance testing alone only answers the question “If the sample represents the population, how likely is the obtained [sample] result?” (Thompson, 1998, p. 34, emphasis in original). Too, statistical conclusion on the hypothesis is a function of obtained $p$-values, which, as Henson and Smith suggested (2000, p.286, emphasis in original) only “indicate the probability (0 to 1.0) of attaining the presently observed results from the present sample assuming that the null hypothesis is exactly true in the population.” This makes it necessary to supplement such judgments with alternative reporting methods, such as effect size measures to indicate the magnitude of the finding, not just the likelihood of the finding.

According to Kirk (1996), reporting a statistic that indicates a specific magnitude of effect, rather than reporting a general reference to the use of effect sizes, is more favorable. He further noted that $r^2$ and $\eta^2$ are readily recorded as such, when using statistical software packages, such as SPSS (Kirk, 1996).

Practices and Recommendations

Of the articles reviewed in The Journal of Education for Students Placed At Risk using multiple regression, three of them reported p-values or F statistics. Of these however, only two offered effect sizes magnitude; none gave structure coefficients.
It is poor practice to report statistical significance testing values without also reporting and interpreting effect size values (Thompson, 1998). Thompson also posited "most authors will simply not change their practices until editorial policies require them to do so (Thompson, 1998, p. 35). In this same article, he also confronted the wording of the American Psychological Association’s 4th edition publication manual in reference to reporting practices for effect sizes of “encouraging” authors to report effect sizes; he cited this wording as “too vague to enforce “ (Thompson, 1998, p. 35). It is interesting to note here that the APA’s 5th edition (2001) now reads:

For the reader to fully understand the importance of your findings, it is almost always necessary to include some index of effect size or strength of relationship in your Results section. You can estimate the magnitude of effect or the strength of the relationship with a number of common effect size estimates, including (but not limited to) $r^2$, $\eta^2$, $\omega^2$, $R^2$, $\varphi^2$, Cramer’s $V$, Kendall’s $W$, Cohen’s $d$ and $\kappa$, Goodman-Kruskal’s $\lambda$ and $\gamma$, Jacobson and Truax’s (1991) and Kendall’s (1999) proposed measure of clinical significance, and the multivariate Roy’s $\Theta$ and the Pillai-Barlett $V$ (pp. 25-26, emphasis added).

The Journal of Education for Students Placed At Risk shows evidence in the quantitative articles reviewed that effect size reporting and interpretation is practiced. It must be noted her that The Journal of Education for Students Placed At Risk does include both quantitative and qualitative articles. Of these articles (forty-five), however, only twelve of them were quantitative studies. In examining the twelve quantitative studies, only three used multiple regression, but of these three, two of them reported effect sizes.
The practice of reporting structure coefficients in *The Journal of Education for Students Placed At Risk*, is not popular to say the least (none were noted). Courville and Thompson (2001) cited “in most cases, regression researchers ought to interpret β weights and structure coefficients (or else bivariate correlations of predictors with the criterion) once a noteworthy omnibus effect is detected” (p. 244). Also, Courville and Thompson (2001) noted the importance of interpreting structure coefficients in that the reason for calling “structure coefficients” such is “that they provide insight regarding what is the nature or structure of the underlying synthetic variables of the actual research focus. (p 238, emphasis added).

**Recommendations**

It is recommended that authors report *p*-values and test statistics from the general linear model when necessary, but also include the reporting and interpreting of effect sizes to explain magnitude of effect. When notable effects are observed, then and only then, report and interpret both standardized weights and structure coefficients to explain how much each predictor is contributing to the model (Daniel & Onwuegbuzie, 2001). Reporting effect sizes also “highlight the distinction between *statistical* and *practical* significance. Results that are statistically significant are not always noteworthy in a practical sense” (Snyder & Lawson, 1993, pp. 334-335, emphasis in original) but effect sizes “tells us how much of the dependent variable can be controlled, predicted, or explained by the independent variable(s)” (Snyder & Lawson, 1993, p. 335).

It is also recommended that researchers conduct a newer, precise “what-if analysis” when using regression, as noted by Henson and Smith (2000) and proposed by Kieffer and Thompson (1999); this newer “what-if analysis,” provides for corrected
effect estimates (Henson & Smith, 2000). A “what if” analysis resembles a post hoc power analysis and helps researchers place statistical significance tests in the context of sample size (Henson & Smith, 2000).

Because most researchers learn their methodology skills in educational statistics courses in university settings, it is recommended that courses and textbooks reflect such practices. Thompson (1998, emphasis in original) noted “empirical studies consistently show that many researchers do not fully understand the logic of statistical tests” (p. 34). He further stated, “Similarly, many textbooks teach misconceptions regarding these tests (Thompson, 1998, p. 34).

Critical to statistical conclusion validity when reporting p-values is to always report and interpret effect sizes. To analyze how much a variable(s) is contributing to that effect, researchers should almost always report structure coefficients. Conducting a “what-if” analysis when interpreting data results and reporting statistical significance findings in terms of “sample size,” also helps facilitate understanding of results. As suggested by Thompson (1997):

All analyses are part of one general linear model. When interpreting results in the context of this model, researchers should generally approach the analysis hierarchically, by asking two questions:

- Do I have anything? (Researchers decide this question by looking at some combination of statistical significance tests, effect sizes…and replicability evidence.)
If I have something, where do my effects originate? (Researchers often consult both the standardized weights implicit in all analyses and structure coefficients to decide this question.) (p.31)
References

All articles used in the review are marked with an asterisk (*).


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