



[www.wj-et.eu](http://www.wj-et.eu)

## Research trends in dynamic geometry software: A content analysis from 2005 to 2021

Rabia Nur Öndeş\*, Department of Mathematics Education, Ataturk University, Erzurum, Turkey,

<https://orcid.org/0000-0002-9787-4382>

### Suggested Citation:

Ondes, R. N. (2021). Research trends in dynamic geometry software: A content analysis from 2005 to 2021. *World Journal on Educational Technology: Current Issues*. 13(2), 236-260.  
<https://doi.org/10.18844/wjet.v13i2.5695>

Received from December 12, 2020; revised from February 15, 2021; accepted from April 10, 2021;  
Selection and peer review under responsibility of Prof. Dr. Servet Bayram, Yeditepe University, Turkey.  
©2021 United World Center of Research Innovation and Publication. All rights reserved.

### Abstract

Dynamic geometry software (DGS), especially GeoGebra, have been used in mathematics lessons around the world since it enables a dynamic learning environment. To date, there exist so many published researches about DGS, which leads to the need for meaningful organisation. This study aims to give a broad picture about researches related to DGS. For this reason, 210 articles accessed from the Web of Science database were analysed in terms of their purpose, research design, sample level, sample size, data collection tools and data analysing methods by using the content analysis method. According to the findings, for each section the most frequently used ones were as follows: 'the effect of DGS on something' as a purpose, qualitative method as a research design, high school students as a sample level, 101–300 intervals as a sample size, documents and achievement tests as instruments and descriptive analysis for quantitative and qualitative studies. These results can help researchers to see the past trends in DGS and conduct new studies.

Keywords: Dynamic geometry software, DGS, GeoGebra, content analysis, mathematics education

\* ADDRESS OF CORRESPONDENCE: Rabia Nur Öndeş, Department of Mathematics Education, Ataturk University, Erzurum, Turkey,

Email Address: [ondeseme@gmail.com](mailto:ondeseme@gmail.com)

## 1. Introduction

The usage of technology in both teaching and learning mathematics is increasing. Since multiple representations in mathematics have an important role in understanding concepts more effectively, the physical models or concrete manipulatives were transformed to computers in order to make their access easy. So, students and teachers from all around the world can reach these manipulatives and make practice more than by using limited number of models. Besides, computerised physical models give teachers the opportunity to integrate them in their lessons to create a more effective learning environment for their students (Bouck & Flanagan, 2009; Van de Walle et al., 2007). However, the need for constructing more specific models with respect to their own lesson subject or mathematical problems has come to light, which leads them to use dynamic geometry software (DGS) programmes in classrooms. DGS programmes enable us to make constructions by using simple tools and moving them by dragging points or slides (Young, 2017). Thus, teachers can use their own constructions in their lessons to conceptualise problems and to show different examples with the help of its dynamic features. Moreover, dynamic geometry software programmes enable students to visualise concepts, build relationships, discover patterns, generalise them, make geometrical proofs and develop their skills like problem-solving and creative thinking (Acikgul, 2017; Chan, 2014; Samur, 2015).

Considering the significance of DGS with its contributions to education, GeoGebra is the most popular one among the others, like Cabri 3D, Geometer's Sketchpad and Geometric Supporter, because GeoGebra is an open source software and it includes a combination of arithmetic, geometry, algebra and calculus systems. Also, it enables us to connect other users from all over the world, access others' materials and download available files (Hohenwarter & Fuchs, 2004). As a result, so many studies, theses and researches involve GeoGebra as the most commonly used DGS in mathematics education (Akyuz, 2016). For example, there are some studies that look at the effects of using GeoGebra on students' success, their mathematics attitudes (Arbain & Shukor, 2015; Saha et al., 2010) or their skills like problems-solving (Jacinto & Carreira, 2017; Koyuncu et al., 2015; Murni et al., 2017) and some studies also provide an example of how to use GeoGebra in teaching specific subjects in mathematics (Breda & Santos, 2016; Fonseca & Franchi, 2016; Nobre et al., 2016; Poon, 2018; Takaci et al., 2015). This means that there are studies on GeoGebra in the literature conducted by different methods, samples and procedures. Therefore, due to the mass of published works on DGS, there is a need to organise them in a meaningful way. Similarly, in the field of mathematics education and technology-supported mathematics education, there are some studies that have examined articles available in various databases with different time intervals and categories (Baki et al., 2011; Ciltas et al., 2010; Chan, 2014; Tatar et al., 2014; Ulutas & Ubuz, 2008; Young, 2017).

Baki et al. (2011) analysed 284 graduate theses in the field of mathematics education between the years 1998 and 2007 retrieved from online databases of the Higher Education Council and Proquest and the library of each university. According to the results of this study, teaching mathematics as a research topic, experimental design as a research design, questionnaires and achievement tests as data collection tools and 6th, 7th and 8th grade students as participants are the most preferable ones.

In mathematics education, the study conducted by Ulutas and Ubuz (2008) analysed 129 articles between the years 2000 and 2006. These articles were published in *Eurasian Journal of Educational Research*, *Hacettepe University Journal of Education*, *Elementary Education Online* and *Education and Science Journal*. The analyses indicate that most studies have samples of the education faculties of universities in the Central Anatolia Region and members are elementary students or preservice

teachers. In addition to these, the most common research designs are experimental and quantitative in nature using tests and questionnaires; the most common research topics are numbers and geometry topics and their cognitive-affective domains.

Ciltas et al. (2010) analysed 359 articles related to mathematics education in the years from 1987 to 2009. These articles were obtained from 32 different journals, which were national (27) and indexed in Web of Science [Social Sciences Citation Index (SSCI)] (5). The results of the study state that most of the studies used quantitative research as the research design, learning activities, studies as research topic and frequency as the data analysis method. Also, more than one data collection instrument was used in most studies.

For technology-enhanced mathematics instruction, Young (2017) conducted a second-order meta-analysis of 19 researches that were obtained from the databases of ERIC, PsycINFO, ProQuest Dissertations and Theses Full-text and Academic Search Complete between the years 1985 and 2015. The aim of the study was to determine the cumulative effects of technology on student achievement with a summary of 30 years of research. As a conclusion, this study provides that technology-enhanced instruction has a moderate cumulative effect on student achievement. Also, it concluded that technology component and study quality are important contributors effecting size variation.

In addition to the content analyses on mathematics education, Tatar et al. (2014) conducted a study to analyse 105 graduate theses about technology-supported mathematics education in Turkey. According to the study, mathematics education among the categories of mathematics, mathematics education and technology as keywords, algebra as a subject, computer as a technology device and 6th, 7th and 8th grade students as a sample were used more frequently in the studies. Also, most of the studies preferred to use the mixed research methods, quantitative and qualitative studies, respectively. The most commonly used data collection instrument is achievement tests; the most commonly used data analyses methods are mean/standard deviation for quantitative data and descriptive analysis for qualitative data. Furthermore, it was indicated that experimental groups who had technology-supported education have higher scores in achievement, attitude towards mathematics, interest in mathematics, motivation for mathematics and retention of learning.

Chan (2014) analysed nine eligible articles on DGS-based instruction from 587 studies from 2001 to 2013 by using the databases of ERIC, JSTOR, ProQuest, PsycINFO and SwetsWise. The purpose of this meta-analysis was to determine the effects of DGS-based instruction on students' mathematics achievement in K-12 education as regards the traditional pencil-and-ruler instruction. So, the results of the study demonstrate that DGS-based instruction has a positive and large affect ( $d = +1.02$ ) on mathematics achievement.

Joung and Byun (2021) analysed 23 digital mathematics games used in mathematics education in terms of NCTM (National Council of Teachers of Mathematics) content and process standards, which could help teachers to choose the appropriate games for their lessons. In this study, the number of puzzle games is more than the other types, which are categorised as action, strategy and others. Also, it was found that most of the games are related to the number and operations among the contents of number and operations, algebra, geometry and measurement and data analysis and probability. The most frequently used process standards to least the ones are stated, respectively, as problem-solving, connection, reasoning proof and representation.

As seen from these studies, researches should be analysed and arranged regularly in order to lead researchers to see the big picture in a specific area. Trends in a specific area can be determined by analysing the contents of the studies. So, by considering the contributions of identified trends, future researches can be developed. In this research, the content analysis method was used to analyse the studies on DGS published in Web of Science and indexes such as Social Science Citation Index (SSCI), Science Citation Index Expanded (SCI) and Emerging Sources Citation Index (ESCI). Therefore, the aim of the study is to determine the trends in DGS, especially in mathematics education. The research questions addressed by this study are as follows:

1. Which research purposes are included in the articles until 2018?
2. Which research designs have been used in the articles until 2018?
3. With which samples have been studied in the articles until 2018?
4. With which sample sizes have been studied in the articles until 2018?
5. Which data collection tools have been used in the articles until 2018?
6. Which data analysing methods have been used in the articles until 2018?

## **2. Methods**

### *2.1. Research design*

*Content analysis is defined as ‘a systematic, replicable technique for compressing many words of text into fewer content categories based on explicit rules of coding’ (Stemler, 2000). In this study, this method was used to analyse the articles related to DGS accessed from the Web of Science database. Since the aim of the research is to identify the trends in studies regarding DGS, it is appropriate to use this method which enables to classify data by specific themes and concepts (Frankel et al., 2012). Thus, the systematically organised and categorised data can help the reader to understand the evaluations and interpretations about the trends in this specific area (Gay et al., 2012).*

### *2.2. Sample*

*The population of the study includes DGS articles that were published in the journals and indexed in Web of Science. The reason why this database was chosen is because it includes qualitative journals in academics and it has enough related journals for content analysis. So, the population was restricted to this database. From this population, the sample was selected by using the convenience sampling method since it allows using already available sample based on a specific interest and characteristic features of the study (Frankel et al., 2012). As a result, 210 English articles about DGS published in more than 50 different journals in the indexes of SSCI, SCI and ESCI from 2005 to mid-2021 were accessed for a sample of this research. The keywords ‘GeoGebra’ and ‘dynamic geometry software’ were used. The names of the articles analysed are presented in Appendix 1.*

### *2.3. Data collection tools*

*In this study, the modified type of the combination of two forms, which are the Educational Technology Publication Classification Form developed by Goktas et al. (2012) and the Paper Classification Form (PCF) developed by Sozbilir et al. (2012), were used as data collection tools. In order to categorise the contents of the articles, the original version of these forms was changed with respect to the purpose of this study. At the end of the adaptation process of the forms, the modified version was used for the present study. This form consists of seven components, which are (1) identification, (2) the purpose of the paper, (3) research design/methods, (4) sample level, (5) sample size, (6) data collection tools and (7) data analysis methods used in the papers. For the purpose of the paper, categories were*

*created according to the articles considered after reading each of them. Therefore, in addition to the identification of the formal structure of the articles in terms of research design, data collection tools, sampling and sample size and data analysis methods, the purpose of DGS was added as a component in the modified version of the form in order to examine the articles in a more contextual way.*

#### 2.4. Data analyzes

In the context of the study, data gathered by the content analysis method of the articles were analysed by using descriptive statistics. With the help of the Excel programme, data frequencies and percentage tables were formed and the results were presented as graphics for each research question.

### 3. Results

*The findings obtained through the analysis of the articles related to DGS indexed by SSCI, SCI and ESCI in the Web of Science database are presented under six sections. The sections parallel to the research questions are as follows: purposes, research design, sample level, sample size, data collection tools and data analysing methods. Under each section, the findings are represented by tables or/and figures.*

#### 3.1. Purposes

The studies identified are classified under four main categories: ‘the effect of DGS’, ‘the usage of DGS’, ‘technical development of DGS’ and ‘others’.

- *The effect of DGS* refers to the studies that examine the effect of DGS on different outcomes. In this sense, the studies emphasise participants’ achievement in mathematics or learning a specific mathematical concept with the help of DGS or understanding the mathematical concepts by using it; these have been categorised as the effect of DGS on achievement /learning/understanding. The studies with regard to the impact of DGS on participants’ skills like connection and problem-solving have been analysed under the effect of DGS on skills in terms of their types. Also, the studies addressing the impact of DGS on participants’ views about something like DGS integration in lessons or their attitudes towards something like mathematics have been categorised as the effect of DGS on attitudes/views towards/about something. The studies considering the effect of DGS on participants’ cognitive processes and their competence on something like mathematics have been categorised under the effect of DGS on cognitive processes and the effect of DGS on competence.
- *Sample applications of DGS* refer to the studies using DGS for different purposes. The studies showing an example about how to use DGS for teaching specific concepts have been categorised as the sample applications of DGS for teaching the concept. Also, some studies demonstrating an example about how to make a construction of a specific concept in the DGS environment or how to visualise/illustrate the concept by using DGS have been categorised as the sample applications of DGS for constructing/visualising/illustrating a specific concept.
- *Technical development of DGS* refers to the studies about improving a tool/programme in DGS or technical features.
- *Others* refer to the studies not sorted by these categories and not having common features.

Table 1 indicates the distribution of the articles’ purposes based on the classification regarding these categories. Figure 1 shows the distribution of categories as proportions. In Figure 1, it can be seen that ‘the effect of DGS’ consists of 58.8% of the identified studies and ‘the usage of DGS’ consists of 30.8% of them, ‘technical development of DGS’ consists of 6.6% of them and ‘others’ consists of 3.8% of them.

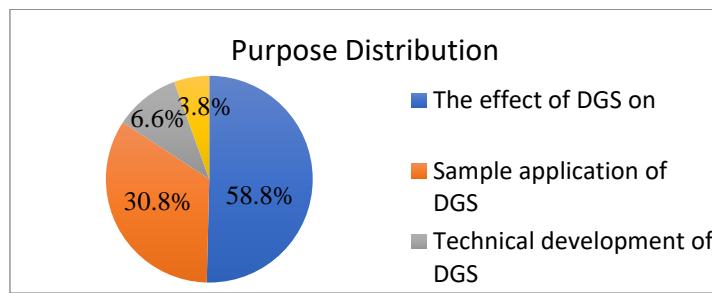


Figure 1. Distribution of the articles on DGS according to their purposes

In Table 1, it can be seen that the majority of researches are about the effect of DGS on achievement/learning/understanding ( $f = 54$ ) among the categories under the effect of DGS. However, the effect of DGS' cognitive processes ( $f = 10$ ) is the least preferred purpose outcome among them. Also, spatial/visualisation skills ( $f = 8$ ), reasoning/argumentation skills ( $f = 8$ ) and teaching skills of technology-integrated lessons ( $f = 8$ ) are used in the studies examined more than the other skills. Besides, constructing/visualising/illustrating the concept ( $f = 47$ ) is more frequently used rather than teaching the concept ( $f = 28$ ) in the sample application of DGS.

Table 1. Distribution of the articles on DGS according to their purposes

| Themes                    | Categories  | Sub-categories | <i>f</i> |
|---------------------------|---|----------------|----------|
| The effect of DGS         | Achievement/learning/understanding                    |                | 54       |
|                           | Spatial/visualisation skills                          |                | 8        |
|                           | Reasoning/argumentation skills                        |                | 8        |
|                           | Teaching skills of technology-integrated lessons      |                | 8        |
|                           | Problem-solving skills                                |                | 7        |
|                           | Connection skills                                     |                | 5        |
|                           | Proofing skills                                       |                | 4        |
|                           | Questioning skills                                    |                | 3        |
|                           | Creativity skills                                     |                | 2        |
|                           | Communication skills                                  |                | 1        |
|                           | Advanced mathematical thinking                        |                | 5        |
|                           | Geometric cognitive growth                            |                | 5        |
| Cognitive processes       |   |                |          |
| Attitudes /views          | Integration DGS                                       |                | 9        |
|                           | Using DGS   |                | 8        |
| Competence                | Mathematics   |                | 3        |
|                           | Mathematical competence                               |                | 5        |
|                           | Mathematics self-efficacy                             |                | 4        |
|                           | Computer self-efficacy                                |                | 2        |
| Motivation                |   |                | 2        |
| Sample application of DGS | For constructing/visualising/illustrating the concept |                | 47       |
|                           | For teaching the concept                              |                | 28       |

|                              |     |
|------------------------------|-----|
| Technical development of DGS | 16  |
| Others                       | 9   |
| Total                        | 243 |

### 3.2. Research design

The research designs used in the examined articles are given in Table 2. Also, Figure 2 shows the distribution of the research designs in terms of qualitative, quantitative and mixed methods. So, it can be said that the most preferred method is qualitative method (60.3%) among them.

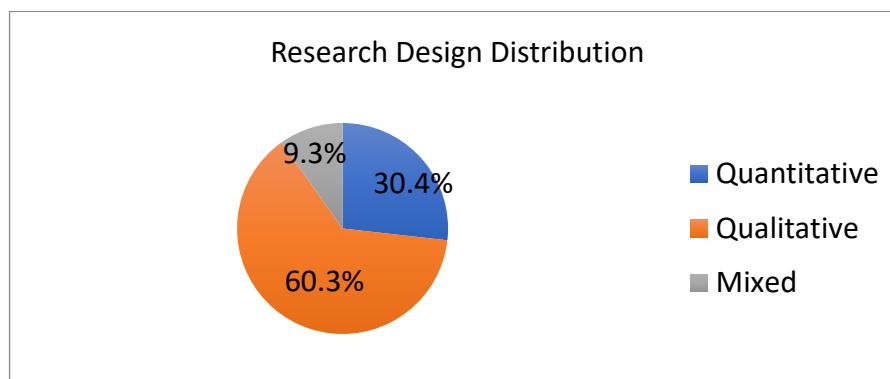


Figure 2. Distribution of the articles on DGS according to their research designs

In Table 2, it can be seen that the quasi-experiment (47) is the most preferred design among the quantitative methods; the case study (56) and the concept analysis (43) are the most preferred designs among the qualitative methods; and embedded design (9) is the most preferred among the mixed methods. Also, it can be seen that the non-experimental designs [descriptive (2), comparison (2) and correlation (2)] are not used in studies as much as the experimental designs [weak (7), true (2) and quasi (47) experiments].

Table 2. Distribution of the articles on DGS according to their research designs

| Research design |                  |                       | Frequency |
|-----------------|------------------|-----------------------|-----------|
| Quantitative    | Experimental     | Quasi-experimental    | 47        |
|                 |                  | Weak experimental     | 7         |
|                 |                  | True experimental     | 2         |
|                 | Non-experimental | Descriptive           | 2         |
|                 |                  | Comparison            | 2         |
|                 |                  | Correlation           | 2         |
| Qualitative     | Interactive      | Case study            | 56        |
|                 |                  | Design-based research | 6         |
|                 |                  | Action research       | 3         |
|                 | Non-interactive  | Phenomenology         | 2         |
|                 |                  | Grounded theory       | 2         |
|                 |                  | Concept Analysis      | 43        |

|       |               |                      |     |
|-------|---------------|----------------------|-----|
|       |               | Review/meta-analysis | 11  |
| Mixed | Embedded      |                      | 9   |
|       | Exploratory   |                      | 6   |
|       | Explanatory   |                      | 2   |
|       | Triangulation |                      | 2   |
| Total |               |                      | 204 |

### 3.3. Sample level

The frequencies and percentages of sample levels used in the identified studies are given Table 3 and its demonstration with a pie chart is shown in Figure 3. It can be seen that the most frequently used sample level is high school students ( $f = 38, 24.8\%$ ). This is followed by the pre-service mathematics teachers ( $f = 37, 24.2\%$ ), other university students ( $f = 26, 17\%$ ), middle school students ( $f = 21, 13.7\%$ ) and mathematics teachers ( $f = 19, 12.4\%$ ). In addition to these, master/PhD students ( $f = 6, 3.9\%$ ), elementary school students ( $f = 6, 2.6\%$ ) and others ( $f = 2, 1.3\%$ ) are the least frequently used samples in the studies.

Table 3. Distribution of the articles on DGS according to their sample level

| Sample level                            | Frequency<br><i>f</i> | Percentages |
|---|-----------------------|-------------|
|   |                       | %           |
| High school students (9–12)             | 38                    | 24.8        |
| Pre-service mathematics teachers        | 37                    | 24.2        |
| Other university students               | 26                    | 17.0        |
| Middle school students (6–8)            | 21                    | 13.7        |
| Mathematics teachers                    | 19                    | 12.4        |
| Master/PhD students                     | 6                     | 3.9         |
| Elementary school students (1–5)        | 4                     | 2.6         |
| Others/researcher/trainer/mathematician | 2                     | 1.3         |
| Total                                   | 153                   | 100         |

### 3.4. Sample size

The sample sizes used in the studies are classified into intervals according to the PCF selected. Table 4 shows the frequencies and percentages of the sample size intervals used. Thus, it can be seen that the majority of the studies preferred to use 101–300 intervals ( $f=44, 32.6\%$ ) as a sample size. After this, 11–30 intervals ( $f = 31, 23\%$ ), 31–1000 intervals ( $f = 31, 23\%$ ) and 1–10 intervals ( $f = 25, 18.5\%$ ) were mostly used ones. Also, the table and figure show that the studies using greater than 300 participants are not common [301–1000 interval ( $f = 3, 2.2\%$ ), greater than 1000 ( $f = 1, 0.7\%$ )].

Table 4. Distribution of the articles on DGS according to their sample sizes

| Sample size       | Frequency<br><i>f</i> | Percentage |
|-------------------|-----------------------|------------|
|                   |                       | %          |
| 1–10 interval     | 25                    | 18.5       |
| 11–30 interval    | 31                    | 23.0       |
| 31–100 interval   | 31                    | 23.0       |
| 101–300 interval  | 44                    | 32.6       |
| 301–1000 interval | 3                     | 2.2        |
| Greater than 1000 | 1                     | 0.7        |
| Total             | 135                   | 100        |

### 3.5. Data collection tools

The frequencies and percentages of the data collection tools used in the studies examined are shown in Figure 3 as a graphical distribution. So, it can be seen that the most preferred tools are documents ( $f = 63, 22.4\%$ ) and achievement tests ( $f = 63, 22.4\%$ ), which are followed by observations ( $f = 57, 20.2\%$ ), interviews ( $f = 47, 16.7\%$ ), questionnaires ( $f = 37, 13.2\%$ ) and other tests ( $f = 14, 5\%$ ).



Figure 3. Distribution of the articles on DGS according to their data collection tools

From Table 5, revealing the data collection tools in more detail, it can be seen that studies preferred to use Likert type (10%) more than open-ended (3.2%) questionnaires; multiple choice (14.2%) more than open ended (8.2%) in achievement test; semi-structured (14.2%) more than structured (2.5%) in interviews; with participant (16.4%) more than focus group (2.1%) and without participant (1.8%) in observations.

Table 5. Distribution of the articles on DGS according to their data collection tools

| Data collection tools |                     | Frequency | Percentage |
|-----------------------|---------------------|-----------|------------|
|                       |                     | <i>f</i>  | %          |
| Questionnaire         | Open-ended          | 9         | 3.2        |
|                       | Likert              | 28        | 10.0       |
| Achievement test      | Open-ended          | 23        | 8.2        |
|                       | Multiple choice     | 40        | 14.2       |
| Other tests           | Attitude test       | 3         | 1.1        |
|                       | Skill test          | 8         | 2.8        |
|                       | Self-efficacy test  | 3         | 1.1        |
| Interview             | Structured          | 7         | 2.5        |
|                       | Semi-structured     | 40        | 14.2       |
| Observation           | Focus group         | 6         | 2.1        |
|                       | With participant    | 46        | 16.4       |
|                       | Without participant | 5         | 1.8        |
| Documents             |                     | 63        | 22.4       |
| Total                 |                     | 281       | 100        |

### 3.6. Data analysing methods

Table 6 demonstrates the frequencies and percentages of the data analysing methods used in the studies identified. As can be seen, descriptive analysis (23.5%), *t*-test (11.6%) and analysis of variance (ANOVA)/analysis of covariance (ANCOVA) (7.1%) from inferential statistics are the most frequently used methods in quantitative studies. Besides, the usage of the descriptive analysis (22.3%) is more than the usage of the content analysis (13.2%) and document analysis (12.6%) in qualitative studies.

Table 6. Distribution of the articles on DGS according to their data analyzing methods

| Data analysing method |             |  | Frequency<br><i>f</i> | Percentage<br>% |
|-----------------------|-------------|--|-----------------------|-----------------|
| Quantitative          | Descriptive | Frequency/Percentage   | 32                    | 10.3            |
|                       |             | Mean/SD  | 41                    | 13.2            |
|                       |             | <i>t</i> -test   | 36                    | 11.6            |
|                       |             | ANOVA/ANCOVA   | 22                    | 7.1             |
|                       |             | Correlation  | 4                     | 1.3             |
|                       |             | Multivariate analysis of variance /Multivariate analysis of covariance | 6                     | 2.0             |
|                       |             | Factor analyse   | 2                     | 0.6             |
|                       |             | Regression   | 1                     | 0.3             |
|                       |             | Non-parametric tests   | 17                    | 5.5             |
|                       | Qualitative | Descriptive Analysis   | 69                    | 22.3            |
|                       |             | Content analysis   | 41                    | 13.2            |
|                       |             | Document analysis  | 39                    | 12.6            |
| Total                 |             |  | 310                   | 100             |

## 4. Discussion and conclusion

In this study, it has been aimed to examine the trends in researches on Dynamic Geometry Software, especially on GeoGebra. So, 210 articles with regard to this subject matter accessed from Web of Science and indexed in SSCI, SCI and ESCI were analysed.

The first research question of the present study is regarding the identification of the research purposes in the examined studies. At the end of the content analysis, the findings indicate that observing 'the effect of DGS on something' is the most preferred purpose and its effect on achievement/learning/understanding is most frequently used among others. This may result from the fact that by the increasing the popularity of DGS, the uncertainty of the DGS effect on learning mathematical concepts and the curiosity, whether it aroused students success on mathematics, lead researchers to test, observe and analyse its effects on achievement (Young, 2017). In addition, the reason why 'the usage of DGS' is the second category including the majority of studies may be that its integration to lessons have become a problem among educators and teachers, leading them to give some construction and lesson examples.

The second research question of the present study is about the examination of the distribution of the research designs used in the identified articles. The results indicating that the most preferred method is qualitative method (60.3%) among them contradicted the results of other studies. The results of the studies conducted by Baki et al. (2011) and Ulutas et al. (2008) show that the most common design in the mathematics education is the experimental design. Also, Ciltas et al. (2010) report that the quantitative design is the most frequently used design in mathematics education. Furthermore, according to the results of Tatar et al.'s (2014) study, the mixed method is the most common in the technology-supported mathematics education. This contradiction may result from the lack of technological pedagogical content knowledge about the usage of DGS on teaching mathematical concepts as a material, since the present study shows that the concept analysis and case study are the most frequently used designs. How to make constructions of some mathematical concepts by using DGS and to teach concepts by using it may lead the studies to use qualitative methods to show some examples and sample instructions. On the other hand, it was observed that experimental study was used more than the non-experimental design among the quantitative studies in the present study. So, this result is parallel to the studies addressing the experimental design as the most common method (Baki et al., 2011; Ulutas & Ubuz, 2008). It can be concluded that the tendency to observe the effect of DGS on something (achievement, skills etc.) may result in using control and experimental groups in the studies with the experimental design.

According to the third research question relating to the examination of the sample level distribution, the results indicate that high school students, pre-service mathematics teachers and other university students are the most frequently used samples in the studies identified. This may result from the convenient sampling which enables researchers to use their own students (pre-service math teachers and other undergraduate students). Also, the reason for using the high school students mostly may be related to the nature of DGS and mathematics. Calculus and middle school mathematics curriculum objectives may be more appropriate to use DGS than others, and also the high school students can learn DGS easier than elementary school students. Like the results of the present study, other studies in mathematics education commonly prefer to use middle-grade students as a sample (Baki et al., 2011; Tatar et al., 2014). Moreover, Ulutas and Ubuz (2008) state that the most frequently used participants are pre-service teachers or elementary students. At this point, although this study supports the results of the present study for pre-service teachers, it contradicts the present study's findings which indicate that the elementary students are among the least frequently used samples. Thus, it can be suggested that elementary students can be preferred as much as university and middle-grade students.

Based on the findings of the present study related to the fourth question, 101–300 intervals is the most common among them as a sample size. These findings support the results of the studies conducted by Ciltas et al. (2010) and Tatar et al. (2014). Besides, this may be a result of the fact that the experimental studies, especially quasi-experimental design, require mostly two groups with more than 30 to compare them in some specific dimension.

The fifth question is related to the exploration of the distribution of the data collection tools used in examined studies. As the findings indicated, documents and achievement tests are the most preferred instruments. With regard to achievement test, this result can be supported by the result of Tatar et al.'s (2014) study in which achievement test was found to be the most common tool. Moreover, other studies conducted by Baki et al. (2011), Ciltas et al. (2010) and Ulutaş and Ubuz (2008) determined that the achievement test and questionnaires are the most frequently used instruments in mathematics education. The reason of using achievement tests frequently may be the measurement desire since

experimental studies mostly require monitoring participants' progress or comparing groups in terms of learning and understanding. Moreover, in this present study, the reason why documents were found to be one of the common instruments may be the fact that textbooks used as concepts analysis, students' writings, their reflection papers, their responses on tasks and their videos were considered as documents in qualitative studies, which forms approximately two-thirds of the all studies.

As the last question investigates the trends of the data analysing methods used in examined studies, the findings indicate that for quantitative studies, the descriptive analysis and *t*-test are used; for qualitative studies, document, descriptive and content analysis are the most frequently used analyses. These results support the findings of other studies claiming that the frequency (Ciltas et al., 2010) and mean/standard deviation are the most frequently used analyses for quantitative data and descriptive analysis for qualitative data (Tatar et al., 2014). Furthermore, it can be said that concept analysis and case study designs in qualitative studies may cause an increase in the number of documents, descriptive and content analyses used. Also, it can be concluded that experimental studies may result in the increase in number of descriptive analyses and *t*-tests used.

To sum up, it can be concluded that since DGS have been introduced in mathematics education, the researches mostly have started to show how to construct mathematical concepts/models in a DGS environment and how to integrate them in mathematics courses pedagogically. Also, researches have been conducted to test the effects of DGS on participants in terms of achievement, skills, competence, attitudes and cognitive processes, and also these researches were mostly carried out using qualitative designs with high school students and pre-service mathematics teachers.

## 5. Suggestions

- The mixed methods can be preferred more for DGS researches in the future.
- Elementary students and master/PhD students can be preferred as much as others.
- The investigation of DGS effect on something like achievement and skills separately should consider using the whole effect of DGS by using multiple data collection instruments.
- Additionally, the comparison of the experiment and control groups with/without DGS and the researches about the different teaching methods with DGS can be considered.
- Technological and pedagogical content knowledge level and integration of DGS to lesson can be studied more in the mathematics education field.

## References

- Acikgul, K. (2017). *Geogebra destekli mikro ogretim uygulamasi ve oyunlastirilmis TPAB etkinliklerinin ilkogretim matematik ogretmen adaylarinin TPAB duzeylerine etkisi* (Doktora Tezi). YOK Ulusal Tez Merkezi.
- Akyuz, D. (2016). Fakli ogretim yontemleri ve sinif seviyelerine gore ogretmen adaylarinin TPAB analizi. *Turk Bilgisayar ve Matematik Egitimi Dergisi*, 7(1), 89–111.
- Arbain, N., & Shukor, N. A. (2015). The effects of GeoGebra on students achievement. *Procedia Social and Behavioral Sciences*, 172, 208–214.
- Baki, A., Guven, B., Karatas, I., Akkan, Y., & Cakiroglu, U. (2011). Trends in Turkish mathematics education research: from 1998 to 2007. *Hacettepe Universitesi Egitim Fakultesi Dergisi (H. U. Journal of Education)*, 40, 57–68.

Ondes, R. N. (2021). Research trends in dynamic geometry software: A content analysis from 2005 to 2021. *World Journal on Educational Technology: Current Issues*, 13(2), 236–260. <https://doi.org/10.18844/wjet.v13i2.5695>

- Bouck, E., & Flanagan, S. M. (2009). Virtual manipulatives: what they are and how teachers can use them. *Sage Journals*, 45, 3.
- Breda, A. M. D., & Santos, J. M. D. (2016). Complex functions with GeoGebra. *Teaching Mathematics and its Applications*, 35, 102–110.
- Chan, K. K. (2014). Dynamic geometry software improves mathematical achievement: systematic review and meta-analysis. *Journal of Educational Computing Research*, 51(3), 311–325.
- Ciltas, A., Guler, G., & Sozbilir, M. (2010). Mathematics education research in Turkey: a content analysis study. *Educational Sciences: Theory & Practice*, 12(1), 574–578.
- Fraenkel, J. R., Wallen, N. E., & Hyun, H. H. (2012). *How to design & evaluate research in education* (8th ed.). McGraw Hill.
- Fonseca, D., & Franchi, R. (2016). Exploring the convergence of sequences in the embodied world using GeoGebra. *Teaching Mathematics and its Applications*, 35, 88–101.
- Gay, L. R., Mills, G. E., & Airasian, P. W. (2012). *Educational research: competencies for analysis and applications* (10th ed.). Pearson.
- Goktaş, Y., Kucuk, S., Aydemir, M., Telli, E., Arpacik, O., Yildirim, G., & Reisoglu, I. (2012). Educational technology research trends in Turkey: a content analysis of the 2000–2009 decade. *Educational Sciences: Theory & Practice*, 12(1), 177–199.
- Hohenwarter, M., & Fuchs, K. (2004). *Combination of dynamic geometry, algebra and calculus in the software system geogebra*. Computer algebra systems and dynamic geometry systems in mathematics teaching conference.
- Jacinto, H., & Carreira, S. (2017). Mathematical problem solving with technology: the techno-mathematical fluency of a student with GeoGebra. *International Journal of Science and Mathematics Education*, 15, 1115–1136.
- Joung, E., & Byun, J. (2021). Content analysis of digital mathematics games based on the NCTM content and process standards: an exploratory study. *School Science and Mathematics*, 121(3), 127–142. <https://doi.org/10.1111/ssm.12452>
- Koyuncu, I., Akyuz, D., & Cakiroglu, E. (2015). Investigating plane geometry problem-solving startegies of prospective mathematics teachers in technology and paper-pancel environments. *International Journal of Science and Mathematics Education*, 13, 837–862.
- Murni, V., Sariyasa, S., & Ardana, I. M. (2017). GeoGebra assist discovery learning model for problem solving ability and attitude toward mathematics. *Journal of Physics: Conference Series*, 895.
- Nobre, C. N., Meireles, R. G., Vieira-Junior, N., Resende, M. N., Costa, L. E., & Rocha, R. C. (2016). The use of GeoGebra software as a calculus teaching and learning tool. *Informatics in Education*, 15(2), 253–267.
- Poon, K. K. (2018). Learning fraction comparison by using a dynamic mathematics software-GeoGebra. *International Journal of Mathematical Education in Science and Technology*, 49 (3), 469–479.
- Saha, R. A., Ayub, A. F., & Tarmizi, R. A. (2010). The effects of GeoGebra on mathematics achievement: enlightening coordinate geometry learning. *Procedia Social and Behavioral Sciences*, 8, 686–693.
- Samur, H. (2015). *The effects of dynamic geometry use on eighth grade students' achievement in geometry and attitude towards geometry on triangle topic* (MS thesis). Middle East Technical University, Turkey.
- Sozbilir, M., Kutu, H., & Yasar, M. D. (2012). Science education research in Turkey: a content analysis of selected features of papers published. In J. Dillon & D. Jorde (Eds.), *The world of science education: handbook of research in Europe* (pp. 1–35). Sense publishers.
- Stemler, S. (2000). An overview of content analysis. *Practical Assessment, Research and Evaluation*, 7(1), 17.

- Takaci, D., Stankov, G., & Milanovic, I. (2015). Efficiency of learning environment using GeoGebra when calculus contents are learned in collaborative groups. *Computers and Education*, 82, 421–431.
- Tatar, E., Akkaya, A., & Kagizmanli, T. B. (2014). Trends in dissertations involving technology-assisted mathematics instruction: the case of Turkey. *Eurasia Journal of Mathematics, Science & Technology Education*, 10(6), 547–558.
- Ulutas, F., & Ubuz, B. (2008). Matematik eğitiminde arastirmalar ve egilimler: 2000 ile 2006. *Elementary Education Online*, 7(3), 614–626.
- Van de Walle, J. A., Karp, K. S., & Bay-Williams, J. M. (2007). *Elementary and middle school mathematics: teaching developmentally* (7th ed.). Pearson Education.
- Young, J. (2017). Technology-enhanced mathematics instruction: a second-order meta-analysis of 30 years of research. *Educational Research Review*, 22, 19–33. <https://doi.org/10.1016/j.edurev.2017.07.001>

#### Appendix-1

1. Abánades, M., Botana, F., Kovács, Z., Recio, T., & Sólyom-Gecse, C. (2016). Development of automatic reasoning tools in GeoGebra. *ACM Communications in Computer Algebra*, 50(3), 85-88.
2. Abdullah, A. H., Misrom, N. S., Kohar, U. H. A., Hamzah, M. H., Ashari, Z. M., Ali, D. F., ... & Abd Rahman, S. N. S. (2020). The effects of an inductive reasoning learning strategy assisted by the geogebra software on students' motivation for the functional graph II topic. *IEEE Access*, 8, 143848-143861. <https://doi.org/10.1109/ACCESS.2020.3014202>.
3. Abrahamson, D., & Abdu, R. (2020). Towards an ecological-dynamics design framework for embodied-interaction conceptual learning: the case of dynamic mathematics environments. *Educational Technology Research and Development*, 1-35. <https://doi.org/10.1007/s11423-020-09805-1>
4. Açıkgül, K. (2021). Mathematics teachers' opinions about a GeoGebra-supported learning kit for teaching polygons. *International Journal of Mathematical Education in Science and Technology*, 1-22. <https://doi.org/10.1080/0020739X.2021.1895339>
5. Açıkgül, K., & Aslaner, R. (2019). Effects of Geogebra supported micro teaching applications and technological pedagogical content knowledge (TPACK) game practices on the TPACK levels of prospective teachers. *Education and Information Technologies*, 1-25. <https://doi.org/10.1007/s10639-019-10044-y>
6. Adelabu, F. M., Makgato, M., & Ramaligela, M. S. (2019). The importance of dynamic geometry computer software on learners' performance in geometry. *Electronic Journal of E-Learning*, 17(1), 52-63.
7. Akkoç, H. (2015). Formative questioning in computer learning environments: a course for pre-service mathematics teachers. *International Journal of Mathematical Education in Science and Technology*, 46(8), 1096-1115. <https://doi.org/10.1080/0020739X.2015.1031835>
8. Alabdulaziz, M. S., Aldossary, S. M., Alyahya, S. A., & Althubiti, H. M. (2020). The effectiveness of the GeoGebra Programme in the development of academic achievement and survival of the learning impact of the mathematics among secondary stage students. *Education and Information Technologies*, 1-29. <https://doi.org/10.1007/s10639-020-10371-5>
9. Albaladejo, I. M. R., García, M. D. M., & Codina, A. (2015). Developing mathematical competencies in secondary students by introducing dynamic geometry systems in the classroom. *Egitim ve Bilim*, 40(177).
10. Albano, G., & Iacono, U. D. (2019). GeoGebra in e-learning environments: a possible integration in mathematics and beyond. *Journal of Ambient Intelligence and Humanized Computing*, 10(11), 4331-4343. <https://doi.org/10.1007/s12652-018-1111-x>
11. Albano, G., Iacono, U. D., & Fiorentino, G. (2016). An online Vygotskian learning activity model in mathematics. *Journal of e-Learning and Knowledge Society*, 12(3).

12. Alessio, F. G., Demeio, L., & Telloni, A. I. (2019). A formative path in tertiary education through geogebra supporting the students' learning assessment and awareness. *International Journal for Technology in Mathematics Education*, 26(4). [https://doi.org/10.1564/tm\\_e\\_v26.4.03](https://doi.org/10.1564/tm_e_v26.4.03)
13. Alqahtani, M. M., & Powell, A. B. (2016). Instrumental appropriation of a collaborative, dynamic-geometry environment and geometrical understanding. *International Journal of Education in Mathematics, Science and Technology*, 4(2), 72-83.
14. Andraphanova, N. V. (2015). Geometrical similarity transformations in dynamic geometry environment GEOGEBRA. *European Journal of Contemporary Education*, 12(2), 116-128. <https://10.13187/ejced.2015.12.116>
15. Atasoy, E., & Konyalıhatipoğlu, M. E. (2019). Dinamik geometri yazılımı kullanılan öğrenme ortamında öğrencilerin analitik ve bütüncül düşünme stillerinin incelenmesi. *Eğitim ve Bilim*, 44(199). <https://doi.org/10.15390/EB.2019.8003>
16. Attorps, I., Björk, K., & Radic, M. (2016). Generating the patterns of variation with GeoGebra: the case of polynomial approximations. *International Journal of Mathematical Education in Science and Technology*, 47(1), 45-57. <https://10.1080/0020739X.2015.1046961>
17. Avci, E. & Coşkuntuncel, O. (2019). Middle school teachers' opinions about using Vustat and Tinkerplots in the data processing in middle school mathematics. *Pegem Eğitim ve Öğretim Dergisi*, 9(1), 01-36. <https://doi.org/10.14527/pegegog.2019.001>
18. Avcu, S., & Çetinkaya, B. (2019). An instructional unit for prospective teachers' conceptualization of geometric transformations as functions. *International Journal of Mathematical Education in Science and Technology*, 1-30. <https://doi.org/10.1080/0020739X.2019.1699966>
19. Baccaglini-Frank, A. (2020). To tell a story, you need a protagonist: how dynamic interactive mediators can fulfill this role and foster explorative participation to mathematical discourse. *Educational Studies in Mathematics*, 1-22. <https://doi.org/10.1007/s10649-020-10009-w>
20. Baki, A., Kosa, T., & Guven, B. (2011). A comparative study of the effects of using dynamic geometry software and physical manipulatives on the spatial visualisation skills of pre-service mathematics teachers. *British Journal of Educational Technology*, 42(2), 291-310.
21. Bansilal, S. (2015). Exploring student teachers' perceptions of the influence of technology in learning and teaching mathematics. *South African Journal of Education*, 35(4).
22. Bayaga, A., Mthethwa, M. M., Bosse, M. J., & Williams, D. (2019). Impacts of implementing geogebra on eleventh grade student's learning of Euclidean Geometry. *South African Journal of Higher Education*. <http://dx.doi.org/10.20853/33-6-2824>
23. BeltrÁn-Meneu, M. J., Murillo-Arcila, M., & Albarracín, L. (2016). Emphasizing visualization and physical applications in the study of eigenvectors and eigenvalues. *Teaching Mathematics and its Applications: An International Journal of the IMA*, 36(3), 123-135.
24. Benzer, A. I., & Yıldız, B. (2019). The effect of computer-aided 3D modeling activities on pre-service teachers' spatial abilities and attitudes towards 3d modeling. *Journal of Baltic Science Education*, 18(3), 335.
25. Bergsten, C., & Kondratieva, M. (2021). Secondary school mathematics students exploring the connectedness of mathematics: The case of the parabola and its tangent in a dynamic geometry environment. *The Montana Mathematics Enthusiast*, 18(1-2), 183-209.
26. Bhagat, K. K., & Chang, C. Y. (2015). Incorporating GeoGebra into Geometry learning-A lesson from India. *Eurasia Journal of Mathematics, Science & Technology Education*, 11(1).
27. Bidaybekov, Y., Kamalova, G., Bostanov, B., & Salgozha, I. (2017). Development of Information Competency in Students during Training in Al-Farabi's Geometric Heritage within the Framework of Supplementary School Education. *European Journal of Contemporary Education*, 6(3), 479-496.
28. Birgin, O., & Acar, H. (2020). The effect of computer-supported collaborative learning using GeoGebra software on 11th grade students' mathematics achievement in exponential and logarithmic functions. *International Journal of Mathematical Education in Science and Technology*, 1-18. <https://doi.org/10.1080/0020739X.2020.1788186>

29. Birgin, O., Bozkurt, E., Gürel, R., & Duru, A. (2015). The effect of computer-assisted instruction on 7th grade students' achievement and attitudes toward mathematics: the case of the topic "vertical circular cylinder". *Croatian Journal of Education: Hrvatski časopis za odgoj i obrazovanje*, 17(3), 783-813.
30. Birgin, O., & Uzun Yazıcı, K. (2021). The effect of GeoGebra software-supported mathematics instruction on eighth-grade students' conceptual understanding and retention. *Journal of Computer Assisted Learning*. <https://doi.org/10.1111/jcal.12532>
31. Blažek, J., & Pech, P. (2019). Locus computation in dynamic geometry environment. *Mathematics in Computer Science*, 13(1), 31-40. <https://doi.org/10.1007/s11786-018-0355-3>
32. Blažek, J., & Pech, P. (2019). Synthetic proof with the support of dynamic geometry. *International Journal for Technology in Mathematics Education*, 26(3). [https://doi.org/10.1564/tme\\_v26.3.01](https://doi.org/10.1564/tme_v26.3.01)
33. Bokosmaty, S., Maviliđi, M. F., & Paas, F. (2017). Making versus observing manipulations of geometric properties of triangles to learn geometry using dynamic geometry software. *Computers & Education*, 113, 313-326.
34. Botana, F., & Abánades, M. A. (2014). Automatic deduction in (dynamic) geometry: Loci computation. *Computational Geometry*, 47(1), 75-89.
35. Botana, F., Hohenwarter, M., Janičić, P., Kovács, Z., Petrović, I., Recio, T., & Weitzhofer, S. (2015). Automated theorem proving in GeoGebra: Current achievements. *Journal of Automated Reasoning*, 55(1), 39-59.
36. Botana, F., & Kovács, Z. (2015). A Singular web service for geometric computations. *Annals of Mathematics and Artificial Intelligence*, 74(3-4), 359-370.
37. Botana, F., Kovács, Z., & Recio, T. (2020). A mechanical geometer. *Mathematics in Computer Science*, 1-11. <https://doi.org/10.1007/s11786-020-00497-7>
38. Botana, F., & Recio, T. (2016). On the unavoidable uncertainty of truth in dynamic geometry proving. *Mathematics in Computer Science*, 10(1), 5-25.
39. Botana, F., & Recio, T. (2016). Some issues on the automatic computation of plane envelopes in interactive environments. *Mathematics and Computers in Simulation*, 125, 115-125.
40. Botana, F., & Recio, T. (2017). Computing envelopes in dynamic geometry environments. *Annals of Mathematics and Artificial Intelligence*, 80(1), 3-20.
41. Botana, F., & Recio, T. (2019). A proposal for the automatic computation of envelopes of families of plane curves. *Journal of Systems Science and Complexity*, 32(1), 150-157. <https://doi.org/10.1007/s11424-019-8341-7>
42. Božić, R., Takači, Đ., & Stankov, G. (2019). Influence of dynamic software environment on students' achievement of learning functions with parameters. *Interactive Learning Environments*, 1-15. <https://doi.org/10.1080/10494820.2019.1602842>
43. Bozkurt, G., & Ruthven, K. (2017). Classroom-based professional expertise: A mathematics teacher's practice with technology. *Educational Studies in Mathematics*, 94(3), 309-328.
44. Breda, A. M. D. A., & Santos, J. M. D. S. D. (2016). Complex functions with GeoGebra. *Teaching Mathematics and its Applications: An International Journal of the IMA*, 35(2), 102-110.
45. Bulut, M., & Bulut, N. (2011). Pre service teachers' usage of dynamic mathematics software. *Turkish Online Journal of Educational Technology-TOJET*, 10(4), 294-299.
46. Caglayan, G. (2015). Making sense of eigenvalue-eigenvector relationships: math majors' linear algebra-geometry connections in a dynamic environment. *The Journal of Mathematical Behavior*, 40, 131-153.
47. Caglayan, G. (2015). Math majors' visual proofs in a dynamic environment: the case of limit of a function and the  $\epsilon$ - $\delta$  approach. *International Journal of Mathematical Education in Science and Technology*, 46(6), 797-823.
48. Caglayan, G. (2015). Pythagorean theorem with Hippocrates' lunes. *Spreadsheets in Education (eJSiE)*, 8(2), 5.
49. Caglayan, G. (2016). Mathematics teachers' visualization of complex number multiplication and the roots of unity in a dynamic geometry environment. *Computers in the Schools*, 33(3), 187-209.
50. Caglayan, G. (2016). Teaching ideas and activities for classroom: integrating technology into the pedagogy of integral calculus and the approximation of definite integrals. *International Journal of Mathematical Education in Science and Technology*, 47(8), 1261-1279.
51. Caglayan, G. (2018). Real analysis students' understanding of pointwise convergence of function sequences in a DGS assisted learning environment. *The Journal of Mathematical Behavior*, 49, 61-81.

52. Caglayan, G. (2019). Is it a subspace or not? Making sense of subspaces of vector spaces in a technology-assisted learning environment. *ZDM*, 51(7), 1215-1237. <https://doi.org/10.1007/s11858-019-01101-4>
53. Cetin, Y., Mirasyedioglu, S., & Cakiroglu, E. (2019). An inquiry into the underlying reasons for the impact of technology enhanced problem-based learning activities on students' attitudes and achievement. *Eurasian Journal of Educational Research*, 19(79), 191-208.
54. Chan, K. K., & Leung, S. W. (2014). Dynamic geometry software improves mathematical achievement: Systematic review and meta-analysis. *Journal of Educational Computing Research*, 51(3), 311-325.
55. Cheng, K., & Leung, A. (2015). A dynamic applet for the exploration of the concept of the limit of a sequence. *International Journal of Mathematical Education in Science and Technology*, 46(2), 187-204. <https://doi.org/10.1080/0020739X.2014.951007>
56. Chen, X. (2014). Representation and automated transformation of geometric statements. *Journal of Systems Science and Complexity*, 27(2), 382-412.
57. Chen, C. L., & Wu, C. C. (2020). Students' behavioral intention to use and achievements in ICT-Integrated mathematics remedial instruction: Case study of a calculus course. *Computers & Education*, 145, 103740. <https://doi.org/10.1016/j.compedu.2019.103740>
58. Çekmez, E. (2020). Establishing the link between the graph of a parametric curve and the derivatives of its component functions. *International Journal of Mathematical Education in Science and Technology*, 51(1), 115-130. <https://doi.org/10.1080/0020739X.2019.1663950>
59. da Silva, R. S. R., Barbosa, L. M., Borba, M. C., & Ferreira, A. L. A. (2021). The use of digital technology to estimate a value of pi: teachers' solutions on squaring the circle in a graduate course in Brazil. *ZDM-Mathematics Education*, 1-15. <https://doi.org/10.1007/s11858-021-01246>
60. Daher, W. M., & Anabousi, A. A. (2015). Students' recognition of function transformations' themes associated with the algebraic representation. *Journal of Research in Mathematics Education*, 4(2), 179-194.
61. de Moura Fonseca, D. S. S., & de Oliveira Lino Franchi, R. H. (2016). Exploring the convergence of sequences in the embodied world using GeoGebra. *Teaching Mathematics and its Applications: An International Journal of the IMA*, 35(2), 88-101.
62. del Cerro Velázquez, F., & Morales Méndez, G. (2021). Application in augmented reality for learning mathematical functions: a study for the development of spatial intelligence in secondary education students. *Mathematics*, 9(4), 369. <https://doi.org/10.3390/math9040369>
63. Dere, H. E., & Kalelioglu, F. (2020). The Effects of Using Web-Based 3D Design Environment on Spatial Visualisation and Mental Rotation Abilities of Secondary School Students. *Informatics in Education*, 19(3), 399-424. <https://doi.org/10.15388/infedu.2020.18>
64. Diković, L. (2009). Applications GeoGebra into teaching some topics of mathematics at the college level. *Computer Science and Information Systems*, 6(2), 191-203.
65. Di Paola, F., Pedone, P., Inzerillo, L., & Santagati, C. (2015). Anamorphic projection: analogical/digital algorithms. *Nexus network journal*, 17(1), 253-285.
66. Disbudak, O., & Akyuz, D. (2019). the comparative effects of concrete manipulates and dynamic software on the geometry achievement of fifth-grade students. *International Journal for Technology in Mathematics Education*, 26(1). [https://doi.org/10.1564/tme\\_v26.1.01](https://doi.org/10.1564/tme_v26.1.01)
67. Dogruer, S. S., & Akyuz, D. (2020). Mathematical practices of eighth graders about 3D shapes in an argumentation, technology, and design-based classroom environment. *International Journal of Science and Mathematics Education*, 18(8), 1485-1505. <https://doi.org/10.1007/s10763-019-10028-x>
68. Dvir, A., & Tabach, M. (2017). Learning extrema problems using a non-differential approach in a digital dynamic environment: the case of high-track yet low-achievers. *ZDM*, 49(5), 785-798.
69. Echeverría, L., Cobos, R., & Morales, M. (2019). Improving the students computational thinking skills with collaborative learning techniques. *IEEE Revista Iberoamericana de Tecnologias del Aprendizaje*, 14(4), 196-206.
70. Erkek, Ö., & Bostan, M. I. (2019). Prospective middle school mathematics teachers' global argumentation structures. *International Journal of Science and Mathematics Education*, 17(3), 613-633. <https://doi.org/10.1007/s10763-018-9884-0>
71. Erkoc, M. F., Gecu, Z., & Erkoc, C. (2013). The effects of using Google SketchUp on the mental rotation skills of eighth grade students. *Educational Sciences: Theory and Practice*, 13(2), 1285-1294.

72. Ferdiánová, V. (2017). GeoGebra materials for LMS moodle focused monge on projection. *Electronic Journal of e-Learning*, 15(3), 259-268.
73. Ferrarello, D., Mammana, M. F., & Taranto, E. (2019). Non-euclidean geometry with art by means of GeoGebra. *International Journal for Technology in Mathematics Education*, 26(3). [https://doi.org/10.1564/tme\\_v26.3.02](https://doi.org/10.1564/tme_v26.3.02)
74. Fiallo, J., & Gutiérrez, A. (2017). Analysis of the cognitive unity or rupture between conjecture and proof when learning to prove on a grade 10 trigonometry course. *Educational Studies in Mathematics*, 96(2), 145-167.
75. Flores, A., Bernhardt, S. A., & Shipman, H. L. (2015). Rowing competitions and perspective. *International Journal of Mathematical Education in Science and Technology*, 46(2), 284-291. <https://doi.org/10.1080/0020739X.2014.950708>
76. Forsythe, S. K. (2015). Dragging maintaining symmetry: can it generate the concept of inclusivity as well as a family of shapes?. *Research in Mathematics Education*, 17(3), 198-219.
77. Fung, C. H., & Poon, K. K. (2020). Can dynamic activities boost mathematics understanding and metacognition? A case study on the limit of rational functions. *International Journal of Mathematical Education in Science and Technology*, 1-15. <https://doi.org/10.1080/0020739X.2020.1749905>
78. Gainutdinova, T. Y., Denisova, M. Y., Smirnova, A. V., Shakirova, Z. F., & Shirokova, O. A. (2019). The use of dynamic geometry systems as a means of visual thinking activation for students who study mathematical analysis. // *OABJ*, 10, 1-5. <https://doi.org/10.33225/jbse/19.18.335>
79. Gergelitsová, Š., & Holan, T. (2016). GeoTest—A system for the automatic evaluation of geometry-based problems. *Computer Applications in Engineering Education*, 24(2), 297-304. <https://doi.org/10.1002/cae.21712>
80. Glassmeyer, D., Brakoniecki, A., & M. Amador, J. (2019). Promoting uncertainty to support preservice teachers' reasoning about the tangent relationship. *International Journal of Mathematical Education in Science and Technology*, 50(4), 527-556. <https://doi.org/10.1080/0020739X.2018.1527405>
81. Gómez-Chacón, I. M., Albaladejo, I. M. R., & López, M. D. M. G. (2016). Zig-zagging in geometrical reasoning in technological collaborative environments: a mathematical working space-framed study concerning cognition and affect. *ZDM*, 48(6), 909-924.
82. Gómez-Chacón, I. M., & Kuzniak, A. (2015). Spaces for geometric work: figural, instrumental, and discursive geneses of reasoning in a technological environment. *International Journal of Science and Mathematics Education*, 13(1), 201-226.
83. Granberg, C., & Olsson, J. (2015). ICT-supported problem solving and collaborative creative reasoning: Exploring linear functions using dynamic mathematics software. *The Journal of Mathematical Behavior*, 37, 48-62.
84. Guncaga, J., & Žilková, K. (2019). Visualisation as a method for the development of the term rectangle for pupils in primary school. *European Journal of Contemporary Education*, 8(1), 52-68. <https://doi.org/10.1387/ejced.2019.1.69>
85. Güven, B., & Kosa, T. (2008). The effect of dynamic geometry software on student mathematics teachers' spatial visualization skills. *Turkish Online Journal of Educational Technology-TOJET*, 7(4), 100-107.
86. Guven, B. (2012). Using dynamic geometry software to improve eighth grade students' understanding of transformation geometry. *Australasian Journal of Educational Technology*, 28(2).
87. Hara, T., & Ahara, K. (2020). On materials which allow students to find out mathematical propositions using snapping on GeoGebra. *International Journal for Technology in Mathematics Education*, 27(1). [https://doi.org/10.1564/tme\\_v27.1.02](https://doi.org/10.1564/tme_v27.1.02)
88. Hašek, R. (2019). Dynamic geometry software supplemented with a computer algebra system as a proving tool. *Mathematics in Computer Science*, 13(1), 95-104. <https://doi.org/10.1007/s11786-018-0369-x>
89. Hašek, R. (2019). Exploration of dual curves using a dynamic geometry and computer algebra system. *Mathematics in Computer Science*, 1-8. <https://doi.org/10.1007/s11786-019-00433-4>
90. Hähkiöniemi, M. (2017). Student teachers' types of probing questions in inquiry-based mathematics teaching with and without GeoGebra. *International Journal of Mathematical Education in Science and Technology*, 48(7), 973-987. <https://doi.org/10.1080/0020739X.2017.1329558>
91. Herceg, Đ., & Herceg, D. (2019). Arduino and numerical mathematics. In *Proceedings of the 9th Balkan Conference on Informatics*. <https://doi.org/10.15388/infedu.2020.12>

92. Hernández, A., Perdomo-Díaz, J., & Camacho-Machín, M. (2020). Mathematical understanding in problem solving with GeoGebra: a case study in initial teacher education. *International journal of mathematical education in science and technology*, 51(2), 208-223. <https://doi.org/10.1080/0020739X.2019.1587022>
93. Herceg, D., Radaković, D., Herceg, D., & Mandić, V. H. (2019). Subject-Specific Components in Dynamic Geometry Software. *International Journal for Technology in Mathematics Education*, 26(2). [https://doi.org/10.1564/tme\\_v26.2.07](https://doi.org/10.1564/tme_v26.2.07)
94. Hıdıroğlu, Ç. N., & Bükova Güzel, E. (2013). Conceptualization of approaches and thought processes emerging in validating of model in mathematical modeling in technology aided environment. *Educational Sciences: Theory and Practice*, 13(4), 2499-2508.
95. Hıdıroğlu, Ç. N., & Bükova Güzel, E. (2017). The conceptualization of the mathematical modelling process in technology-aided environment. *The International Journal for Technology in Mathematics Education*, 24(1), 17-36.
96. Halele, B. M. (2020). Developing the usage index for teaching with technology: A case study for Motheo district, South Africa. *TD: The Journal for Transdisciplinary Research in Southern Africa*, 16(1), 1-9. <https://doi.org/10.4102/td.v16i1.668>
97. Hollebrands, K., & Okumuş, S. (2018). Secondary mathematics teachers' instrumental integration in technology-rich geometry classrooms. *The Journal of Mathematical Behavior*, 49, 82-94.
98. Isiksal, M., & Askar, P. (2005). The effect of spreadsheet and dynamic geometry software on the achievement and self-efficacy of 7th-grade students. *Educational Research*, 47(3), 333-350.
99. Isotani, S., & de Oliveira Brandão, L. (2008). An algorithm for automatic checking of exercises in a dynamic geometry system: iGeom. *Computers & Education*, 51(3), 1283-1303.
100. Jacinto, H., & Carreira, S. (2017). Mathematical problem solving with technology: the techno-mathematical fluency of a student-with-GeoGebra. *International Journal of Science and Mathematics Education*, 15(6), 1115-1136.
101. Janičić, P. (2010). Geometry constructions language. *Journal of Automated Reasoning*, 44(1-2), 3.
102. Jesso, A. T., & Kondratieva, M. F. (2016). Instructors' use of technology in post-secondary undergraduate mathematics teaching: a local study. *International Journal of Mathematical Education in Science and Technology*, 47(2), 216-232. <https://doi.org/10.1080/0020739X.2015.1066896>
103. Jokić, M., & Takači, Đ. (2020). Efficiency of dynamic computer environment in learning absolute value equation. *Symmetry*, 12(3), 473. <https://doi.org/10.3390/sym12030473>
104. Kabaca, T. (2013). Using dynamic mathematics software to teach one-variable inequalities by the view of semiotic registers. *Eurasia Journal of Mathematics, Science & Technology Education*, 9(1), 73-81.
105. Kanbur, T. B., & Argün, Z. (2019). Investigation of pre-service elementary mathematics teachers' problem posing situations in dynamic geometry environment= İlköğretim matematik öğretmen adaylarının dinamik geometri yazılımı ile desteklenmiş ortamda problem kurma durumlarının incelenmesi. *Pegem Journal of Education and Instruction*, 9(1), 125-148. <https://doi.org/10.14527/pegegog.2019.005>
106. Kaplar, M., Radović, S., Veljković, K., Simić-Muller, K., & Marić, M. (2021). The influence of interactive learning materials on solving tasks that require different types of mathematical reasoning. *International Journal of Science and Mathematics Education*, 1-23. <https://doi.org/10.1007/s10763-021-10151-8>
107. Khoza, S. B., & Biyela, A. T. (2019). Decolonising technological pedagogical content knowledge of first year mathematics students. *Education and Information Technologies*, 1-15. <https://doi.org/10.1007/s10639-019-10084-4>
108. Knapp, A. K., Barrett, J. E., & Moore, C. J. (2016). Prompting teacher geometric reasoning through coaching in a dynamic geometry software context. *School Science and Mathematics*, 116(6), 326-337.
109. Kohen, Z., Amram, M., Dagan, M., & Miranda, T. (2019). Self-efficacy and problem-solving skills in mathematics: the effect of instruction-based dynamic versus static visualization. *Interactive Learning Environments*, 1-20. <https://doi.org/10.1080/10494820.2019.1683588>
110. Kostić, V. D., Jovanović, V. S., Sekulić, T. M., & Takači, D. B. (2016). Visualization of problem solving related to the quantitative composition of solutions in the dynamic GeoGebra environment. *Chemistry Education Research and Practice*, 17(1), 120-138. <https://doi.org/10.1039/c5rp00156k>

111. Kovács, Z. (2017). Real-time animated dynamic geometry in the classrooms by using fast Gröbner basis computations. *Mathematics in Computer Science*, 11(3-4), 351-361.
112. Kovács, Z. (2019). Achievements and challenges in automatic locus and envelope animations in dynamic geometry. *Mathematics in Computer Science*, 13(1-2), 131-141. <https://doi.org/10.1007/s11786-018-0390-0>
113. Kovács, Z. (2020). Automated detection of interesting properties in regular polygons. *Mathematics in Computer Science*, 14(4), 727-755. <https://doi.org/10.1007/s11786-020-00491-z>
114. Kovács, Z., Recio, T., Richard, P. R., Van Vaerenbergh, S., & Vélez, M. P. (2020). Towards an ecosystem for computer-supported geometric reasoning. *International Journal of Mathematical Education in Science and Technology*, 1-10. <https://doi.org/10.1080/0020739X.2020.1837400>
115. Kovács, Z., Recio, T., & Sólyom-Gecse, C. (2019). Rewriting input expressions in complex algebraic geometry provers. *Annals of Mathematics and Artificial Intelligence*, 85(2), 73-87. <https://doi.org/10.1007/s10472-018-9590-1>
116. Kovács, Z., Recio, T., & Vélez, M. P. (2019). Detecting truth, just on parts. *Revista Matemática Complutense*, 32(2), 451-474. <https://doi.org/10.1007/s13163-018-0286-1>
117. Kovács, Z., Recio, T., & Vélez, M. P. (2020). Reasoning about linkages with dynamic geometry. *Journal of Symbolic Computation*, 97, 16-30. <https://doi.org/10.1016/j.jsc.2018.12.003>
118. Koyuncu, I., Akyuz, D., & Cakiroglu, E. (2015). Investigating plane geometry problem-solving strategies of prospective mathematics teachers in technology and paper-and-pencil environments. *International Journal of Science and Mathematics Education*, 13(4), 837-862.
119. Kurtuluş, A. (2013). The effects of web-based interactive virtual tours on the development of prospective mathematics teachers' spatial skills. *Computers & Education*, 63, 141-150.
120. Kusumah, Y. S., Kustiawati, D., & Herman, T. (2020). The effect of GeoGebra in three-dimensional geometry learning on students' mathematical communication ability. *International Journal of Instruction*, 13(2), 895-908. <https://doi.org/10.29333/iji.2020.13260a>
121. Kuzle, A. (2017). Delving into the nature of problem solving processes in a dynamic geometry environment: Different technological effects on cognitive processing. *Technology, Knowledge and Learning*, 22(1), 37-64.
122. Lavicza, Z., & Papp-Varga, Z. (2010). Integrating GeoGebra into IWB-equipped teaching environments: preliminary results. *Technology, Pedagogy and Education*, 19(2), 245-252. <https://doi.org/10.1080/1475939X.2010.491235>
123. Lavicza, Z., Prodromou, T., Fenyvesi, K., Hohenwarter, M., Juhos, I., Koren, B., & Manuel Diego-Mantecón, J. (2020). Integrating STEM-related technologies into mathematics education at a large scale. *International Journal for Technology in Mathematics Education*, 27(1).
124. Lognoli, D. (2017). The Area of the disk in middle school grade by GeoGebra. *International Journal of Emerging Technologies in Learning (iJET)*, 12(11), 28-40.
125. Mainali, B. R., & Heck, A. (2017). Comparison of traditional instruction on reflection and rotation in a Nepalese high school with an ICT-rich, student-centered, investigative approach. *International Journal of Science and Mathematics Education*, 15(3), 487-507.
126. Manganyana, C., van Putten, S., & Rauscher, W. (2020). The use of GeoGebra in disadvantaged rural geometry classrooms. *International Journal of Emerging Technologies in Learning (iJET)*, 15(14), 97-108. <https://doi.org/10.3991/inet.v15i14.13739>
127. Marciuc, D., Miron, C., & Barna, E. S. (2016). Using geogebra software in the teaching of oscillatory motions. *Romanian Reports in Physics*, 68(3), 1296-1311.
128. Martinovic, D., & Manizade, A. G. (2020). Teachers using GeoGebra to visualize and verify conjectures about trapezoids. *Canadian Journal of Science, Mathematics and Technology Education*, 20(3), 485-503. <https://doi.org/10.1007/s42330-020-00103-9>
129. Mazzotti, A. A. (2014). A Euclidean approach to eggs and polycentric curves. *Nexus Network Journal*, 16(2), 345-387.
130. Mazzotti, A. A. (2014). What Borromini might have known about ovals. Ruler and compass constructions. *Nexus Network Journal*, 16(2), 389-415.
131. Milanović, I., Vukobratović, R., & Raičević, V. (2012). Mathematical modelling of the effect of temperature on the rate of a chemical reaction. *Croatian Journal of Education*, 14(3), 681-709.

132. Miletic, L., & Lešaja, G. (2016). Research and evaluation of the effectiveness of e-learning in the case of linear programming. *Croatian Operational Research Review*, 7(1), 109-127. Doi: 10.17535/crorr.2016.0008
133. Misfeldt, M., & Zacho, L. (2016). Supporting primary-level mathematics teachers' collaboration in designing and using technology-based scenarios. *Journal of Mathematics Teacher Education*, 19(2-3), 227-241.
134. Misrom, N. B., Muhammad, A., Abdullah, A., Osman, S., Hamzah, M., & Fauzan, A. (2020). Enhancing students' higher-order thinking skills (HOTS) through an inductive reasoning strategy using geogebra. *International Journal of Emerging Technologies in Learning (iJET)*, 15(3), 156-179.
135. Monteiro Paulo, R., Pereira, A. L., & Pavanelo, E. (2021). The constitution of mathematical knowledge with augmented reality. *The Mathematics Enthusiast*, 18(3), 641-668.
136. Mthethwa, M., Bayaga, A., Bossé, M. J., & Williams, D. (2020). GeoGebra for learning and teaching: a parallel investigation. *South African Journal of Education*, 40(2). <https://doi.org/10.15700/saje.v40n2a1669>
137. Mudaly, V., & Fletcher, T. (2019). The effectiveness of geogebra when teaching linear functions using the iPad. *Problems of Education in the 21st Century*, 77(1), 55. <https://doi.org/10.33225/pec/19.77.55>
138. Murtafiah, W., Sa'dijah, C., Tjang, D. C., & Susiswo, S. (2019). Decision making of the winner of the national student creativity program in designing ICT-based learning media. *TEM Journal*, 8(3), 1039. <https://doi.org/10.18421/TEM83-49>
139. Mushipe, M., & Ogbonnaya, U. I. (2019). Geogebra and grade 9 learners' achievement in linear functions. <https://doi.org/10.3991/ijet.v14i08.9581>
140. Ngwabe, A., & Felix, C. (2020). Using GeoGebra to address students' misconceptions about the transformation of algebraic hyperbola functions. *African Journal of Research in Mathematics, Science and Technology Education*, 24(3), 348-360. <https://doi.org/10.1080/18117295.2020.1854494>
141. Nikolić, M., Marinković, V., Kovács, Z., & Janičić, P. (2019). Portfolio theorem proving and prover runtime prediction for geometry. *Annals of Mathematics and Artificial Intelligence*, 85(2), 119-146. <https://doi.org/10.1007/s10472-018-9598-6>
142. Nobre, C. N., Meireles, M. R. G., Vieira Jr, N., De Resende, M. N., Da Costa, L. E., & Da Rocha, R. C. (2016). The use of geogebra software as a calculus teaching and learning tool. *Informatics in Education*, 15(2), 253-267.
143. Nordin, N., Zakaria, E., Mohamed, N. R. N., & Embi, M. A. (2010). Pedagogical usability of the Geometer's Sketchpad (GSP) digital module in the mathematics teaching. *Turkish Online Journal of Educational Technology-TOJET*, 9(4), 113-117.
144. Olsson, J., & Granberg, C. (2019). Dynamic software, task solving with or without guidelines, and learning outcomes. *Technology, knowledge and learning*, 24(3), 419-436. <https://doi.org/10.1007/s10758-018-9352-5>
145. Oner, D. (2013). Analyzing group coordination when solving geometry problems with dynamic geometry software. *International Journal of Computer-Supported Collaborative Learning*, 8(1), 13-39.
146. Ovodenko, R., & Kouropatov, A. (2019). The use of digital tools to confront errors during advanced calculus learning: the case of the inflection point. *Mathematics in Computer Science*, 13(1), 217-236. <https://doi.org/10.1007/s11786-018-0365-1>
147. Oxman, V., & Stupel, M. (2020). Conserved properties in polygons obtained by a point reflecting process. *International Journal of Mathematical Education in Science and Technology*, 1-11. <https://doi.org/10.1080/0020739X.2020.1850898>
148. Öcal, M.F., Kar, T., Güler, G., and Ipek, A.S. (2020). Comparison of prospective mathematics teachers' problema posing abilities in paper-pencil test and on dynamic geometry environment in terms of creativity. *REDIMAT – Journal of Research in Mathematics Education*, 9(3), 243-272. <https://doi.org/10.17583/redimat.2020.3879>
149. Öner, D. (2008). Supporting students' participation in authentic proof activities in computer supported collaborative learning (CSCL) environments. *International Journal of Computer-Supported Collaborative Learning*, 3(3), 343.
150. Paiva, R. C., Ferreira, M. S., Mendes, A. G., & Eusébio, A. M. (2015). Interactive and multimedia contents associated with a system for computer-aided assessment. *Journal of Educational Computing Research*, 52(2), 224-256.
151. Palomares-Ruiz, A., Cebrián, A., López-Parra, E., & García-Toledano, E. (2020). Influence of ICTs on math teaching-learning processes and their connection to the digital gender gap. *Sustainability*, 12(16), 6692. <https://doi.org/10.3390/su12166692>

152. Park, J., & Flores, A. (2015). Fermat's point from five perspectives. *International Journal of Mathematical Education in Science and Technology*, 46(3), 425-441.
153. Pitta-Pantazi, D., & Christou, C. (2009). Cognitive styles, dynamic geometry and measurement performance. *Educational Studies in Mathematics*, 70(1), 5-26.
154. Pittalis, M. (2020). Extending the technology acceptance model to evaluate teachers' intention to use dynamic geometry software in geometry teaching. *International Journal of Mathematical Education in Science and Technology*, 1-20. <https://doi.org/10.1080/0020739X.2020.1766139>
155. Podayeva, N. G., Podayev, M. V., & Agafonov, P. A. (2019). The social and cultural approach to forming geometric concepts among schoolchildren. *Amazonia Investiga*, 8(20), 459-467.
156. Podaeva, N. G., Podaev, M. V., & Agafonov, P. A. (2021). Development of the activity of gifted schoolchildren in mastering geometric concepts in figurative structures. *Propósitos y Representaciones*, 9(SPE3), 1126. <https://doi.org/10.20511/pyr2021.v9nSPE3.1126>
157. Ponce Campuzano, J. C., Roberts, A. P., Matthews, K. E., Wegener, M. J., Kenny, E. P., & McIntyre, T. J. (2019). Dynamic visualization of line integrals of vector fields: a didactic proposal. *International Journal of Mathematical Education in Science and Technology*, 50(6), 934-949. <https://doi.org/10.1080/0020739X.2018.1510554>
158. Poon, K. K., & Wong, K. L. (2017). Pre-constructed dynamic geometry materials in the classroom—how do they facilitate the learning of 'Similar Triangles'? *International Journal of Mathematical Education in Science and Technology*, 48(5), 735-755.
159. Poon, K. K. (2018). Learning fraction comparison by using a dynamic mathematics software—GeoGebra. *International Journal of Mathematical Education in Science and Technology*, 49(3), 469-479.
160. Prusak, N., Hershkowitz, R., & Schwarz, B. B. (2012). From visual reasoning to logical necessity through argumentative design. *Educational Studies in Mathematics*, 79(1), 19-40.
161. Radaković, D., & Herceg, Đ. (2018). Towards a completely extensible dynamic geometry software with metadata. *Computer Languages, Systems & Structures*, 52, 1-20.
162. Radović, S., Radojičić, M., Veljković, K., & Marić, M. (2020). Examining the effects of Geogebra applets on mathematics learning using interactive mathematics textbook. *Interactive Learning Environments*, 28(1), 32-49. <https://doi.org/10.1080/10494820.2018.1512001>
163. Rau, M. A. (2017). Do knowledge-component models need to incorporate representational competencies?. *International Journal of Artificial Intelligence in Education*, 27(2), 298-319.
164. Redo, T., Richard, P. R., & Vélez, M. P. (2019). Designing tasks supported by GeoGebra automated reasoning tools for the development of mathematical skills. *International Journal for Technology in Mathematics Education*, 26(2). [https://doi.org/10.1564/tme\\_v26.2.05](https://doi.org/10.1564/tme_v26.2.05)
165. Reyes-Rodriguez, A., Santos-Trigo, M., & Barrera-Mora, F. (2016). The construction of a square through multiple approaches to foster learners' mathematical thinking. *Teaching Mathematics and its Applications: An International Journal of the IMA*, 36(3), 167-181.
166. Richard, P. R., Marcén, A. M. O., & Seguí, V. M. (2016). The concept of proof in the light of mathematical work. *ZDM*, 48(6), 843-859.
167. Roanes-Lozano, E. (2017). A brief note on the approach to the conic sections of a right circular cone from dynamic geometry. *Mathematics in Computer Science*, 11(3-4), 439-448.
168. Romero, C., & Martínez, E. (2013). Achievements of engineering students on a fluid mechanics course in relation to the use of illustrative interactive simulations. *European Journal of Physics*, 34(4), 873.
169. Rososzczuk, R. (2015). Application of Cabri 3D in teaching stereometry. *Advances in Science and Technology Research Journal*, 9(26), 148-151.
170. Santos-Trigo, M., & Reyes-Rodriguez, A. (2016). The use of digital technology in finding multiple paths to solve and extend an equilateral triangle task. *International Journal of Mathematical Education in Science and Technology*, 47(1), 58-81.
171. Segal, R., Stupel, M., & Oxman, V. (2016). Dynamic investigation of loci with surprising outcomes and their mathematical explanations. *International Journal of Mathematical Education in Science and Technology*, 47(3), 443-462.
172. Selaković, M., Marinković, V., & Janičić, P. (2020). New dynamics in dynamic geometry: Dragging constructed points. *Journal of Symbolic Computation*, 97, 3-15. <https://doi.org/10.1016/j.jsc.2018.12.002>

- 173.Semenikhina, O. V., Drushlyak, M. H., Bondarenko, Y. A., Kondratuk, S. M., & Dehtiarova, N. V. (2019). Cloud-based service GeoGebra and its use in the educational process: the BYOD-approach. <https://doi.org/10.18421/TEM81-08>
- 174.Sigler, A., Stupel, M., & Flores, A. (2017). Relations among five radii of circles in a triangle, its sides and other segments. *International Journal of Mathematical Education in Science and Technology*, 48(5), 782-793.
- 175.Soliman, M., Lavicza, Z., Prodromou, T., Al-Kandari, M., & Houghton, T. (2019). Enhancing Kuwaiti teachers' technology-assisted mathematics teaching practices. *International Journal for Technology in Mathematics Education*, 26(2). [https://doi.org/10.1564/tme\\_v26.2.04](https://doi.org/10.1564/tme_v26.2.04)
- 176.Solin, P., & Roanes-Lozano, E. (2020). Using computer programming as an effective complement to mathematics education: experimenting with the standards for mathematics practice in a multidisciplinary environment for teaching and learning with technology in the 21 st century. *International Journal for Technology in Mathematics Education*, 27(3). [https://doi.org/10.1564/tme\\_v27.3.03](https://doi.org/10.1564/tme_v27.3.03)
- 177.Stols, G., & Kriek, J. (2011). Why don't all maths teachers use dynamic geometry software in their classrooms?. *Australasian Journal of Educational Technology*, 27(1).
- 178.Stols, G. (2012). Does the use of technology make a difference in the geometric cognitive growth of pre-service mathematics teachers?. *Australasian Journal of Educational Technology*, 28(7).
- 179.Stupel, M., Weissman, S., & Sigler, A. (2020). Closed orbits parallel to quadrilaterals inscribed in various conic sections. *International Journal of Mathematical Education in Science and Technology*, 1-11. <https://doi.org/10.1080/0020739X.2020.1819575>
- 180.Sümmermann, M. L., Sommerhoff, D., & Rott, B. (2021). Mathematics in the digital age: the case of simulation-based proofs. *International Journal of Research in Undergraduate Mathematics Education*, 1-28. <https://doi.org/10.1007/s40753-020-00125-6>
- 181.Takači, D., Stankov, G., & Milanovic, I. (2015). Efficiency of learning environment using GeoGebra when calculus contents are learned in collaborative groups. *Computers & Education*, 82, 421-431.
- 182.Takači, D., Takači, A., & Takači, A. (2014). On the operational solutions of fuzzy fractional differential equations. *Fractional Calculus and Applied Analysis*, 17(4), 1100-1113.
- 183.Takato, S., McAndrew, A., Vallejo, J. A., & Kaneko, M. (2017). Collaborative Use of KeTCindy and free computer algebra systems. *Mathematics in Computer Science*, 11(3-4), 503-514.
- 184.Tamur, M., Juandi, D., & Kusumah, Y. S. (2020). The effectiveness of the application of mathematical software in Indonesia; a meta-analysis study. *International Journal of Instruction*, 13(4), 867-884. <https://doi.org/10.29333/iji.2020.13453a>
- 185.Tatar, E., & Zengin, Y. (2016). Conceptual understanding of definite integral with Geogebra. *Computers in the Schools*, 33(2), 120-132.
- 186.Tomić, M. K., Aberšek, B., & Pesek, I. (2019). GeoGebra as a spatial skills training tool among science, technology engineering and mathematics students. *Computer Applications in Engineering Education*, 27(6), 1506-1517. <https://doi.org/10.1002/cae.22165>
- 187.Turgut, M. (2019). Sense-making regarding matrix representation of geometric transformations in  $R^2$ : a semiotic mediation perspective in a dynamic geometry environment. *ZDM*, 51(7), 1199-1214. <https://doi.org/10.1007/s11858-019-01032-0>
- 188.Ubuz, B., Üstün, I., & Erbaş, A. K. (2009). Effect of dynamic geometry environment on immediate and retention level achievements of seventh grade students. *Eurasian Journal of Educational Research (EJER)*, (35).
- 189.Urrutia, F. Z., Loyola, C. C., & Marín, M. H. (2019). A tangible user interface to facilitate learning of trigonometry. *International Journal of Emerging Technologies in Learning (iJET)*, 14(23), 152-164. <https://doi.org/10.3991/ijet.v14i23.11433>
- 190.Uygun, T. (2020). An inquiry-based design research for teaching geometric transformations by developing mathematical practices in dynamic geometry environment. *Mathematics Education Research Journal*, 1-27. <https://doi.org/10.1007/s13394-020-00314-1>
- 191.Velikova, E., & Petkova, M. (2019). Analysing students' creativity in integrating GeoGebra applets in solving geometrical problems. *Baltic Journal of Modern Computing*, 7(3), 419-429. <https://doi.org/10.22364/bjmc.2019.7.3.08>

- 192.Verhoef, N. C., Coenders, F., Pieters, J. M., van Smaalen, D., & Tall, D. O. (2015). Professional development through lesson study: teaching the derivative using GeoGebra. *Professional development in education*, 41(1), 109-126.
- 193.Weinhandl, R., Lavicza, Z., Hohenwarter, M. & Schallert, S. (2020). Enhancing flipped mathematics education by utilising GeoGebra. *International Journal of Education in Mathematics, Science and Technology (IJEMST)*, 8(1), 1-15.
- 194.Widjajanti, K., Nusantara, T., As'ari, A. R., Irawati, S., Haris, Z. A., Akbar, D. N., & Lusbiantoro, R. (2019). Delaying scaffolding using geogebra: improving the ability of vocational students to draw conclusions. *TEM Journal*, 8(1), 305. <https://doi.org/10.18421/TEM81-42>
- 195.Xing, W., Guo, R., Petakovic, E., & Goggins, S. (2015). Participation-based student final performance prediction model through interpretable Genetic Programming: Integrating learning analytics, educational data mining and theory. *Computers in Human Behavior*, 47, 168-181.
- 196.Xing, W., Wadholm, R., Petakovic, E., & Goggins, S. (2015). Group learning assessment: Developing a theory-informed analytics. *Journal of Educational Technology & Society*, 18(2).
- 197.Yanik, H. B. (2013). Learning geometric translations in a dynamic geometry environment. *Education & Science/Egitim ve Bilim*, 38(168).
- 198.Yao, X. (2020). Unpacking learner's growth in geometric understanding when solving problems in a dynamic geometry environment: Coordinating two frames. *The Journal of Mathematical Behavior*, 60, 100803. <https://doi.org/10.1016/j.jmathb.2020.100803>
- 199.Yi, T. (2017). Creating teaching module in pdf with embedded animations and lecture note. *International Journal Of Education And Information Technologies*, 11, 51-57.
- 200.Zambak, V. S., & Tyminski, A. M. (2020). Examining mathematical technological knowledge of pre-service middle grades teachers with Geometer's Sketchpad in a geometry course. *International Journal of Mathematical Education in Science and Technology*, 51(2), 183-207. <https://doi.org/10.1080/0020739X.2019.1650302>
- 201.Žilinskienė, I., & Demirbilek, M. (2015). Use of GeoGebra in primary math education in Lithuania: An Exploratory Study from Teachers' Perspective. *Informatics in Education*, 14(1).
- 202.Zengin, Y. (2017). Investigating the use of the Khan Academy and mathematics software with a flipped classroom approach in mathematics teaching. *Journal of Educational Technology & Society*, 20(2), 89-100.
- 203.Zengin, Y. (2017). The effects of GeoGebra software on pre-service mathematics teachers' attitudes and views toward proof and proving. *International Journal of Mathematical Education in Science and Technology*, 48(7), 1002-1022.
- 204.Zengin, Y. (2019). Development of mathematical connection skills in a dynamic learning environment. *Education and Information Technologies*, 24(3), 2175-2194. <https://doi.org/10.1007/s10639-019-09870-x>
- 205.Zengin, Y., Furkan, H., & Kutluca, T. (2012). The effect of dynamic mathematics software geogebra on student achievement in teaching of trigonometry. *Procedia-Social and Behavioral Sciences*, 31, 183-187.
- 206.Zengin, Y., & Tatar, E. (2015). The teaching of polar coordinates with dynamic mathematics software. *International Journal of Mathematical Education in Science and Technology*, 46(1), 127-139. <https://doi.org/10.1080/0020739X.2014.904529>
- 207.Zengin, Y., & Tatar, E. (2017). Integrating dynamic mathematics software into cooperative learning environments in mathematics. *Journal of Educational Technology & Society*, 20(2), 74-88.
- 208.Zetriuslita, N., & Istikomah, E. (2021). The increasing self-efficacy and self-regulated through GeoGebra based teaching reviewed from initial mathematical ability (IMA) level. *International Journal of Instruction*, 14(1), 587-598. <https://doi.org/10.29333/iji.2021.14135a>
- 209.Zulnaidi, H., Oktavika, E., & Hidayat, R. (2020). Effect of use of GeoGebra on achievement of high school mathematics students. *Education and Information Technologies*, 25(1), 51-72. <https://doi.org/10.1007/s10639-019-09899-y>
- 210.Zulnaidi, H., & Zamri, S. N. A. S. (2017). The effectiveness of the geogebra software: the intermediary role of procedural knowledge on students' conceptual knowledge and their achievement in mathematics. *Eurasia Journal of Mathematics, Science and Technology Education*, 13(6), 2155-2180.

Ondes, R. N. (2021). Research trends in dynamic geometry software: A content analysis from 2005 to 2021. *World Journal on Educational Technology: Current Issues*. 13(2), 236-260. <https://doi.org/10.18844/wjet.v13i2.5695>