An empirical approach is adopted in this paper to explore a possible model for prediction of students' science achievement in China and the United States. Construction of the model is based on the ninth-grade data base from Phase 2 of the Second International Education Association Science Study (SISS) in the United States and the SISS Extension Study (SES) in Hubei province in China. The common independent variables of science achievement are classified into gender, attitude, home background, classroom experience, and personal effort, according to the distinction between visible and latent characteristics and scree plots from principal-components analysis. Latent factors are represented by the first principal components in each of the four latent categories of student attitudes, home backgrounds, classroom experience, and personal effort. Predictors of the model are constructed by polynomials of the visible and latent factors and their interactions in a multivariate Taylor series. Significant predictors at the alpha=0.05 level are selected through a backward elimination procedure in the Statistical Analysis System. The structure of the four latent factors and the model complexity have been compared between the two countries in terms of their educational, political, social, and cultural contexts. Eight tables and two figures are included. (Contains 45 references.) (Author/SLD)
An Empirical Approach toward the Prediction of Students' Science Achievement in the United States and the Peoples' Republic of China

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Running Head: Empirical Model

Abstract

An empirical approach is adopted in this paper to explore a possible model for prediction of students' science achievement in China and the United States. Construction of the model is based on the ninth grade data base from the Phase II of the Second IEA Science Study (SISS) in the United States and the SISS Extension Study (SES) in Hubei province of China. The common independent variables of the students' science achievement are classified into five categories, students' gender, attitude, home background, classroom experience, and personal effort, according to the distinction between visible and latent characteristics, and scree plots from principal component analyses. Latent factors are represented by the first principal components in each of the four latent categories, students' attitudes, home background, classroom experience, and personal effort. Predictors of the model are constructed by polynomials of the visible and latent factors and their interactions in a multivariate Taylor series. Significant predictors at α = .05 level are selected through a backward elimination procedure in Statistical Analysis System (SAS). The structure of the four latent factors and the model complexity have been compared between the two countries in terms of their educational, political, social and cultural contexts.
An Empirical Approach toward the Prediction of Students' Science Achievement in the United States and the Peoples' Republic of China

The development of prediction models for assessing students' science achievement is a fundamental question in science education (Dryden, 1987). Yet, no prediction model is uniformly supported by theories. The structure of the model may also vary across countries, depending on their cultures, social systems and schools. The purpose of this comparative research is to explore a possible empirical model for prediction of students' science achievement in China and the United States.

Rationale

The United States of America (USA) and the People's Republic of China (PRC) are two leaders in the world community. Almost equal in land area, China has nurtured the largest population in the world, and the United States has developed the most advanced industrial and technological civilization. While the economy of the United States has been the largest for more than a hundred years, it has been predicted that China may replace the position of the United States by the turn of this century (Mitchell, 1994). Currently, few countries play roles similar to the United States and China. As a result, China and the United States were chosen in this study to conduct an international comparison.

In spite of various international differences, national development in both the U.S. and China is essentially based on the effectiveness of their education, especially in the area of mathematics, science and technology. Purves (1987) pointed out: "To look at the effectiveness of any system, one needs to get beyond it" (p.27). Under the assumption that countries can learn from each other, this comparative study between China and the United States may provide valuable information for improving the prediction of Chinese and American students' science achievement.
Most prediction models in education postulate a linear relationship between student science achievement and related personal, school, or social predictors (Sockloff, 1976). At least two major reasons exit for using a linear model. First, a linear model is simple. Since no other models have been consistently supported by theories in science education, it is tempting to choose the simplest one, a linear model, in a preliminary exploration. Second, a large number of alternatives to a linear model exist. Each alternative is based on a non-linear function, and it is impossible to verify all the potential nonlinear functions in a comparative study.

Nevertheless, a linear model is not a panacea. Several researchers have reported nonlinear relations between measures of achievement and direct and/or proxy measures of classroom practices (e.g., Brophy & Evertson, 1974; Loucks, 1975; Rim & Coller, 1978; Soar, 1966, 1968, 1971, 1973; Soar & Soar, 1972). Flanders (1970) indicates that “the main credit for identifying and conceptualizing nonlinear (or curvilinear) relationships belongs to Soar” (p. 403). Soar and Soar (1976) claim:

Although linear relationships have most often been used in studies of teaching effectiveness to identify relationships between classroom behavior and pupil gain, it seems clear that they are limited in the extent to which they can help us answer the question of what good teaching is. They are simplistic in implying that if some of a behavior is good, more is better and once the question is raised, it becomes difficult to imagine very many behaviors for which increasing amounts would be unqualifiedly good. (p.265) Nonlinear relations were found between measures of achievement gain and measures of teacher behavior which appeared to represent teacher limitation of pupil freedom in the development of subject matter and thought. (p.263)

Best and Kahn (1993) point out:

Only within the last century has the methodology of science been applied to the study of various areas of human behavior. (p.7) By attempting to apply the rigorous, systematic observation and analysis used in the physical and biological sciences to areas of social behavior, the social sciences have grown and have advanced humanity’s knowledge of itself. (p.7)

In physical and biological sciences, whenever a problem has no theoretical solution in sight, experiments are conducted and theoretical explanations are pursued based on the empirical
results. A similar situation exists in the prediction of student science achievement. Accordingly, an empirical approach is taken in this study to compare the international differences in the model of prediction.

Mathematically, under the condition of the Taylor Theorem (Ayres, 1964), functions of prediction models, linear or nonlinear, can be expressed as a Taylor polynomial series. For example, a linear function:

\[ a \cdot x + b = b + a \cdot x + 0 \cdot x^2 + 0 \cdot x^3 + 0 \cdot x^4 + \ldots ; \]

and nonlinear functions:

\[ e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \frac{x^4}{4!} + \ldots ; \]

\[ e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \frac{x^4}{4!} + \ldots ; \]

\[ \cos(x) = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \ldots ; \]

\[ \ln(1 + x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \ldots ; \]

\[ \arcsin(x) = x + \frac{1 \cdot x^3}{2 \cdot 3} + \frac{1 \cdot 3 \cdot x^5}{2 \cdot 3 \cdot 5} + \ldots ; \]

and

\[ \arctan(x) = x - \frac{x^3}{3} + \frac{x^5}{5} - \frac{x^7}{7} + \ldots . \]

Hence, the exploration of empirical models is simplified to the identification of a set of polynomial coefficients. It has been proved in calculus that within a region of convergence, a truncated Taylor series provides a good approximation of the original function (Ayres, 1964).
The validity of an empirical approach depends on two conditions. First, one needs well-designed data sets which include the necessary information about the research variables. Second, the data must contain a large number of observations to estimate the coefficients of high degrees of polynomials and interactions. These two conditions served as a benchmark in the selection of the empirical data base.

**Data Selection**

Walberg (1983) has pointed out: "The best and perhaps only test data that permit reliable international comparisons of science achievement were obtained by the International Association for the Evaluation of Educational Achievement" (p.6). The International Association for the Evaluation of Educational Achievement (IEA) is an international research organization. Members of IEA are major educational research institutions from each participating country. The broad purpose of the IEA research is to study the relationship between relevant input factors in social, economic, and pedagogical realm and output as measured by performance on international tests measuring both cognitive and non-cognitive outcomes (Postlethwaite, 1974). According to Husen (1987), "The association has been one of the most influential research efforts in the history of educational research, and it certainly has done the best known international research on education" (p.29).

The most recent IEA data in science education were collected through the Second IEA Science Study (SISS), an international project designed to provide an overview of science education across the world (Keeves & Rosier, 1981). The project started in 1981 and involved twenty-three countries. The survey was conducted at three population levels: 5th grade; 9th grade; and 12th grade (Jacobson & Doran, 1988). The development of the international instruments for each population was a collaborative effort involving all participating countries to ensure the fairness of cross-national comparisons.

Both China and the United States participated in the SISS project. The results are
presented in a three-volume IEA publication (Rosier & Keeves, 1991; Postlethwaite & Wiley, 1992; and Keeves, 1992). Unfortunately, as a reviewer stated (Gottfried, 1993), "these volumes do not follow a format that helps the reader make sense of the study" (p. 328).

In the United States, SISS was conducted in two phases. In preparing the three-volume publication, the U.S. SISS advisory panel directed that only the data from the Phase II SISS survey in 1986 be used as the student data in the IEA international comparisons (Postlethwaite & Wiley, 1992). However, this direction has not been followed through the data analysis process. The following paragraph is quoted from the second volume of the IEA publication:

This "direction" was followed but it created two problems: the first was that multivariate analyses for the United States became virtually impossible because many variables were not administered in the second round of testing, since no rotated tests were employed at Populations 1 and 2, and several items were dropped from the biology, chemistry, and physics tests. Hence, the "direction" could not be followed for all data analyses as it would have eliminated comparisons involving the United States. In the cases where these data were used, the purpose was not to estimate population means or proportions, but to explore variability and assess relationships of particular student and school characteristics to achievement. (Postlethwaite and Wiley, 1992; p. 7)

On the other hand, SISS in China was named the "SISS Pilot Study" because the survey was conducted only at the 9th grade level in three large cities, Beijing, Tianjin and Taiyuan (Rosier & Keeves, 1991). The primary objective of the SISS Pilot Study was to help Chinese researchers to understand the IEA methodology. The survey results, however, do not reflect the nature of Chinese science education since the population in rural regions has been excluded in the sample design.

In 1988, the China IEA Center modified the IEA instruments and launched a SISS Extension Study (SES) at the 9th grade level in seven provinces. Coincidentally, the same IEA instruments had been revised in the U.S. in 1986 for the Phase II SISS survey. Common instruments of the Phase II SISS and SES which included almost all Phase II SISS student variables (Humrich, 1988) are listed in Table 1. According to a representative of the National
Science Foundation, the data collected from the revised instruments have the quality for the IEA international assessment (Postlethwaite and Wiley, 1992).

It should be noted that SES was originally designed for an inter-province comparison or a province-other country comparison. Each of the seven provinces in China was treated as an independent system. Hence, there is no legitimate method for integrating the survey over the seven provinces. To use the SES data for an international comparison, one of the provinces must be identified to represent the Chinese situation.

In China, the eastern and southern areas are more developed than the northern and western areas. On balance, a central province is more representative of the entire country than a boundary province. Among the SES seven provinces, Hubei province is the only one located in the central region of China. Thus, the data from Hubei province is chosen in this research to represent the Chinese situation in 1988.

In summary, as suggested by the United States SISS advisory panel, the Phase II SISS is better than the Phase I SISS. On the other hand, compared to the SISS Pilot Study, the SES has at least two advantages: (1) The SES data were collected in both urban and rural regions; (2) The population in each province is larger than the population of the SISS Pilot Study. Hence, the China SES and the U.S. Phase II SISS data provide the best opportunity to compare school science education between the two countries.

The research presented in this paper is based on the SES and Phase II SISS data sets. Although at least thirteen dissertations (Chandavarkar, 1988; Chang, 1988; Clive, 1983; Dryden,
Empirical Model

1987; Ekeocha, 1986; Ferko, 1989; Humrich, 1988; Kanis, 1988; Micik, 1986; Miller, 1985; Baker, 1989; Bayer, 1990; O'Rafferty, 1991) have examined on the U.S. SISS project, none of the studies explored an empirical polynomial model for prediction of students' science achievement. On the other hand, the SISS Extension Study (SES) was a national project conducted by the China IEA Center, and the data have not yet been forwarded to the IEA International Headquarters. The first author was a member of the Chinese IEA team and participated in the first two stages of the SES survey, population investigation and data collection. The present research is the first report in which the SES data base is employed in the construction of an empirical model. Because the SES and Phase II SISS data sets contain a large number of observations and appropriate research variables, they fulfill the two conditions, large and informative data, necessary for the construction of potentially valid empirical models of prediction.

Two limitations are embedded in this study. First, this empirical study is based on the common instruments of SES and Phase II SISS at the ninth grade level. The two-country comparison is not concurrent because the U.S. data were collected in 1986 while the Chinese data were collected in 1988. Inaccuracy may also result from the fact that the Chinese information is represented by the SES data in Hubei province. The construction of empirical models has been confined within the common variables of the SES and Phase II SISS projects, and other variables not present in the two data bases can not be taken into the consideration.

Second, results of this empirical study should be considered as preliminary, open to multiple interpretations, and perhaps difficult to interpret. Differences or difficulty of interpretation may be due to the instability of the results, mis-codings in the data, and confounding variables which were not considered in SES and Phase II SISS, or are even unknown in nowadays. Thus, the exploratory results presented herein need further empirical reconfirmation. Only those that are consistently reconfirmed by follow-up empirical studies form the foundation of sound interpretation and theoretical explanation. While the exploratory interpretations made in
this paper represent the authors' best knowledge, and may provide information to improve future empirical studies, readers are urged to exercise caution due to possible statistical artifacts and post hoc fallacies.

Research Questions

To fully utilize the information collected in SES and Phase II SISS, all common variables of the two projects are employed in this study to construct empirical models for prediction of the students' science achievement. Presented in Table 1, these variables are related to six aspects, gender, attitude, home background, classroom experience, personal effort, and science achievement. To date, no theoretical solutions have been reported regarding the integrated effects of the first five aspects, linear or nonlinear, on students' achievement. In an empirical exploration, neither linear nor nonlinear relations should be imposed as a pre-condition on the model of prediction. Instead, the first five aspects are treated as five factors, and a unified Taylor series (Ayres, 1964), including linear and nonlinear models as special cases, is adopted as a mathematical function in the model construction. The questions that guide this research are:

1. What are the linear or nonlinear factors and their interactions which have significant effects on the students' science achievement?
2. Do differences exit between the United States and China in terms of the factor structures and interpretations?
3. Do differences in complexity exist between the Chinese and American models, and can the differences be explained based on differing educational, political, social and cultural context in each country?

Methods

The factors affecting students' science achievement can be characterized as visible, such as
gender, or latent, such as students' attitude, classroom experience, home background and personal effort. Latent factors which are not directly measurable may be interpreted through students' responses to certain related questions. These questions are called indicators of the latent factors (Joreskog & Sorbom, 1984). Statistically, the first principal component, which accounts the largest proportion of the indicator information, is recommended to represent a latent factor (e.g., 1982). The total number of appropriate latent factors is called the dimension of latent prediction space. The indicators of students' attitude, classroom experience, home background, and personal effort are listed in Table 2. Thus, the dimension of the latent prediction space identified by the total number of latent factors is 4 in this study. These latent dimensions are yet to be reconfirmed through the examination of multicollinearity using the SES and Phase II SISS data sets.

| Table 2 inserted around here |

In general, when a factor is nearly a linear combination of other factors, the affected estimates are unstable and have high standard errors. This situation is known in statistics as multicollinearity (SAS, 1982; p. 54). Jagodzinski, Weede and Tiefenbach (1981) pointed out: "Even in second-order polynomial regression there are some problems; often there is extreme multicollinearity between simple and squared terms" (p. 447). Liu (1981) studied multicollinearity in her dissertation. She suggests principal component regression as a means of ameliorating the adverse effect of linear dependencies in a polynomial regression model. The potential multicollinearity of latent factors is examined in this study by scree plots from the principal component analysis in SAS. If none of the factors is a linear combination of others, the latent dimension identified by the indicators of the four factors should be no less than 4. Otherwise, the data matrix of the latent factors is singular, and multicollinearity occurs (Graybill, 1976).
Without pre-conditions of linear or nonlinear models, the effects of the five factors, visible or latent, on students' science achievement are investigated using a multivariate Taylor series. A multivariate Taylor series is illustrated through the following bivariate Taylor series (e.g., Franklin, 1944):

$$f(x,y) = A_{00} + A_{10}x + A_{01}y + A_{20}x^2 + A_{11}xy + A_{02}y^2 + \ldots + A_{pq}x^py^q + \ldots$$

where $x$ and $y$ are factors of the dependent variable $f(x,y)$, and $A_{00}, A_{10}, A_{01}, \ldots, A_{pq}, \ldots$ are Taylor coefficients. It is apparent in the multivariate Taylor model that predictors of the dependent variable $f(x,y)$ are polynomials ($x, y, x^2, y^2, \ldots$) and interactions ($xy, x^py^q, \ldots$) of the two factors, $x$ and $y$. The Taylor coefficients ($A_{00}, A_{10}, A_{01}, \ldots, A_{pq}, \ldots$) are estimated through least square regression. A linear model corresponds to the case when the values of $A_{pq}$'s ($p+q>1$) equal zero, while a nonlinear model of prediction contains the effects of higher degrees of polynomials or interactions. Hence, a multivariate Taylor model includes linear and nonlinear models as special cases, and the highest degree of the polynomials or interactions indicates the appropriateness of linear and nonlinear models.

Graybill (1976) further states: "We assume that the degree of the polynomial $\mu(x)$ is less than or equal to $K$, and the problem is to determine the exact degree" (p. 303). Based on the common variables of SES and Phase II SISS, predictors of students' science achievement are polynomials of the five factors, gender, attitude, classroom experience, home background, and personal effort, and their interactions. To obtain a good approximation, higher order polynomials and interactions are included in the exploratory model until the degree of $(K+1)$ is reached, at which the higher order predictors are no longer significant at $\alpha = .05$ level. $K$, then, is the highest degree of polynomial in the prediction model. Significant predictors of the model are selected from all possible polynomials and interactions which have degrees less than or equal to $K$.

To facilitate construction of models, three adjustments have been made on the SES and
Phase II SISS data bases. First, the attitude scales (ATT05-36) are recoded as: agree = 1, uncertain = 0, and disagree = -1, and are treated as an interval scale. Second, parents' education (P_ED) is defined as: P_ED = max (FPOSTED, MPOSTED), the highest level of father's and mother's education. The variable of parents' education is used to replace FPOSTED and MPOSTED as an indicator of students' home background. Third, the visible factor, SEX, is recoded as: female =0 and male =1. The advantages of this recoding are: (1) SEX can be used as a dummy variable for regression; and (2) the polynomial model is simplified because (SEX)^n=(SEX) for any integer n.

Deletion of missing values is summarized in Table 3. The designed sample sizes of SES and Phase II SISS are proportional to the students' populations. The achieved samples are created by deleting cases which have missing values for the common variables in Table 1. In both the U.S. and Chinese data sets, the percentage of missing values is less than 20%, and the achieved sample in each country contains more than 2000 students. Thus, in this exploratory study, the missing values are deleted from the SES and Phase II SISS data sets.

Results

**Dimension of Latent Prediction Space**

Dimension of the latent prediction space is empirically identified by scree plots through the principal component analysis in Statistics Analysis System (SAS). Information on indicators is represented by a set of orthogonal principal components. By default, SAS treats the principal
components which have eigenvalues greater than 1 as information and the remaining components as noise. A disadvantage of this default option is that the eigenvalues of some principal components may be so close to 1 that it is not appropriate to set the threshold among them. In a scree plot, eigenvalues are plotted for each principal component. Hence, a clear-cut threshold can be selected to differentiate principal components between information and noise. The dimension of the latent space is determined by the total number of orthogonal principal components identified to represent information of the indicators.

Scree plots for the Phase II SISS and SES surveys are presented in Figures 1 and 2 respectively. Inspection of both figures shows that the fourth, fifth and sixth principal components have eigenvalues around 1, and the differences of eigenvalues between the fourth and fifth principal components is larger than the difference between the fifth and sixth principal components. Hence, the dimension of the latent prediction space is four based on the Chinese and U.S. data sets. This result reconfirms the fact that four latent factors exist among the common variables of SES and Phase II SISS.

Structure of the Four Latent Factors

The indicators are categorized into four groups in Table 2 based on the contents of these items. The first principal component is calculated for each group of indicators, and the structure of
the latent factors is expressed by factor loadings of the indicators on their corresponding first principal component. The factor loadings calculated from the U.S. and Chinese data sets are listed in Table 4.

Table 4 inserted around here

**Significant Predictors of the Empirical Model**

Predictors of the empirical model are the polynomials and interactions of the visible and latent factors, gender, attitude, classroom experience, home background and personal effort. The criterion of selecting significant predictors has been set at $\alpha = .05$ level. Only those predictors which have regression coefficients significantly differing from zero are retained in the model. The coefficients of regression are estimated through the backward elimination procedure in SAS. The empirical model based on the American data contains significant predictors up to and including the fifth degree of polynomial. On the other hand, no significant predictors beyond the fourth degree of polynomial are found significant in the Chinese model. Hence, the highest degree of predictor is 4 for the Chinese model, and 5 for the U.S. model. The significant predictors of polynomials and interactions are listed in Tables 5 and 6, respectively.

Table 5 inserted around here

Table 6 inserted around here
Summary

Indicators of latent factors in the common instruments of SES and Phase II SISS are classified into four groups, attitude, classroom experience, home background and personal effort. The four dimensions of latent prediction space are confirmed by the scree plots from the principal component analysis. The latent factors are represented by the first principal components in each of the four latent dimensions. Predictors of the model are constructed by polynomials of the visible (gender) and latent factors and their interactions in the multivariate Taylor series. Significant predictors at \( \alpha = .05 \) level are selected through a backward elimination procedure in Statistical Analysis System (SAS). The Chinese and American predictors in Tables 5 and 6 are summarized in equations (1) and (2):

\[
Y = \beta_{1u} + \beta_{1u} \cdot C + \beta_{2u} \cdot E + \beta_{3u} \cdot S + \beta_{4u} \cdot (E^2) + \beta_{5u} \cdot (H^2) + \beta_{6u} \cdot (S \cdot H \cdot C) + \beta_{7u} \cdot (H \cdot A \cdot E) + \\
\beta_{8u} \cdot (H \cdot E \cdot C) + \beta_{9u} \cdot (C^2 \cdot A) + \beta_{10u} \cdot (A^2 \cdot S) + \beta_{11u} \cdot (C^2 \cdot S) \\
\]

(1)

\[
Y = \beta_{1u} + \beta_{1u} \cdot A + \beta_{2u} \cdot E + \beta_{3u} \cdot H + \beta_{4u} \cdot S + \beta_{5u} \cdot (C^2) + \beta_{6u} \cdot (H^2) + \beta_{7u} \cdot (E^2) + \beta_{8u} \cdot (E^4) + \\
\beta_{9u} \cdot (E^6) + \beta_{10u} \cdot (H^2 \cdot E) + \beta_{11u} \cdot (S \cdot A^2) + \beta_{12u} \cdot (S \cdot C^2) + \beta_{13u} \cdot (S \cdot H \cdot A) + \beta_{14u} \cdot (S \cdot H \cdot E) + \\
\beta_{15u} \cdot (H^2 \cdot A) + \beta_{16u} \cdot (A^2 \cdot C) + \beta_{17u} \cdot (C^2 \cdot E) + \beta_{18u} \cdot (E^2 \cdot C) + \beta_{19u} \cdot (S \cdot H^2 \cdot A) + \\
\beta_{20u} \cdot (S \cdot H^2 \cdot A^2) \\
\]

(2)

where \( y \) represents the students' science achievement, and \( S, H, E, A, C, \beta_{1u} \) and \( \beta_{2u} \) are defined in the footnotes of Tables 5 and 6.

The number of significant predictors constructed by the five visible or latent factors is listed in Table 7.
Discussion

The focus of this comparative research is the identification of significant predictors of students' science achievement based on the common variables of SES and Phase II SISS. Since no theoretical solution to this problem is in sight, an empirical approach was adopted to construct exploratory models. The results of the American and Chinese models can be classified into consistent and inconsistent categories. The consistent part is discussed in this section, and the inconsistent part, which needs further investigations, is highlighted at the end of this discussion.

The significant items of the empirical Taylor series at $\alpha = .05$ level are called the predictors of students' science achievement constructed by the polynomials and interactions of the students' visible factor, gender, and latent factors, attitude, home background, personal effort, and classroom experience. The structure of the four latent factors is presented by factor loadings in Table 4. It is interesting to note in this table that the corresponding factor loadings between the U.S. and China have the same positive or negative signs. Thus, the structural differences between the Chinese and American predictors are in their magnitudes rather than directions. The similarities and differences of the empirical models are discussed in this section in terms of the educational, political, social, and cultural contexts in each country.

Latent Factor Structures

The structures of the latent factors are expressed by factor loadings in Table 4. The first common point to note is that the factors of home background and personal efforts have two indicators, and are represented by their first principal component. In a two-indicator principal component analysis, the axis of the first principal component is set at a direction of $45^\circ$ to each indicator axis. Accordingly, the factor loading of either indicator is: $\sin(45^\circ) = \cos(45^\circ) = 0.707$, i.e.,
the two indicators are weighted equally in the construction of their latent factor. Hence, the identical factor loadings of the two factors in both China and the U.S. are caused by the principal component definition in the two-indicator cases rather than the actual situations of the two countries.

The other two latent factors, students' attitude and classroom experience, have more than two indicators. Their factor loadings reflect the relative contributions of each indicator to the corresponding latent factor. Thus, the interpretation of the factor loadings in this section focuses only on the factors of students' attitude and classroom experience.

In the U.S. model, indicators which have the largest contributions to the students' attitudes are the students' interest in science (Table 4: P_ATT34) and their feelings of enjoying school science experience (Table 4: P_ATT35). This result is also supported by the Chinese data (Table 4). In addition, attitudes of the Chinese students are strongly represented by their school pressure (Table 4: P_ATT06). In both countries, teachers' demonstrations and students' experiments are important science activities (Table 4: P2DES08 and P2DES18). But, the effects of these activities in China are not as strong as in the United States in determining the factor of classroom experience. A more important contribution in China comes from students' tests (Table 4: P2DES14).

Schools in China are classified as key schools and general schools. A major criterion of the classification is the number of students in each school who have passed the National College Entrance Examination. No matter what kind of pressure exists on a school, if many students in that school can pass the examination, the school will be promoted as a key school. This is consistent with what Deng, Xiao-ping said, "It does not matter whether a cat is white or black as long as it catches rats".

In a centralized educational and political system, examination of students is a feasible
method of avoiding corruption in students' admission to higher education. The Chinese government takes great care to eliminate cheating on the National College Entrance Examination. As a result, students must pass the examination in order to pursue formal higher education regardless of parents' power and influence. According to the wisdom of Chinese educators, the best way to cope with the examination is to give students difficult tests in secondary education. Hence, the pressure of students' tests as the highest factor loading on Chinese classroom experience is readily explained.

In both the U.S. and China, teachers' demonstrations and students' experiments are important laboratory activities in science education. Nevertheless, in China it is impossible to provide a sufficient amount of laboratory equipment to simultaneously measure the experimental skills of millions of high school graduates in the National College Entrance Examination. Thus, this important examination is a paper-pencil test, and does not require experimental skills to achieve good scores. Moreover, China is a developing country and many schools, especially in rural areas, do not have well equipped teaching laboratories. Compared to the U.S. model, the lack of equipment and the pressure of school examination appear to be major reasons for the smaller loading of the laboratory activities on the Chinese classroom experience.

Relative Complexity of the Models

The predictors of students' science achievement are constructed by polynomials and interactions of gender, attitude, home background, personal effort and classroom experience. The model complexity is shown in Table 8 in terms of the numbers and highest degrees of these predictors. Inspection of Table 8 shows that the American model contains more significant predictor, and has higher degrees of polynomials or interactions. Hence, the American model is more complicated than the Chinese model. The interpretation of differences in complexity in this paper is based on the differing social and cultural contexts in each country.
The United States is a country populated by people from all over the world. The compulsory education enforced in the U.S. requires school-age children from various cultural backgrounds to complete their education at no less than the ninth grade level. Although education is compulsory, not all U.S. students perceive an equal opportunity to learn. Coleman, Campbell, Hobson, McPartland, Mood, Weinfeld and York (1966) found that many minority students felt that somebody blocked them from success, even though they had the ability to learn. Also, the authority to determine the school curricula is the responsibility of individual school districts or communities. In summary, a heterogeneous student population and diversified curricula are two variables which increase the complexity of predicting students' science achievement in the United States.

On the other hand, China has been a unified country since 221 B.C. About ninety-four percent of Chinese population is Han nationality. "China" in Chinese means "the middle kingdom". It has been said that the Chinese people were the descendants of a dragon and their Emperor was the son of the God. The national minorities in remote areas were ruled by courtiers of the Emperor, and have been assimilated as members of the Chinese family after age-long cultural communications. The feudal system was not abandoned until the beginning of this century. The cultural foundation of Chinese feudalism is Confucian philosophy. Confucius stressed that those who study mentally should govern the people who work physically, and those who work physically should serve the people who study mentally. Under this cultural background, education is a vehicle to promote the social status of a family.

Improvement of education is also closely tied to the development of the Chinese economy. Because the feudal social system impeded Chinese economic development for more than 2000
years, China remains a third world country in many aspects. For example, compulsory education has not yet been fully enforced in China. In 1988, less than half of the children finished their middle school education. Those who studied at the ninth grade were selected through the regional Middle School Entrance Examinations. Thus, the Chinese model of prediction is based on the information from a more homogeneous cohort of selected middle school students.

Moreover, authority to determine Chinese school curriculum belongs to the central government. The national curriculum has an effect of standardizing the school science education over the country. Hence, it is understandable that the Chinese model is less complicated given the unified culture, selected students, and standardized curriculum.

Inconsistent results between the two countries may result from empirical errors, essential international differences and confounding factors which have not been included in construction of the model. It is interesting to note in Table 7 that the numbers of significant predictors are different in the Chinese and U.S. models. Because the predictors are constructed by the five different factors and are measured on different scales, the larger regression coefficients do not necessarily imply greater contributions to the students' science achievement. The contribution of each factor depends on the regression coefficients and the scales of the predictors constructed by the polynomials and interactions. Further questions identified by this research and subject to future empirical investigations are:

1. Can the empirical models be further simplified to improve the comparative interpretation?
2. Will specific structures of the significant predictors re-appear in future IEA surveys?
3. Do the factor loadings and model complexity in the two countries have additional physical meaning?

Graybill (1976) points out:

One of the difficulties with the all regression procedures, in addition to the high amount of computation that is required if K is large, is the interpretation of the results. If one
computes all possible multiple correlation coefficients, it is an immense task to interpret them. (p.449)

Although not all the empirical results are readily interpretable, the tentative interpretations made in this paper may facilitate the development of better empirical models in future. It is the authors' belief that the prediction of students' science achievement in the United States and the Peoples' Republic of China can be improved through continuing efforts on the construction and interpretation of empirical models in each country.
References


### Table 1

**Common Instruments of SES and Phase II SISS**

<table>
<thead>
<tr>
<th>Variable</th>
<th>Instrument</th>
</tr>
</thead>
</table>
| SEX      | What is your sex?  
          | (A) male; (B) female. |
| FPOSTED  | What is the highest level of school your father completed? |
| MPOSTED  | What is the highest level of school your mother completed? |
| HOMEBOOK | How many books are there in your home? |
| HMWKALL  | About how many hours a week do you usually spend on homework or other school work out of class for all subjects? |
| HMWKSCI  | About how many hours a week do you usually spend on homework or other school work out of class for science subjects? |
| P_ATT05  | Science is very important for a country's development.  
          | Agree; Disagree; Uncertain. |
| P_ATT06  | School is not very enjoyable.  
          | Agree; Disagree; Uncertain. |
| P_ATT34  | Science is an enjoyable school subject.  
          | Agree; Disagree; Uncertain. |
| P_ATT35  | The science taught at school is interesting.  
          | Agree; Disagree; Uncertain. |
| P_ATT36  | Science is a difficult subject.  
          | Agree; Disagree; Uncertain. |
| P2DES01  | We use a textbook for our science lessons  
          | Often; Sometimes; Never. |
| P2DES02  | We use books other than textbook for learning science.  
          | Often; Sometimes; Never. |
| P2DES06  | We watch the teacher do experiments during our science lessons.  
          | Often; Sometimes; Never. |
| P2DES14  | We have tests on what we learned in science.  
          | Often; Sometimes; Never. |
| P2DES18  | We do experiments as part of the science lessons  
          | Often; Sometimes; Never. |
| SMT      | Science test score |
Table 2

Structure of Indicator Variables

<table>
<thead>
<tr>
<th>Home Background</th>
<th>Personal Effort</th>
<th>Attitude</th>
<th>Classroom Experience</th>
</tr>
</thead>
<tbody>
<tr>
<td>FPOSTED</td>
<td>HMWKALL</td>
<td>P_ATT05</td>
<td>P2DES01</td>
</tr>
<tr>
<td>MPOSTED</td>
<td>HMWKSCI</td>
<td>P_ATT06</td>
<td>P2DES02</td>
</tr>
<tr>
<td>HOMEBOOK</td>
<td></td>
<td>P_ATT34</td>
<td>P2DES08</td>
</tr>
<tr>
<td></td>
<td></td>
<td>P_ATT35</td>
<td>P2DES14</td>
</tr>
<tr>
<td></td>
<td></td>
<td>P_ATT36</td>
<td>P2DES18</td>
</tr>
</tbody>
</table>

Table 3

Sample Sizes of SES and Phase II SISS Data Sets

<table>
<thead>
<tr>
<th>Sample</th>
<th>The United States</th>
<th>P. R. China</th>
</tr>
</thead>
<tbody>
<tr>
<td>Designed Size</td>
<td>2519</td>
<td>3000</td>
</tr>
<tr>
<td>Achieved Size</td>
<td>2027</td>
<td>2871</td>
</tr>
<tr>
<td>Missing Value (%)</td>
<td>19</td>
<td>4</td>
</tr>
</tbody>
</table>
Table 4

Structures of the Latent Factors

<table>
<thead>
<tr>
<th>Latent Factor</th>
<th>Indicator</th>
<th>Factor Loadings</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>China</td>
</tr>
<tr>
<td>Attitude</td>
<td>P_ATT05</td>
<td>0.276</td>
</tr>
<tr>
<td></td>
<td>P_ATT06</td>
<td>-0.506</td>
</tr>
<tr>
<td></td>
<td>P_ATT34</td>
<td>0.562</td>
</tr>
<tr>
<td></td>
<td>P_ATT35</td>
<td>0.560</td>
</tr>
<tr>
<td></td>
<td>P_ATT36</td>
<td>-0.196</td>
</tr>
<tr>
<td>Classroom Experience</td>
<td>P2DES01</td>
<td>0.387</td>
</tr>
<tr>
<td></td>
<td>P2DES02</td>
<td>0.274</td>
</tr>
<tr>
<td></td>
<td>P2DES08</td>
<td>0.501</td>
</tr>
<tr>
<td></td>
<td>P2DES14</td>
<td>0.535</td>
</tr>
<tr>
<td></td>
<td>P2DES18</td>
<td>0.488</td>
</tr>
<tr>
<td>Home Background</td>
<td>P_ED</td>
<td>0.707</td>
</tr>
<tr>
<td></td>
<td>HOMEBOOK</td>
<td>0.707</td>
</tr>
<tr>
<td>Personal Effort</td>
<td>HMWKALL</td>
<td>0.707</td>
</tr>
<tr>
<td></td>
<td>HMWKSCI</td>
<td>0.707</td>
</tr>
</tbody>
</table>
Table 5

Significant Polynomial Predictors of Students' Science Achievement

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept (β₀)</td>
<td>56.183</td>
<td>0.0001</td>
<td>52.707</td>
<td>0.0001</td>
</tr>
<tr>
<td>A</td>
<td>-2.279</td>
<td>0.0001</td>
<td>-0.670</td>
<td>0.0069</td>
</tr>
<tr>
<td>E</td>
<td>2.861</td>
<td>0.0001</td>
<td>1.970</td>
<td>0.0001</td>
</tr>
<tr>
<td>H</td>
<td>1.940</td>
<td>0.0001</td>
<td>8.248</td>
<td>0.0001</td>
</tr>
<tr>
<td>S</td>
<td>6.026</td>
<td>0.0001</td>
<td></td>
<td></td>
</tr>
<tr>
<td>C²</td>
<td>-1.011</td>
<td>0.0001</td>
<td>-0.416</td>
<td>0.0032</td>
</tr>
<tr>
<td>E²</td>
<td>-1.909</td>
<td>0.0001</td>
<td>0.428</td>
<td>0.0040</td>
</tr>
<tr>
<td>E³</td>
<td>-0.084</td>
<td>0.0003</td>
<td></td>
<td></td>
</tr>
<tr>
<td>E⁴</td>
<td>-0.124</td>
<td>0.0012</td>
<td></td>
<td></td>
</tr>
<tr>
<td>E⁵</td>
<td>0.040</td>
<td>0.0094</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Notes:

[^1] The polynomial predictors in Table 5 and the interaction predictors in Table 6 are selected together through a backward elimination procedure in SAS, and the significant level has been set at α = .05.

[^2] The factor names are abbreviated as: A = Attitude; C = Classroom Experience; E = Effort; H = Home Background; S = Sex; and β₀ corresponds to a zero degree of polynomials.
Table 6

**Significant Interaction Predictors of Students' Science Achievement**

<table>
<thead>
<tr>
<th>Interaction Predictors[^2]</th>
<th>U.S. Parameter Estimate ($\beta_m$)</th>
<th>P-Value</th>
<th>China Parameter Estimate ($\beta_m$)</th>
<th>P-Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>H*E</td>
<td>1.266</td>
<td>0.0019</td>
<td>0.454</td>
<td>0.0409</td>
</tr>
<tr>
<td>S*A²</td>
<td>-0.751</td>
<td>0.0073</td>
<td>-0.256</td>
<td>0.0393</td>
</tr>
<tr>
<td>S*C²</td>
<td>0.930</td>
<td>0.0082</td>
<td>0.254</td>
<td>0.0495</td>
</tr>
<tr>
<td>S<em>H</em>A</td>
<td>-1.126</td>
<td>0.0021</td>
<td>0.143</td>
<td>0.0198</td>
</tr>
<tr>
<td>S<em>H</em>C</td>
<td>-1.449</td>
<td>0.0073</td>
<td>0.143</td>
<td>0.0198</td>
</tr>
<tr>
<td>H<em>A</em>E</td>
<td>0.664</td>
<td>0.0079</td>
<td>0.254</td>
<td>0.0495</td>
</tr>
<tr>
<td>H<em>E</em>C</td>
<td>-0.198</td>
<td>0.0416</td>
<td>0.143</td>
<td>0.0198</td>
</tr>
<tr>
<td>H²*A</td>
<td>-0.541</td>
<td>0.0131</td>
<td>-0.056</td>
<td>0.0010</td>
</tr>
<tr>
<td>A²*C</td>
<td>-0.541</td>
<td>0.0131</td>
<td>-0.056</td>
<td>0.0010</td>
</tr>
<tr>
<td>C²*A</td>
<td>-0.317</td>
<td>0.0227</td>
<td>-0.127</td>
<td>0.0017</td>
</tr>
<tr>
<td>C²*E</td>
<td>-0.317</td>
<td>0.0227</td>
<td>-0.127</td>
<td>0.0017</td>
</tr>
<tr>
<td>A³*S</td>
<td>-0.814</td>
<td>0.0108</td>
<td>0.457</td>
<td>0.0034</td>
</tr>
<tr>
<td>C³*S</td>
<td>-0.814</td>
<td>0.0108</td>
<td>0.457</td>
<td>0.0034</td>
</tr>
<tr>
<td>E³*C</td>
<td>-0.814</td>
<td>0.0108</td>
<td>0.457</td>
<td>0.0034</td>
</tr>
<tr>
<td>S<em>H²</em>A</td>
<td>-0.814</td>
<td>0.0108</td>
<td>0.457</td>
<td>0.0034</td>
</tr>
</tbody>
</table>

Notes:

[1] The interaction predictors in Table 6 and the polynomial predictors in Table 5 are selected together through a backward elimination procedure in SAS, and the significant level has been set at $\alpha = .05$.

[2] The factor names are abbreviated as: A = Attitude; C = Classroom Experience; E = Effort; H = Home Background; S = Sex; and $\beta_0$ corresponds to a zero degree of polynomials.
Table 7

The Number of Significant Predictors Constructed by the Factors of Students' Science Achievement

<table>
<thead>
<tr>
<th>Country</th>
<th>Gender</th>
<th>Attitude</th>
<th>Classroom Experience</th>
<th>Personal Effort</th>
<th>Home Background</th>
</tr>
</thead>
<tbody>
<tr>
<td>U.S.</td>
<td>7</td>
<td>7</td>
<td>5</td>
<td>8</td>
<td>8</td>
</tr>
<tr>
<td>China</td>
<td>4</td>
<td>3</td>
<td>5</td>
<td>4</td>
<td>4</td>
</tr>
</tbody>
</table>

Table 8

Comparison of Model Complexity

<table>
<thead>
<tr>
<th>Country</th>
<th>Highest Degrees of the Predictors</th>
<th>The Total Number of Significant Predictors</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Polynomials</td>
<td>Interactions</td>
</tr>
<tr>
<td>U.S.</td>
<td>5</td>
<td>9</td>
</tr>
<tr>
<td>China</td>
<td>4</td>
<td>5</td>
</tr>
</tbody>
</table>
Figure 1
Scree Plot of Eigenvalues for U.S. Data.
Figure 2

Scree Plot of Eigenvalues for China Data

Number of Principal Components

Eigenvalues

0.0 0.5 1.0 1.5 2.0 2.5

0 2 4 6 8 10 12 14 16