DOCUMENT RESUME

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By-Rahmlow, Harold F.; And Others OCCUPATIONAL MATHEMATICS; CONCEPTS OF NUMBER BASES. REPORT NO. 16-U. FINAL REPORT. Washington State Coordinating Council for Occupational Education, Olympia.; Washington State Univ.; Pullman. Dept. of Education. Spons Agency-Office of Education (DHEW), Washington, D.C. Bureau No-BR-7-0031 Grant-OEG-4-7-070031-1626 Note-129p. EDRS Price MF-\$0.75 HC-\$524 Descriptors: *ARITHMETIC, *NUMBERS, *NUMBER SYSTEMS, *PROGRAMED TEXTS, *VOCATIONAL EDUCATION This programed mathematics textbook is for student use in vocational education courses. It was developed as part of a programed series covering 21 mathematical

courses. It was developed as part of a programed series covering 21 manifemented competencies which were identified by university researchers through task analysis of several occupational clusters. The development of a sequential content structure was also based on these mathematics competencies. After completion of this program the student should be able to: (1) change from exponential form to expanded form and vice versa, (2) write a number in the base 10 system in expanded exponential form, (3) write a number in the base two system in expanded exponential form, and (4) convert numbers from base two and base five to base 10. The material is to be used by individual students under teacher supervision. Twenty-six other programed texts and an introductory volume are available as VT 006 882-VT 006 909, and VT 006 975. (EM) 1



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June 1968

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CONCEPTS OF NUMBER BASES,

Project No. 0E7-0031 Contract No. 0EG-4-7-070031-1626 Report No. 16-U

> by Harold F. Rahmlow Kari Ostheiler Clarence Potratz Leonard T. Winchell Arthur Snoey

> > June 1968

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Washington State University, Department of Education, Pullman, Washington State Coordinating Council for Occupational Education, Olympia, Washington

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Page A

OBJECTIVES

- The student should be able to change from exponential form to expanded form and vice versa.
- 2. The student should be able to write a number in the base 10 system in expanded exponential form.
- 3. The student should be able to write a number in the base 2 system in expanded exponential form.
- The student should be able to convert numbers
 from base 2 and base 5 to base 10.

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Page B

Greetings! You are about to begin improving your knowledge of basic mathematics. There are many important uses for the mathematics you are learning.

This booklet is not like your ordinary books. It is designed to help you learn as an individual. On the following pages you will find some information about mathematics. After the information is presented, you will be asked a question. Your answers to these questions will determine how you proceed through this booklet. When you have selected your answer to the question, turn to the page you are told to.

Do not write in this booklet. You may wish to have a pencil and some paper handy so you can write when you want to.

Remember this is not an ordinary book.

- 1. Study the material on the page.
- 2. Read the question on the page (you may want to restudy the material on the page).
- 3. Select the answer you believe is correct.
- 4. Turn to the page indicated by your answer.

Are you ready to begin?

- (a) Yes Turn to page 1
- (b) No Turn to page C
- (c) HELP Go see your teacher

Page C

Your answer was (b) No.

ERIC Full Text Provided by ERIC Well, this booklet is a little different:

Go back and read page B again. After you have read it, you will probably be ready to begin.

In order to understand the main ideas about numbers of different bases, we must know a little about exponents.

Now, an exponent is merely a method for showing repeated multiplications. For example, instead of writing 2 x 2 x 2 x 2, we just write 2^4 (2^4 is read as 2 to the fourth power).

What does 5³ mean?

(a) 3 x 5 Turn to page 5
(b) 5 x 5 x 5 Turn to page 3 100



No! Wrong answer!

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No. 2. 1. 1.

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Return to page 1 and begin this Unit again. Read the material carefully before choosing an answer.

5 x 5 x 5 is correct!

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Now, how would you write a x a x a x a in exponential form?

(a)	a ₄	Turn to page 6
(b)	4a	Turn to page 10
(c)	a	Turn to page 8

Incorrect. $4 \times 7 \neq 7 \times 7 \times 7 \times 7$.

Go to page 7 and work the problem again.



Incorrect.

Five to the third power means that we are going to multiply $\underline{3}$ five's together. This is written as 5 x 5 x 5.

How would you write 10⁵?

(a)	10 x 10 x 10 x 10 x 10	Turn	to page	7
(b)	5 x 10	Turn	to page	2

Whoops! Any number written in the lower right hand corner is called a subscript, not an exponent.

Go to page 3 and choose a different answer.



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 $10 \times 10 \times 10 \times 10 \times 10$ is the correct answer!

Now, how would you write $7 \times 7 \times 7 \times 7$ in exponent form?

(a)	4 x 7	Turn	to	page	4
(b)	4 ⁷	Turn	to	page	2
(c)	7 ⁴	Turn	to	page	3
(d)	47	Turn	to	page	13

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Very good!

Try this problem.

In exponential form, $1/10 \times 1/10 \times 1/10 = ?$.

(a)	1/1000	Turn	to	page	9
(b)	$(\frac{1}{10})^3$	Turn	to	page	11
(c)	$\frac{1}{10}3$	Turn	to	page	17
(d)	3/10	Turn	to	page	21

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While 1/1000 is the correct product of $1/10 \times 1/10 \times 1/10 \times 1/10$, it is <u>NOT</u> the exponential form of $1/10 \times 1/10 \times 1/10$.

What is $1/5 \times 1/5 \times 1/5 \times 1/5$ in exponential form?

(a) $(1/5)^4$ Turn to page 20 (b) 4 x 1/5 Turn to page 21



Your answer is incorrect.

4a means 4 x a, not a x a x a x a.

Let's consider an example to show you why your answer was not correct. Let a = 3, then $4a = 4 \times 3 = 12$, while $a \times a \times a \times a = 3 \times 3 \times 3 \times 3 = 81$. Quite a difference, isn't there?

Try this problem now,

 $10 \times 10 \times 10$ in exponential form is:

(a)	1000	Turn	to	page	15
(b)	10 ³	Turn	to	page	18

(c) 3 x 10 Turn to page 21



(1/10)³ is correct!

Now for a very important question.

Does
$$(1/10)^3 = \frac{1}{10}3$$
?

(a)	Yes	Turn to page	12
(b)	No	Turn to page	14

;



Okay, let's continue with this question.





Come now! $7 \times 7 \times 7 \times 7 \neq 47$. In fact, 7×7 is 49 and that is larger than 47 without multiplying by the other seven's.

Go to page 7 and make a better choice this next time.

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Whoops!

$$(1/10)^3 = 1/10 \times 1/10 \times 1/10 = 1/1000.$$

$$\frac{1}{10^3} = \frac{1}{10 \times 10 \times 10} = 1/1000.$$

Thus,
$$(1/10)^3 \frac{1}{100} \frac{1}{10} \frac{1}{10}$$
,

Turn to page 12 and continue.



While 1000 is equal to $10 \times 10 \times 10$, it is <u>not</u> the exponential form of $10 \times 10 \times 10$.

Return to page 10 and make a more appropriate selection.

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You seem to be having trouble multiplying fractions.

Go to Unit 6 and review the concepts presented there. Then, upon completion, return to page 1 of this Unit.

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 $\frac{1}{10}$ 3 is correct.

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Now for a very important question.

Does
$$\frac{1}{10}3 = (1/10)^3$$
?
(a) Yes Turn to page 12
(b) No Turn to page 14

Correct!

Continue with this problem.

Write x^4 in expanded form.

- (a) 4x Turn to page 21
- (b) (x)(x)(x)(x) Turn to page 8

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Ocops! You forgot the definition of an exponent.

Return to page 1 and begin again.



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 $(1/5)^4$ is correct.

Now go to page 8 and continue.



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No! Wrong answer!

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Return to page 1 and begin this Unit again. Read the material carefully before choosing an answer.



You are doing fine! Let's continue.

In some problems we will see a negative exponent, i.e., 3^{-2} . The minus sign in front of the exponent indicates that we want the reciprocal of the given number. For example, 3^{-2} means the <u>RECIPROCAL</u> of 3^{2} .

What is the reciprocal of 3^2 ? It is $\frac{1}{3}^2$. (Note: If this idea gives you trouble, you should go work Unit 17 on Reciprocals before continuing.)

Now answer this question.

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Which of the following answers is correct for x^{-3} ?

(a)	x ³	Turn to page 28
(b)	<u>1</u> 3x	Turn to page 31
(c)	$\frac{1}{(x)(x)(x)}$	Turn to page 26

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Okay! 1/9 is correct!

Work this problem.

$$(1/x)(1/x)(1/x) = ?$$

(a)	1/3x	Turn to page	21
(b)	3(1/x)	Turn to page	19
(c)	$\frac{1}{x^3}$	Turn to page	22



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Incorrect.

 10^{-4} means you want the <u>RECIPROCAL</u> of 10^{4} which is $\frac{1}{10^{4}}$.

Which answer below is equal to 5^{-1} ?

(a)	1/5	Turn	to	page	36

- (b) 5 Turn to page 35
- (c) -5 Turn to page 33



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No!
$$\frac{1}{6}4 = (1/6)^4 = 1/6 \times 1/6 \times 1/6 \times 1/6 = 1/1296.$$

What does $\frac{1}{3}^2$ equal?

(a)	1/9	Turn	to	page	23
(b)	1/6	Turn	to	page	27
(c)	2/3	Turn	to	page	19

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Very good!

Continue with this question.

Which answer below is equal to 10^{-4} ?

(a)	$\frac{1}{10}4$	Turn	to	page	29
(b)	1/40	Turn	to	page	24

(c) 10 x 10 x 10 x 10 Turn to page 32

Wait a minute!

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1.4

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$$\frac{1}{3}^2$$
 means $(1/3)^2$ or $1/3 \times 1/3$.

Now, what is $1/3 \times 1/3$?

(a)	1/6	Turn	to	page	16
(b)	1/9	Turn	to	page	23
(c)	2/3	Turn	to	page	21

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No!

 x^{-3} is the <u>reciprocal</u> of x^3 .

What answer below is correct for 10^{-3} ?

(a)	1/30	Turn	to	page	33
(b)	$\frac{1}{10^3}$	Turn	to	page	30
(-)	-3	-			• •





Excellent! Keep up the good work.

There is one more type of exponent that needs to be explained. This is when the exponent is zero. ANYTHING to the zero power is <u>1</u>. For example, $a^{0} = 1$, $10^{0} = 1$, $(25 \times 13 \times bc)^{0} = 1$, etc.

Maybe the entire sequence of exponents will fall into place if we look at the numbers from 10^3 to 10^{-3} .

Thus, 10^3 , 10^2 , 10^1 , 10^0 , 10^{-1} , 10^{-2} , 10^{-3} written without exponents are 1000, 100, 10, 1, 1, 1/10, 1/100, 1/1000.

Now, what does 3^0 equal?

- (a) 0 Turn to page 43
- (b) 1 Turn to page 41
- (c) 3 Turn to page 39

That's correct!

Which answer below is equivalent to x^{-1} ?

- (a) x Turn to page 35
- (b) -1x Turn to page 33
- (c) 1/x Turn to page 26


No!

 x^{-3} is the <u>reciprocal</u> of x^{3} .

What answer below is correct for $10^{\sim3}$?

(a)	1/30	Turn to page	33
(b)	$\frac{1}{10^3}$	Turn to page	30

(c) 10^3 Turn to page 35

•



Incorrect.

 10^{-4} means you want the <u>RECIPROCAL</u> of 10^4 which is $\frac{1}{10^4}$.

Which answer below is equal to 5^{-1} ?

٠.

(a)	1/5	Turn	to	page	36
(b)	5	Turn	to	page	35
(c)	-5	Turn	to	page	33

W. J. C.



Your answer is incorrect.

Are you having trouble with reciprocals?

What is the <u>reciprocal</u> of 5^3 ?

- (a) 125 Turn to page 34
- (b) 1/125 Turn to page 30



Incorrect.

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ERIC. Aruit such Provident by EBIC In order to give you a better understanding of reciprocals, go to Unit 17 and work through that unit. Then return to page 22 of this unit.

Your answer is incorrect.

Are you having trouble with reciprocals?

What is the <u>reciprocal</u> of 5^3 ?

- (a) 125 Turn to page 34
- (b) 1/125 Turn to page 30



1

Your answer is correct.

Try this problem.

1/8 is equal to which of the following? (Be careful
now.)

(a)	$\frac{1}{2}$ -3	Turn to page	38
(b)	4 -2	Turn to page	37
(c)	2 ⁻³	Turn to page	29



0 ops! $4^2 = 16$, not 8.

Return to page 36 and make a better choice next time.

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Your answer is incorrect.

Just keep in mind that the minus sign in front of the exponent denotes a RECIPROCAL. Hence $\frac{1}{2}$ -3 equals the RECIPROCAL of $(1/2)^3$ or 8.

Now, 1/2 is equal to which answer below?

(a)	2-1	Turn	to	page	36
(b)	2 ¹	Turn	to	page	33



ÑO !

Any number raised to the ZERO power is 1.

What does a⁰ equal?

(a)	a	Turn	to	page	42
(b)	1	Turn	to	page	45



No!

Anything to the \underline{ZERO} power is 1.

Return to page 44 and try again.



Very good! Any number of quantity to the zero power is 1.

Work this one now.

10x⁰ equals:

(a)	10	Turn	to	page	48
(b)	10 x	Turn	to	page	46
(c)	1	Turn	ΰ0	page	44

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That zero exponent is giving you trouble. It isn't that hard.

Return to page 29 and begin this section again. Take your time and read the material carefully before selecting your answers.

Turn to page 29.

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No!

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Any number raised to the ZERO power is 1.

What does a⁰ equal?

(a)	a	Turn	to	page	42
(b)	1	Turn	to	page	45



Oops!

 $10x^0$ means 10 times x^0 . Now $x^0 = 1$, so $10x^0 = 10(x^0) = 10(1) = 10$.

What does $(5x)^0$ equal?

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(a)	5	Turn to page 49
(b)	5x	Turn to page 40
(c)	1	Turn to page 47

1 is correct!

What does (3a)⁰ equal?

(a)	3	Turn	to	page	42
(b)	3a	Turn	to	page	39
(c)	1	Turn	to	page	41





0ops!

 $10x^0$ means 10 times x^0 . Now, $x^0 = 1$, so $10x^0 = 10(x^0) = 10(1) = 10$.

What does $(5x)^0$ equal?

(a)	5	Turn	to	page	49
(Ь)	5x	Turn	to	page	40
(c)	1	Turn	to	рәде	47





Fine! 1 is correct.

What does $5x^0$ equal?

a)	5	Turn	to	page	48
b)	1	Turn	to	rage	50



Very good! Your answer is correct.

What does 2⁴ equal?

(a)	16	Turn	to	page	53
(b)	8	Turn	to	page	55



Your answer is incorrect.

 $(5x)^0$ means that the quantity 5x is raised to the zero power.

What does $(10x^2)^0$ equal?

(a)	10	Turn	to	page	42
(5)	1	Turn	to	page	47
(c)	10x ²	Turn	to	page	39

.



Whoops!

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ERIC[®] Pull back Provided by ESIC $5x^0$ means 5 times x^0 .

Now, what is 5 times x^{0} ?

(a)	5x	Turn	to	page	43
(b)	0	Turn	to	page	39
(c)	1	Turn	to	page	42
(d)	5	Turn	to	page	48



Which of the following is equal to 16?

(a)	2 ⁸	Turn to page	54
(b)	4 ²	Turn to page	53
(c)	8 ²	Turn to page	56



Your answer is wrong.

The minus sign in front of the exponent indicates a RECIPROCAL. Remember? Therefore, 3^{-3} is the reciprocal of 3^{3} .

The reciprocal of 3^3 is:

(a)	1/27	Turn	to	page	57
(b)	1/9	Turn	to	page	59



Correct!

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ERIC Arul Exc Provided by Effic What does 3^{-3} equal?

(a)	27	Turn to page 52
(b)	1/9	Turn to page 58
(c)	1/27	Turn to page 60

Y.

Oops! You forgot the definition of an exponent.

Return to page 1 and begin again.

.

Incorrect!

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 $2^4 = 2 \times 2 \times 2 \times 2$, which is 16.

What does 3⁴ equal?

a)	81	Turn	to	page	51	
b)	12	Turn	to	page	54	
(c)	64	Turn	to	page	56	

No! No! No! .

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An exponent indicates repeated multiplication. Ex. mples: 4^3 means $4 \times 4 \times 4$, $2^4 = 2 \times 2 \times 2 \times 2$, etc.

Now return to page 55 and work the problem on that page.

Gkay!

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Now, what does 3⁻³ equal?

(a)	1/9	Turn to page 59
(b)	1/27	Turn to page 60
(c)	27	Turn to page 33

Your answer is wrong.

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The minus sign in front of the exponent indicates a RECIPROCAL. Remember? Therefore, 3^{-3} is the reciprocal of 3^{3} .

The reciprocal of 3^3 is:

(a)	1/27	Turn to page	57
(b)	1/9	Turn to page	59

Wait a minute!

2 2 1

The reciprocal of 3^3 is $\frac{1}{3}3$ which is equal to $\frac{1}{3 \times 3 \times 3}$ or 1/27.

What is the reciprocal of 5^3 ?

(a)	125	Turn	to	page	34
(b)	1/15	Turn	to	page	56
(c)	1/125	Turn	to	page	57

In order to understand how numbers can be written in different bases, we must know how the numbers we use can be expressed in terms of exponents and what these numbers really mean.

Consider the number 314. It is really the sum of 300 + 10 + 4. We write it as 314 to save time, paper, and work. We could and sometimes should write 314 in tabular form like:

hundreds	tens	units
3	1	4

which shows us that we have 3 hundreds, one ten, and 4 units. In order to show this relationship, we sometimes write in EXPANDED EXPONENTIAL FORM as follows:

314 = 300 + 10 + 4= 3 x 100 + 1 x 10 + 4 x 1 = 3 x 10² + 1 x 10¹ + 4 x 10⁰ 3 x 10² + 1 x 10¹ + 4 x 10⁰ is 314 in <u>expanded</u> <u>exponential form</u>.

Turn to page 61 ·

Write 1523 in expanded exponential form:

(a) 1000 + 500 + 20 + 3Turn to page 65 (b) $1 \times 1000 + 5 \times 100 + 2 \times 10 + 3 \times 1$ Turn to page 68 (c) $1 \times 10^{3} + 5 \times 10^{2} + 2 \times 10^{1} + 3 \times 10^{0}$ Turn to page 70

Incorrect!

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Expanded exponential form requires that our expanded form be equal to the number from which it came. For example, $4 \times 10^4 + 5 \times 10^3 + 7 \times 10^2 + 2 \times 10^1 + 8 \times 10^0 = 40000 + 5000 + 70 + 20 + 8 = 45,728.$

Keeping this example in mind, which of the following is true?

(a)
$$4020 = 5 \times 10^{3} + 0 \times 10^{2} + 2 \times 10^{0}$$

Turn to page 71
(b) $1030 = 1 \times 10^{3} + 0 \times 10^{2} + 3 \times 10^{1} + 0 \times 10^{0}$
Turn to page 67
(c) $2003 = 2 \times 10^{1} + 3 \times 10^{0}$
Turn to page 80
(d) $305 = 3 \times 10^{2} + 5 \times 10^{0}$
Turn to page 70

See.

That's correct!

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Now write 2003 in expanded exponential form.

(a) $2 \times 10^{1} + 3 \times 10^{0}$ Turn to page 80 (b) $2 \times 10^{3} + 0 \times 10^{2} + 0 \times 10^{1} + 3 \times 10^{0}$ Turn to page 75 (c) 2000 + 3 Turn to page 65



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Correct!

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If 10,010 = $1 \times 2^4 + 1 \times 2^1$, then 10,010 is written in base:

(a)	2	Turn	to	page	73	
(b)	10	Turn	to	page	85	

Incorrect.

While expanded exponential form is writing our number as a sum of multiples of 10, it is still not in its correct form until we have the multiples of 10 written in EXPONENTIAL form. For example, $100 = 1 \times 10^2$ $3000 = 3 \times 1000 = 3 \times 10^3$ $2 = 2 \times 1 = 2 \times 10^0$ $25 = 20 + 5 = 2 \times 10 + 5 \times 1 = 2 \times 10^1 + 5 \times 10^0$

Now, which is in expanded exponential form?

(a) 300 + 50 + 2 Turn to page 71 (b) $3 \times 100 + 5 \times 10 + 2 \times 1$ Turn to page 72 (c) $3 \times 10^2 + 5 \times 10^1 + 2 \times 10^0$ Turn to page 63

No, no, no!

 5×10^7 means 5 times 10 to the seventh power.

Therefore, the EXPONENT is 7 and shows us that the base number is:

(a)	10	Turn	to	page	64
(b)	5	Turn	to	page	78


Correct!

2,003 written in expanded exponential form is:

(a) $2 \times 10^3 + 3 \times 10^0$ Turn to page 75 (b) $2 \times 10^3 + 0 \times 10^2 + 1 \times 10^1 + 3 \times 10^0$ Turn to page 62 (c) $2 \times 200 + 2$

(c) 2,000 + 3 Turn to page 65





While it is correct to write 1523 as $1 \times 1000 + 5 \times 100 + 2 \times 10 + 3 \times 1$, it still is not in expanded exponential form. You should know this since there are no exponents on any of the numbers.

Which of the following is in expanded exponential form?

(a) $3 \times 100 + 4 \times 10 + 6 \times 1$ Turn to page 72 (b) $3 \times 10^2 + 4 \times 10^1 + 6 \times 10^0$ Turn to page 63

Incorrect.

The <u>subscript</u> tells you what base you are using.

Return to page 82 and make a different selection.



That's correct!

ERIC Pattect Provided by ENC Now write 2003 in expanded exponential form.

(a) $2 \times 10^{1} + 3 \times 10^{0}$ Turn to page 80 (b) $2 \times 10^{3} + 0 \times 10^{2} + 0 \times 10^{1} + 3 \times 10^{0}$ Turn to page 75 (c) 2000 + 3 Turn to page 65

- 1 +2

Incorrect.

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Return to page 60 and continue from there.



Wrong choice.

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ERIC.

A number like $3 \times 1000 + 2 \times 100 + 4 \times 10 + 3 \times 1$ is <u>NOT</u> in exponential form. The reason is obvious. 1000, 100, 10, and 1 are not written as 10 to some exponent.

Be more careful and try this problem.

Which of the following is written in expanded exponential form?

(a) $4 \times 10^3 + 3 \times 10^1$ Turn to page 63 (b) 4000 + 30 Turn to page 71 (c) $4 \times 1000 + 0 \times 100 + 3 \times 10 + 0 \times 1$ Turn to page 65

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Correct!

Let's continue.

The number $1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0$ is written in Base:

(a)	10	Turn	to	page	85	
(b)	5	Turn	to	page	77	
(c)	2	Turn	to	page	82	



Incorrect.

The problem is in Base 10 if <u>NO</u> subscript is written. This is because we use base 10 the most, and it is too much trouble to write the subscript every time.

Return to page 79 and make another choice.



Very good! $2 \times 10^3 + 0 \times 10^2 + 0 \times 10^1 + 3 \times 10^0$ is correct.

We hope you have noticed that the number which has the exponent determines the place or the column in which the number belongs. Thus $2 \times 10^5 + 0 \times 10^2 +$ $0 \times 10^1 + 3 \times 10^0$ is

10 ³	10 ²	10 ¹	10 ⁰
2	0	0	3

or as we usually write it, 2003.

This number with the exponent is called the <u>Base</u> of the number. So far, the numbers we have been using have been to the Base 10.

Turn to page 76

If we had a number written in the expanded exponential form of $4 \times 5^2 + 3 \times 5^1 + 1 \times 5^0$, it would be written in Base:

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(a)	5	Turn	to	page	73
(b)	10	Turn	to	page	78
(c)	2	Turn	to	page	81
(d)	4	Turn	to	page	85



What??????

Where did the 5 come from?

Return to page 73 and make a different selection.

fatat.



Incorrect.

The number with the exponent is the base number.

 $3 \times 4^3 \div 2 \times 4^1 = 3020$ in Base:

(a)	2	Turn	to	page	85
(b)	3	Turn	to	page	81
(c)	4	Turn	to	page	64



That's correct!

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ERIC FullTaxt Provided by ERIC What base is 532 written in?

(a)	5	Turn	to	page	74
(b)	2	Turn	to	page	88
(c)	10	Turn	to	page	90

N. S. Mark

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0ops!

 $2 \times 10^{1} + 3 \times 10^{0} = 20 + 3 = 23$. You were supposed to write 2003 in exponential form, not 23.

What number is $4 \times 10^4 + 9 \times 10^2 + 5 \times 10^1 + 2 \times 10^0$ equal to?

(a)	4952	Turn to page 62
(b)	40,952	Turn to page 67
(c)	4,090,502	Turn to page 83

Wrong choice.

The base number is the number with the exponent on it, when written in expanded exponential form.

The number $5 \times 10^7 + 3 \times 10^5 + 2 \times 10^1$ is written in base:

(a)	5	Turn	to	page	66
(b)	10	Turn	to	page	64



Very good! Your answer was correct.

To show that numbers are written to different cases, a number (called a subscript) is written in the lower right hand corner by the number. For example, 3201₅ means that 3201 is written to the base 5 and is designated by the subscript 5. (Note: If no subscript is shown, then the number is written in base 10.)

 $10,101_2$ means that 10,101 is written in base:

(a)	1	Turn	to	page	69
(b)	2	Turn	to	page	79
(c)	10	Turn	to	page	84

Oops!

endersteel same

Much too big a number.

Return to page 80 and make a better choice.



Incorrect.

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The <u>subscript</u> tells you what base you are using. Return to page 82 and make a different selection.

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Wrong choice.

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The base number is the number with the exponent on it, when written in expanded exponential form.

The number $5 \times 10^7 + 3 \times 10^5 + 2 \times 10^1$ is written in base:

(a)	5	Turn	to	page	66
(b)	10	Turn	to	page	64



That's correct!

Write 4032_5 in expanded exponential form.

(a)
$$4 \times 10^{3} + 0 \times 10^{2} + 3 \times 10^{1} + 2 \times 10^{0}$$

Turn to page 89
(b) $4 \times 2^{3} + 0 \times 2^{2} + 3 \times 2^{1} + 2 \times 2^{0}$
Turn to page 91
(c) $4 \times 5^{2} + 3 \times 5^{1} + 2 \times 5^{0}$
Turn to page 94
(d) $4 \times 5^{3} + 0 \times 5^{2} + 3 \times 5^{1} + 2 \times 5^{0}$
Turn to page 97

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No!

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Our problem is in base 2. Let's be more careful when we read and work these.

Return to page 94 and work the problem there.



Incorrect.

The problem is in Base 10 if \underline{NO} subscript is written. This is because we use base 10 the most, and it is too much trouble to write the subscript every time.

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Return to page 79 and make another choice.



Incorrect.

Full Text Provided by ERIC

The subscript of 5 indicates that we are working in base 5. Therefore, the number with the exponent on it should be a 5.

Return to page 86 and work that problem again.

Your answer is correct!

Now write $1,101_2$ in expanded exponential form.

- (a) $1 \times 10^3 + 1 \times 10^2 + 1 \times 10^0$ Turn to page 95
- (b) 1000 + 100 + 1 Turn to page 92
- (c) $1 \times 2^3 + 1 \times 2^2 + 1 \times 2^0$ Turn to page 86

Incorrect.

The subscript of 5 indicates that we are working in base 5. Therefore, the number with the exponent on it should be a 5.

Return to page 86 and work that problem again.



No!

1,101₂ is in base 2, not base 10.

Return to page 90 and try again.

ERIC."

Wrong choice.

 $10,101_2$ is written in expanded exponential form as $1 \times 2^4 + 0 + 1 \times 2^2 + 0 + 1 \times 2^0$ or 16 + 0 + 4 + 0 + 1 or 21.

Try this one.

 $20,120_3$ is the number _____ in base 10.

(a) 22	Turn	to	page	106
--------	------	----	------	-----

- (b) 1,285 Turn to page 109
- (c) 96 Turn to page 112



Your answer is incorrect.

The exponent on the 5 tells you what column the coefficient belongs. Thus, $4,032_5$ is written in tabular form like this:

or like this: $4 \times 5^3 + 0 \times 5^2 + 3 \times 5^1 + 2 \times 5^0$.

Now write $10,101_2$ in expanded exponential form.

(a)
$$1 \times 10^{4} + 0 \times 10^{3} + 1 \times 10^{2} + 0 \times 10^{1} + 1 \times 10^{0}$$

Turn to page 87
(b) $1 \times 2^{4} + 0 \times 2^{3} + 1 \times 2^{2} + 0 \times 2^{1} + 1 \times 2^{0}$
Turn to page 96
(c) $1 \times 5^{4} + 0 \times 5^{3} + 1 \times 5^{2} + 0 \times 5^{1} + 1 \times 5^{0}$
Turn to page 98
(d) $1 \times 2^{3} + 0 + 1 \times 2^{2} + 0 + 1 \times 2$
Turn to page 100

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No!

1,101₂ is in base 2, not base 10.

Return to page 90 and try again.



That is correct! Let's continue.

Since most of our work is done in base 10, we often wish to convert from other bases to base 10. Let's look at an example to see how it's done.

10,111₂ is a number written to base 2. Written in expanded exponential form, it is $1 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$. We now evaluate each term and add them up.

				t	oti	al		23	Therefore, 10,111 ₂ = 23.
1	X	2 ⁰	=	1	•	1	2	<u> </u>	
1	X	21	3	1	•	2	9 1	2	
1	x	2 ²	2	1	٠	Ą	ij	4	
0	x	2 ³	=	Û		3	2	0	
1	X	2 ⁴	2	1	٠	16	2	16	

Let's see if you can convert $10,101_2$ to base 10.

(a)	21	Turn	tc	page	9 9
(b)	11	Turn	to	page	93
(c)	3	Turn	to	page	101

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That is correct! Let's continue.

Since most of our work is done in base 10, we often wish to convert from other bases to base 10. Let's look at an example to see how it's done.

10,111₂ is a number written to base 2. Written in expanded exponential form, it is $1 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$. We now evaluate each term and add them up.

1	X	2 ⁴	=	1	•	16	=	16										
0	x	2 ³		0	•	8	Ŧ	0										
1	x	2 ²	=	1	٠	4	=	4										
1	x	2 ¹	=	1	•	2	=	2										
1	x	2 ⁰	=	1	•	1	=	1										
				t	ht:	~ 1		23	Th	oro [.]	fore	.	10).1	11_	Ŧ	2	3.

Let's see if you can convert $10,101_2$ to base 10.

(a)	21	Turn	to	page	99
(b)	11	Turn	to	page	93
(c)	3	Turn	to	page	101

No!

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Our problem is in base 2. Let's be more careful when we read and work these.

Return to page 94 and work the problem there.



Okay, 21 was correct!

Write $4,321_5$ in base 10.

(a)	81	Turn	to	page	103
(b)	586	Turn	to	page	105
(c)	211	Turn	to	page	108

1



Incorrect.

10,101₂ is written in tabular form as:

	24	2 ³	2 ²	2 ¹	2 ⁰		Th	e				
	1	0	1	0	1	٠	inus,	in expanded				
exp	onent	ial fo	rm we	have 1	x 2 ⁴ +	0	x 2 ³ +	1 x 2 ² +				
0 >	(2 ¹ +	1 x 2	0, or	simply	1 x 2 ⁴	+	1×2^2	+ 1 x 2 ⁰ .				

Now write $10,010_2$ in expanded exponential form.

(a)
$$1 \times 2^4 + 1 \times 2$$
 Turn to page 86
(b) $1 \times 2^1 + 0 + 0 + 1 \times 2^0 + 0$ Turn to page 104
(c) $1 \times 10^4 + 0 + 0 + 1 \times 10^1 + 0$ Turn to page 98





Wrong choice.

10,101₂ is written in expanded exponential form as $1 \times 2^{4} + 0 + 1 \times 2^{2} + 0 + 1 \times 2^{0}$ or 16 + 0 + 4 + 0 + 1 or 21.

Try this one.

Full Fast Provided by ERIC

 $20,120_3$ is the number _____ in base 10.

- (a) 22 Turn to page 106
- (b) 1,285 Turn to page 109
- (c) 96 Turn to page 112

Your answer is incorrect.

,

The first thing we must do before we can convert to base 10 is to write our problem in expanded exponential form.

6327 written in this form is:

- (a) $7 \times 6^2 + 7 \times 3^1 + 7 \times 2^0$ Turn to page 118 (b) $6 \times 7^2 + 3 \times 7^1 + 2 \times 7^0$ Turn to page 107
Sorry, wrong answer.

$$4,321_{5} = \frac{5^{3}}{4} \frac{5^{2}}{3} \frac{5^{1}}{2} \frac{5^{1}}{5^{0}}$$
$$= 4 \times 5^{3} \text{ or } 500$$
$$3 \times 5^{2} \text{ or } 75$$
$$2 \times 5^{1} \text{ or } 10$$
$$1 \times 5^{0} \text{ or } 1$$

586

Try this one: 6327

total

(a)	317	Turn	to	page	113
(b)	32	Turn	to	page	111
(c)	572	Turn	to	page	102



That's incorrect.

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an in a formation of the second s

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ERIC-Palline for the set Be <u>careful</u> of those <u>exponents</u>.

Rework the problem on page 100.

Very good!

Nork this one.

 $2,012_3$ is the number _____ in base 10.

a) 21	Turn	to	page	11	4
a) 21	Turn	to	page	11	(

- (b) 59 Turn to page 115
- (c) 23 Turn to page 117



Incorrect.

ALC: NO.

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We are working with base 3. You can tell by the subscript, remember?

Return to page 93 and try again.



That's correct!

Now let's turn to page 108 and finish the problem by converting 632_7 to base 10.



Sorry, wrong answer.

$$4,321_{5} = \frac{5^{3}}{4} \frac{5^{2}}{3} \frac{5^{2}}{2} \frac{5^{1}}{1} \frac{5^{0}}{5^{0}}$$
$$= 4 \times 5^{3} \text{ or } 500$$
$$3 \times 5^{2} \text{ or } 75$$
$$2 \times 5^{1} \text{ or } 10$$
$$1 \times 5^{0} \text{ or } 1$$
$$= 1$$

Try this one: 6327

(a)	317	Turn to page 113
(b)	32	Turn to page 111
(c)	572	Turn to page 102



Incorrect.

5

We are working with base 3. You can tell by the subscript, remember?

Return to page 93 and try again.

Incorrect.

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ERIC. Ataliate Provided by Edit The subscript of 5 indicates that we are working in base 5. Therefore, the number with the exponent on it should be a 5.

Return to page 86 and work that problem again.

No!

We are in base 7. Return to page 103 and try again.



96 is the correct answer!

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Now write $4,321_5$ in base 10.

(a)	81	Turn	to	page	103	
(b)	586	Turn	to	page	105	
(c)	211	Turn	to	page	301	

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₩a ſ

317 is the correct answer!

COLUMN TO A

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ERIC Avelant provided to ERIC Now work this one.

2,010₅ is the number _____ in base 10.

(a) 18	Turn	to	page	110
--------	------	----	------	-----

- (b) 1275 Turn to page 116
- (c) 255 Turn to page 105

Your answer is incorrect.

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ERIC."

Return to page 97 and begin this last section again.

Very good! You have completed this Unit. Let's review what we have learned.

- You have learned how to work with integral exponents.
- You have learned how to write numbers to different bases in expanded exponential form.
- 3. You have learned how to convert numbers in different bases to base 10.

You are now ready for a test over this Unit. Go tell your teacher you have finished.



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What??? How did you get that answer?

Work the problem on page 113 again.



Your answer is incorrect.

ERIC."

Return to page 97 and begin this last section again.

;

Incorrect.

The <u>subscript</u> tells you what base you are using. Return to page 102 and work the problem again.



NORTHWEST REGIONAL EDUCATIONAL LABORATORY 400 Lindsay Building - 710 S.W. Second Avenue Portland, Oregon 97204

CAL MATHEMATICS

TEST QUESTIONS

UNIT 20 - CONCEPTS OF NUMBER BASES

- 1. Write 723 in expanded exponential form
 - (a) 700 + 20 + 3
 - (b) $7 \times 100 + 2 \times 10 + 3$
 - (c) $7 \times 10^2 + 2 \times 10^1 + 3 \times 10^0$

2. The number 1011₂ equals _____ in base 10.

- (a) 1011
- (b) 11
- (c) 6

3. Write 11101₂ in expanded exponential form.

(a) $1 \times 10^4 + 1 \times 10^3 + 1 \times 10^2 + 0 \times 10^1 + 1 \times 10^0$ (b) 29 (c) $1 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0$

4. $10^{0} =$

.

- (a) l
- (b) 10
- (c) 0

5. Does $4020 = 5 \times 10^3 + 0 \times 10^2 + 2 \times 10^0$?

- (a) 1.0
- (b) No
- . Write 1001 in expanded expensional form.
 - (a) 🕂 + i
 - (5) . i + 1 (c) $\times 10^3 + 1 \times 10^0$

7. $421_5 =$ ______ base 10 (a) 111 (b) 421 (c) 37 Which of the following is in expanded exponential form? 8. 3000 + 400 + 20 + 5(a) (b) $3 \times 1000 + 4 \times 100 + 2 \times 10 + 5$ (c) $3 \times 10^3 + 4 \times 10^2 + 2 \times 10^1 + 5 \times 10^0$ 100011₂ = _____ base 10 9. 111 (a) (b) 67 100011 (c) Write 25 in expanded exponential form 10. $2 \times 10^{1} + 5 \times 10^{0}$ (a) 20 + 5 (b) (c) 11001_2 Write 101010_2 in expanded exponential form. 11. (a) $2^5 + 2^3 + 2^1$ $1 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0$ (b) (b) 42 111₅ = _____ base 10 12. (a) 16 111 (b) (c) 31 Is 101112 in expanded exponential form? 13. (a) Yes (b) No

a barren and and

14. $3 \times 5^2 + 2 \times 5^1 + 4 \times 5^0 =$ (a) 324 (b) 324₅ $(c) 324_2$ 15. The number $1 \ge 2^4 + 0 \ge 2^3 + 0 \ge 2^2 + 1 \ge 2^1 + 1 \ge 2^0$ is written in base _____. (a) 10 (b) 4 (c) 2 Write 3061 in expanded exponential form. 16. (a) $3 \times 10^3 + 6 \times 10 + 1$ (b) $3 \times 10^2 + 6 \times 10^1 + 1 \times 10^0$ (c) 3000 + 60 + 117. 10010₂ written in expanded exponential form = (a) 10000 + 10(b) $1 \times 10^4 + 0 \times 10^3 + 0 \times 10^2 + 1 \times 10^1 + 0 \times 10^0$ (c) $1 \times 2^4 + 1 \times 2^1$ 18. $111_2 = _$ in base 10. (a) 111 (b) 7 (c) 16 19. $3 \times 7^3 + 2 \times 7^1 + 1 \times 7^0 = 3021$ in base _____. (a) 7 (b) 10 'c) 3 What base is 421 written in? 20. (a) 4 () 10 (c) 2

ERIC.

- 21. $224_5 = ----- base 10$
 - (a) 244
 - (b) 10
 - (c) 74

22. What number is $1 \ge 2^5 + 1 \ge 2^3 + 1 \ge 2$ equal to

- (a) 1011_2
- (b) 101010
- (c) 101010₂

23. 11101₂ means that 11101 is written in base

- (a) 5
- (b) 2
- (c) **1**0

24. 215 = _____10

- (a) 11
- (b) 7
- (c) 21

25. 110013₂ written in expanded exponential form is:

(a) $1 \times 2^{5} + 1 \times 2^{4} + 0 \times 2^{3} + 0 \times 2^{2} + 1 \times 2^{1} - 1 \times 2^{0}$ (b) $1 \times 10^{5} + 1 \times 10^{4} + 0 \times 10^{3} + 0 \times 10^{2} + 1 \times 10^{1} + 1 \times 10^{0}$ (c) $1 \times 2^{4} + 1 \times 2^{3} + 1 \times 2^{1} + 1 \times 2^{0}$



Answer Sheet - Unit 20

Concepts of Number Bases

(3)

1.	с	2	
2.	b	4	
3.	с	3	
4.	а	1	
5.	Ъ	2	
6.	с	<u>ດ</u>	
7.	а	4	
8.	с	1	
9.	b	4	
10.	а	2	
11.	а	3	
12.	с	4	
13.	b	3	
14.	b	1	
15.	с	1	
16.	а	2	
17.	с	3	,
18.	b	4	•
19.	а	1	•
20.	b	1	•
21.	с	4	ŀ
22.	с	I	L
23.	ይ	1	L
24.	`a		3
25.	а		3

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Jark Acht

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