

**Technical Report Number 08-02**

**Instrument Development Procedures for Mathematics Measures**

Eunju Jung

Kimy Liu

Leanne R. Ketterlin-Geller

Gerald Tindal

University of Oregon

Behavioral Research and Teaching



behavioral research & teaching

Published by

Behavioral Research and Teaching  
University of Oregon • 175 Education  
5262 University of Oregon • Eugene, OR 97403-5262  
Phone: 541-346-3535 • Fax: 541-346-5689  
<http://brt.uoregon.edu>

This research was supported by Project INFORM (H327B050013-07) from Office of Special Education Programs, U.S. Department of Education. BRT is affiliated with the College of Education, University of Oregon. Opinions expressed herein do not necessarily reflect those of the U.S. Department of Education or Offices within it.

Copyright © 2008. Behavioral Research and Teaching. All rights reserved. This publication, or parts thereof, may not be used or reproduced in any manner without written permission.

The University of Oregon is committed to the policy that all persons shall have equal access to its programs, facilities, and employment without regard to race, color, creed, religion, national origin, sex, age, marital status, disability, public assistance status, veteran status, or sexual orientation. This document is available in alternative formats upon request.

## Abstract

The purpose of this study was to develop general outcome measures (GOM) in mathematics so that teachers could focus their instruction on needed prerequisite skills. We describe in detail, the manner in which content-related evidence was established and then present a number of statistical analyses conducted to evaluate the technical adequacy of these measures. The outcomes support the test development process and reflect a series of measures that have potential for use in elementary and middle school mathematics programs.

### *Introduction*

Computation is a basic skill of mathematics. Students who have difficulty in computation might have trouble in their daily life, as well as problems with other higher levels of mathematics such as geometry, estimation, and statistics. Computation is an essential tool for studying other demanding mathematical applications such as physics, chemistry, and computer science. Considering the hierarchical nature of mathematics, speed and accuracy in computation play an important role in overall mathematics abilities.

How can we assess computation skills? Researchers have reported that formative evaluation enables teachers to tell if their instructional methods work for their students (Stecker & Fuchs, 2000). Formative evaluation has several advantages for classroom teachers, including easy administration and interpretation, as well as providing useful information about students' performance with repeated and frequent measurement (Deno, 1985; Shinn, 1989; Thurber, Shinn, & Smolkowski, 2002). CBM is well known as a good instrument to measure students' reading proficiency (Deno, 1985; Shinn, 1989, 1998; Thurber, Shinn, & Smolkowski, 2002). Unfortunately, compared with reading CBM, the technical adequacy of mathematics-curriculum-based measurement (M-CBM) is not well known. Of the few studies conducted, Tindal, Marston, and Deno (1983) reported that M-CBM presented high inter-rater agreement (.97), high 1-week test-retest reliability (.87), and moderate alternate form reliability (.66).

The purpose of this technical report is to describe research conducted on computer-administered M-CBM for students in grades 3-8. Students were administered a 15-item M-CBM. Item-response theory (IRT) analyses indicate that the measures adequately fit the model parameters and represent a range of difficulty levels. As such, evidence suggests that these

measures may be useful for providing information about students' mathematics computation ability.

### *Methods*

#### *Setting and Participants*

Twelve elementary- and middle-schools in two large, suburban districts in the Pacific Northwest participated in this study. Approximately 35 teachers from grades 3-8 participated in this pilot testing. A total of over 1,300 students with more than 200 students in each grade took the tests.

Testing took place either in the schools' computer labs or in the teachers' classrooms if they had a mobile laptop lab. For each testing session, the teacher and students were assembled with computers connected to the Internet. BRT staff members (two staff members for each testing session) showed students how to access the test through a secure website. A BRT staff member read the standardized Directions for Administration (Appendix A) to students and then the students began testing. Testing took place during a four-week window from the last week of February 2007 through the third week of March 2007.

#### *Measurement/Instrument Development*

A Research Assistant at BRT wrote all items. The item writer had a B.S. in mathematics as well as a B.A. and a M.A in special education. She was concurrently enrolled in a Ph.D. course in Special Education at the University of Oregon. The item writer had experience in developing and validating mathematics CBM measures for grades 2 through 4 in her Master's program. She has a secondary special educator license with mathematics specialization.

The item writer created 15 computation items for each grade, for grades 3 to 8. These items were written from grade level content standards in the domain of Numbers and Operations.

To do this, the item writer reviewed mathematics standards of NCTM, Oregon State, Washington State, Hawaii State, and West Virginia State. Table 1 below indicates the specific number of items by task type for each grade level.

Table 1.

Number of items by task type for each grade level.

| Grade | Task type                         | # of Items | Specific task type   |
|-------|-----------------------------------|------------|--|
| 3     | Addition<br>(whole numbers)       | 4          | - Adding two three-digit numbers with renaming from tens to hundreds<br>- Adding two three-digit numbers with renaming from ones to tens and tens to hundreds<br>- Adding three two-digit numbers with renaming (one column totals less than 20)<br>- Adding four numbers with renaming from ones to tens and from tens to hundreds (sums of columns below 20)   |
|       |                                   |            | - Subtracting a two-digit number from a three-digit number with renaming from hundreds to tens<br>- Subtracting a three-digit number from a three-digit number with renaming from tens to ones and hundreds to tens<br>- Subtracting a three-digit number from a three-digit number, zero in tens column with renaming from tens to ones and hundreds to tens<br>- Subtracting a four-digit number from a four-digit number with renaming from thousands to hundreds<br>- Subtracting a three-digit number from a four-digit number with renaming from thousands to hundreds |
|       | Subtraction<br>(whole numbers)    | 5          | - Subtracting a two-digit number from a three-digit number with renaming from hundreds to tens<br>- Subtracting a three-digit number from a three-digit number with renaming from tens to ones and hundreds to tens<br>- Subtracting a three-digit number from a three-digit number, zero in tens column with renaming from tens to ones and hundreds to tens<br>- Subtracting a four-digit number from a four-digit number with renaming from thousands to hundreds<br>- Subtracting a three-digit number from a four-digit number with renaming from thousands to hundreds |
|       |                                   |            | - Subtracting a two-digit number from a three-digit number with renaming from hundreds to tens<br>- Subtracting a three-digit number from a three-digit number with renaming from tens to ones and hundreds to tens<br>- Subtracting a three-digit number from a three-digit number, zero in tens column with renaming from tens to ones and hundreds to tens<br>- Subtracting a four-digit number from a four-digit number with renaming from thousands to hundreds<br>- Subtracting a three-digit number from a four-digit number with renaming from thousands to hundreds |
|       | Multiplication<br>(whole numbers) | 3          | - One-digit factor times two-digit factor with no carrying<br>- One-digit factor times two-digit factor with carrying<br>- One-digit factor times two-digit factor (problems written horizontally)   |
|       | Division<br>(whole numbers)       | 3          | - Two-digit dividend; one-digit divisor; one-digit quotient; no remainder  |
|       | Multiplication<br>(whole numbers) | 3          | - Three-digit factor times one-digit factor<br>- Three-digit factor times one-digit factor with zero in tens column<br>- Three-digit factor times one-digit factor with horizontal alignment<br>- Three-digit dividend; one-digit divisor; no remainder<br>- Three-digit dividend; one-digit divisor; remainder  |
|       | Division<br>(whole numbers)       | 4          | - Two-digit dividend; one-digit divisor; two-digit quotient; no remainder<br>- Two-digit dividend; one-digit divisor; two-digit quotient; remainder  |
| 4     | Addition<br>(fractions)           | 2          | - Adding fractions with like denominators  |
|       | Subtraction<br>(fractions)        | 2          | - Subtracting fractions with like denominators   |
|       | Addition<br>(decimals)            | 2          | - Adding tenths, hundredths and whole number<br>- Adding tenths and two whole numbers  |
|       | Subtraction<br>(decimals)         | 2          | - Subtracting tenths from whole number<br>- Subtracting hundredths from whole number   |
|       | Division<br>(whole numbers)       | 4          | - Two-digit divisor; one-digit quotient<br>- Two-digit divisor; two-digit quotient   |
| 5     | Addition<br>(fractions)           | 3          | - Adding two fractions with different denominators<br>- Adding two fractions with reducing and converting to mixed numbers<br>- Adding three fractions with different denominators, reducing, and converting to mixed numbers  |
|       | Subtraction<br>(fractions)        | 3          | - Subtracting mixed numbers from whole number<br>- Subtracting fractions with mixed numbers<br>- Subtracting fractions with different denominators, mixed numbers and reducing   |
|       | Multiplication<br>(decimals)      | 2          | - Multiplying decimals; one-digit factor times three-digit factor<br>- Multiplying decimals; zero to be placed after decimal point   |
|       | Division<br>(decimals)            | 3          | - Whole number divisor; no remainder<br>- Divisor is decimal; adding zeros in dividend required<br>- Divisor is decimal, no adding zeros in dividend necessary   |
|       | Division<br>(decimals)            | 3          | - Whole number divisor; no remainder<br>- Divisor is decimal; adding zeros in dividend required<br>- Divisor is decimal, no adding zeros in dividend necessary   |

|   |                             |   |  |
|---|-----------------------------|---|--|
| 6 | Multiplication (fractions)  | 2 | - Multiplying mixed numbers  |
|   | Division (fractions)        | 6 | - Dividing fractions<br>- Dividing fractions by whole numbers<br>- Dividing mixed numbers by whole numbers   |
|   | Multiplication (decimals)   | 2 | - Multiplying decimals; two digit factor times three digit factor  |
|   | Division (decimals)         | 5 | - Dividing decimals by whole number; quotient begins with zero (2)<br>- Whole number divisor; zeros must be added to dividend after decimal point (3)  |
| 7 | Addition (integers)         | 4 | - Adding integers; two three-digit numbers<br>- Adding integers; three two-digit numbers<br>- Adding integers; four numbers<br>- Adding integers; four-digit numbers   |
|   | Subtraction (integers)      | 4 | - Subtracting integers; three-digit number from a three-digit number<br>- Subtracting integers; two-digit number from a three-digit number<br>- Subtracting integers; four-digit number from a four-digit number<br>- Subtracting integers; two-digit number from a three-digit number, zero in tens column                  |
|   | Multiplication (integers)   | 4 | - Multiplying integers: two-digit factor times two-digit factor<br>- Multiplying integers: two-digit factor times three-digit factor<br>- Multiplying integers: three-digit factor times three-digit factor<br>- Multiplying integers: three-digit factor times three-digit factor; zero in tens factor column of multiplier |
|   | Division (integers)         | 3 | - Dividing integers: three-digit dividend; three-digit quotient<br>- Dividing integers: four-digit quotient; one-digit divisor; four-digit dividend<br>- Dividing integers: two-digit divisor; one digit quotient  |
| 8 | Computation (whole numbers) | 4 | - Adding three four-digit numbers<br>- Subtracting five-digit number from five-digit number<br>- Three-digit factor times three-digit factor<br>- Five-digit dividend; two-digit divisor; three-digit quotient; no remainder   |
|   | Computation (decimals)      | 4 | - Adding hundredths and tenths<br>- Subtracting hundredths from hundredths<br>- Multiplying decimals; three-digit factor times three-digit factor<br>- Whole number divisor; no remainder  |
|   | Computation (fractions)     | 4 | - Adding three fractions with different denominators<br>- Subtracting mixed number from whole number<br>- Mixed number times whole number<br>- Dividing fractions  |
|   | Computation (integers)      | 3 | - Subtraction with three integers<br>- Multiplication with three integers<br>- Four-digit dividend; two-digit divisor; three-digit quotient  |

Each item had four answer options with one correct answer and three distractors. The distractors represented possible student errors. To find student error patterns, the item writer referenced the book, *Designing Effective Mathematics Instruction: A direct instruction approach* (Stein, Silbert, & Carnine, 1997). In addition, to keep students from determining the answer based on position in the choices, the item writer randomly placed the correct answer choices, with four in the first position, four in the second position, four in the third position, and three in the fourth position.

### *Design and Operational Procedures*

After the item writer created the measures, a BRT staff member reviewed the measures to evaluate them for grade-level appropriateness and adherence to test specifications.

### *Internal Review*

*Qualifications of the internal reviewer.* The internal reviewer was a third year Ph.D. student in Special Education at the University of Oregon. She had an elementary teacher certificate for grades 1 to 6 and finished her licensure training for special education teachers. The internal reviewer worked as an ESL teacher for two years, during which time she helped developed a reading curriculum for ESL students. She also worked as an elementary school teacher for two years and a freelance curriculum developer for six months.

*Internal review procedures and results.* The internal reviewer first examined the test items' adherence to the test specifications provided by the instrument developing team. The reviewer claimed that the division problem format was not familiar to students, and suggested a change to an appropriate format. Additionally, she suggested changing several answer choices for common student errors. Finally the reviewer indicated the need for numerals to be aligned by place-value in computation problems in order to avoid students' confusion.

The item writer revised the measures and incorporated the suggestions into the measures. She changed the division format to what students are familiar with (for example,  $23 \overline{)94}$ ). In addition, the item writer revised the answer choices according to the internal reviewer's suggestions. Finally, she rearranged the column line of the test items.



### *External Review*

Six teachers from local public schools participated in reviewing the mathematics measures. They reviewed the items for grade-level appropriateness of language and vocabulary, content and concepts, directions, and potential bias.

*Qualifications of external reviewers.* The external reviewers' teaching experiences ranged from less than one year to 28 years. They all have Master's degrees. The specific teachers' backgrounds and qualifications are listed in Table 2 below.

Table 2.

Teachers' backgrounds and qualifications.

| Teacher | Current teaching position     | Education | Teaching experience |
|---------|-------------------------------|-----------|---------------------|
| 1       | SpED K-5                      | M. Ed     | 17 years            |
| 2       | 5 <sup>th</sup> grade         | M. Ed     | 2 years             |
| 3       | Reading Specialist            | M. Ed     | 4 years             |
| 4       | 6 <sup>th</sup> and 7th grade | M. Ed     | 0.5 year            |
| 5       | 8 <sup>th</sup> grade         | M. Ed     | 3 years             |
| 6       | 7 <sup>th</sup> grade         | M. A.     | 17 years            |

*External review procedures and results.* Each teacher reviewed measures for one grade level by evaluating the grade-level appropriateness and rating them according to several criteria, including language and vocabulary, content and concepts, directions, effectiveness of distractors, and bias. Teachers rated the test items and distractors on a scale of 1 to 4 for each criterion. A rating of 1 meant that the items were not at all appropriate in relation to the criterion; a rating of 2 meant that the items were somewhat appropriate in relation to the criterion; a rating of 3 meant

that the items were sufficiently appropriate in relation to the criterion; and a rating of 4 meant that the items were extremely appropriate in relation to the criterion. Teachers were also asked to provide additional suggestions and comments regarding the measures.

Teacher reviewers provided similar suggestions to the internal reviewer. First, they pointed out that the division format needed to be changed to what students are familiar with. Second, they gave specific suggestions for answer choices for common student errors. Finally, one of the teacher reviewers indicated the column problems needed proper alignment. After receiving teachers' feedback on the measures, the item writer revised the distractors, fixed the division problem format, and rearranged the column line based on the internal reviewer's suggestions.

To finalize the revision process, the item writer conducted a final review of all measures prior to implementing the items in the pilot testing. She evaluated alignment of measures with the test specifications and the appropriateness of content for the target grade level audience. From this procedure, she found that a couple of items did not have correct answers among the answer choices and immediately revised those items.

### *Results*

The parameter files reported the intercepts, slopes and item difficulty for each item. These numbers helped in calculating the likelihood of examinees of different skill levels answering the test item correctly. The BILOG-MG excluded Item 10 of the Grade 4 measure and Item 14 of the Grade 5 measure for the item calibration, because these two items were negatively correlated with the rest of the test items in that particular grade. The authors recommended reviewing these two test items.

### *Pilot Testing Findings*

To evaluate the technical adequacy of the GOM Mathematics measures, three different models of estimating item difficulty were compared: 1) the Classical Test Theory (CTT) Model, 2) the Rasch Model (1 PL model), and 3) the Two-parameter logistic model (2PL model).

*CTT model.* The authors calculated the  $p$ -value or “proportion passing” of all valid responses. The  $p$ -value is the estimate of item difficulty of each item under Classical Test Theory (CTT) (Embretson & Reise, 2000). In this study, the authors calculated the percentage of valid responses that were correct. For example, there were 206 seventh grade students assigned to take the GOM Mathematics measures. For Item 10 in Grade 7, twenty of the students did not answer the question; 93 of the students gave the correct answer and 93 of students gave an incorrect answer. The  $p$ -value of Item 10 in the Grade 7 measure is .5 ( $93 \div 186 = .5$ ).

The results indicated that the Grade 3 measures had the narrowest range (.63 - .88) of  $p$ -value and Grade 5 had the widest range (.05 - .77). The  $p$ -value of items for Grades 3-8 is shown in Appendix B. However, the  $p$ -values were not optimal estimates of respondents’ trait levels, because the estimates of item difficulties under the CTT model are “population dependent.” In other words, given the same items, the more skillful group will have lower estimates of item difficulties, whereas the less skillful group will have higher estimates of item difficulties (Embretson & Reise, 2000).

*IRT models.* The goal of assessment is exact estimation of the students’ abilities. However, under the CTT model, the same item could be considered an easy or a difficult one according to the characteristics of the examinees’ group. To the contrary, IRT provides both invariant item statistics and ability estimates. That is, there is no difference between item parameter estimates even though the data from two groups which have different characteristics

are analyzed. In IRT, we can estimate the examinee's ability regardless of the difficulty of the test.

In this context, the authors opted to use the IRT model to obtain the estimates of item difficulties and respondents' trait levels. Specifically, in the CTT model, the true scores only applied to a specific set of items or their equivalent; item difficulty is influenced by the respondents' overall skill levels; the item difficulty and respondent's trait levels could not be estimated separately (Embretson & Reise, 2000).

*Rasch model.* The Rasch model predicts the probability of respondents' giving correct responses from two independent variables (a respondent's trait level and an item difficulty). IRT models place the trait level and item difficulty at the same scale. When the item difficulty matches the trait level, the respondent has a 50-50 chance to answer that item correctly.

IRT models require two basic assumptions. The first assumption is that the item characteristic curve specified by an IRT model must fit the test data. Under the Rasch model, the values of outfit mean squares of responses in all but the three problematic items (Grade 3, item 1; Grade 5, item 14; Grade 7, item 7) stay within the productive range (0.5 - 1.5) (see Appendices C and F). This implies that the Rasch model fit the test data fairly well. This first assumption is met.

The second assumption is local independence. Local independence means that item parameters and person parameters fully account for interrelationships between items and persons. No other factors will influence the interrelationship between items and persons. The authors did not find evidence of violation of the second assumption as suggested in Yen's (1993) examples. Yen suggested local dependence could occur when (1) the respondent's speed is a factor in their performance, (2) there is differential exposure of the test items (e.g. unfamiliar vocabulary for

English language learners) or (3) the test items are chained together (so that answering one item influences the answers of other items). GOM Mathematics measures are not timed tests. The test items were not chained together. However we did not gather information about the participants' disability, English language learning, and SES status. We did not know whether these extraneous factors would play into the interaction of persons and items. So the second assumption is tentatively assumed not violated.

When the two required assumptions of IRT models are met and items are calibrated appropriately following the IRT calibration procedures, “item invariance” and “person invariance” under the chosen IRT model can be assumed (Embretson & Reise, 2000). “Item invariance” means that, when items were calibrated appropriately, the person's trait level can remain stable, regardless of which items from the item bank were given. “Person invariance” means that the item difficulty will remain unchanged, independent of the respondents' ability levels. Because of “item invariance” and “person invariance,” the comparison across persons with different trait levels using different subtests from the same well-calibrated item bank, under an appropriate IRT model, is meaningful. That is a significant advantage of using IRT models over CTT models to estimate item difficulties.

Under the IRT models, the item difficulties and participants' trait levels (abilities) were placed on the same scale. The items provide the most informative estimates on the respondents' trait levels when items are “on target,” or the distance between the person's estimated trait level and item difficulty of the selected item was short. When the items were “on target,” the measurement errors were relatively small. Therefore, the estimates were more accurate than the extreme scores. Providing items with a wide range of item difficulty increased the likelihood of having items that are on target for respondents' trait levels.

According to the WINSTEPS Help Manual, the items that have outfit means squares between .5 and 1.5 are considered productive measurement, because they generated predictable response patterns in which the students who gave correct answers were more skillful than their counterparts were. The value of outfit mean squares exceeding 2.0 means that “off-variable noises are greater than useful information.” The measurement can be degraded. The value of outfit mean squares between 1.5 and 2.0 means there is noticeable off-variable noises. Although it does not necessarily degrade the measurement, it did not construct the measurement either.

In the GOM Mathematics, all but three test items are considered “productive measurements.” Two items (Grade 5, item 14; and Grade 7, item 7) had the value of outfit mean squares exceeding 1.5; one item (Grade 3, item 1) had the value of outfit mean square exceeding 2.0. The first problematic item in the Grade 3 measure was an addition problem with regrouping. ( $483 + 371 = \underline{\hspace{2cm}}$ ). The question was presented in the column format. The value of outfit mean square exceeds 2.0 suggesting that off-variable noises are greater than useful information. The statistics in the item analysis (Appendix F) indicated that there were 192 students (88% of sample population) who chose the correct answer. The variance of trait levels of the students who answered correctly was narrow (Standard error mean for the trait level for students who chose the correct answer was 1.14). There were 25 students (12% of sample population) choosing distractors. The variances of trait levels between these 25 students were wide (Standard error means of trait level for the students who chose these three distractors were 7.78, 5.70 and 5.53). The item analysis suggested there is an unstable or unpredictable response pattern that was associated with this test item. While the overwhelming majority (88% of the students) answered the question correctly, some very skillful respondents unexpectedly missed this relatively easy question.

The second problematic item was Item 14 of the Grade 5 measures ( $14.26 \div .2 = \underline{\hspace{1cm}}$ ). The problem was presented in the column format. The trait level of the 47 students who chose the correct response (71.3) was 40.93 (with standard error mean of the average measure being 1.28); the trait level of the 122 students who chose the most popular distractor (7.13) was 40.12 (with standard error mean of average measures being .92). There was no significant difference in terms of ability between these two groups. Given the distractors, this response pattern suggested that the fifth grade sample population as a group had not been firm on how to determine the location of the decimal point in the division problem (Appendix F). Even though the outfit mean square of this item exceeds 1.5, the authors recommend keeping this item in the item bank.

The third and last problematic item was Item 7 of the Grade 7 measures ( $(-8000) - (-4264) = \underline{\hspace{1cm}}$ ). The item was presented as shown. Thirty five percent of students answered the problem correctly. The incorrect responses were distributed relatively evenly among the three distractors. There is no significant group difference in trait levels between the students choosing distractors (Appendix F). This might suggest some off-variable noises in place for this item, but the “noises” did not degrade this test item. The students who answered correctly had higher trait levels than the students who answered incorrectly. As explained in the Discussion section, the author recommended keeping this item in the item bank.

In inspecting the functionality of the items, the authors considered not only the predictability of the response patterns, but also the range of item difficulties. If the range of item difficulties is narrow, then the measure is less likely to receive “on-target” responses from the students whose trait levels are outside of the range. The data analysis indicated that the Grade 3 measures had the narrowest range of estimates of item difficulties under the Rasch Model; the

Grade 5 measures had the widest range of estimates of item difficulties. However, the authors advised against comparing estimates of item difficulty across the grade levels because no proper vertical scaling procedure was included in the item writing phase.

With the exception of three problematic items, all items in the GOM Mathematics measures are considered productive measures. The data fit the Rasch model well; the raw score is a sufficient estimate of students' scale score.

*Two-parameter logistic model.* The authors obtained the estimates of item difficulty and item discrimination for each item under the 2PL model using BILOG-MG software. The scores files under the 2PL model generated by BILOG-MG can be found in Appendix D. The scores files reported the minimum and maximum of the scale scores as well as the minimum and maximum of the standard errors of scale scores. They also report the distribution of scores across different scores brackets. When there is only one case within a particular score bracket, the minimum and maximum of scale scores are identical. The standard errors of the extreme scores are larger than the standard errors of average scores.

Appendix E is the parameter files under the 2PL model. The parameter files reported the intercepts, slopes and item difficulty for each test item as well as the standard errors of the intercepts, slopes and item difficulty.

We do not report the scores files and parameter scores for the Grade 7 measures because the data would not converge. Inspecting the distribution of the scores for the measures in Grades 3, 4, 5, 6 and 8, we found the distributions were normal with the exception of the Grade 3 measure.

The authors inspected the scale scores and item characteristics of each item. The Rasch model constrains the slopes to be identical (slope = 1) for all items. The 2PL models tested the



assumption of the Rasch model. The review of parameter models in Appendix E indicated that the Rasch assumption was not true; there were variances among slopes. For example, two test items in Grade 4 measures had very steep slopes. The score files under the 2PL model attempt to give more precise estimates of scale scores via raw scores.

The estimated scale scores and standard errors of scale scores vary depending on which items the examinee answered correctly. For example, 184 students took the Grade 8 measure. Thirty of the examinees answered eight of the fifteen test items correctly. Under the CTT model, these students would receive identical scores (i.e., the p-value, 53.33% correct). Under the 1PL model, although the likelihood of students answering each item correctly varies, the students' raw scores were used as the robust indicators of scale scores. These 30 students would receive similar scale scores. However, under the 2PL model, these students' scale scores falls within the range of .02 and .81 with the standard errors between .59 and .71. The variance in the scale scores is rooted in the different answer patterns. The person who missed the easier half and the person who missed the more difficult half of the questions would have two very different scale scores. Moreover, the students with average skill levels who missed a very simple question could render a less stable pattern and, therefore, the standard errors of his or her scale score would be larger than the examinees who have predictable response patterns. The estimates under the 2PL model are more useful than the single scores provided under the 1PL model.

### *Final Item Selection*

Finally, for each grade 10 items out of 15 were selected. We tried to represent a range of difficulty levels and a range of content covered. In instances where items did not fit into the difficulty range specified, a balance between easy, medium, and difficult items was attempted. Final items' specific task type and item difficulty level were specified in Table 3 below.

Table 3.

Specific task type and item difficulty for final grade 3 measure.

| Item number | Item difficulty level | Specific task type   |
|-------------|-----------------------|--|
| 2           | -2.01                 | - Adding two three-digit numbers with renaming from ones to tens and tens to hundreds  |
| 12          | -1.23                 | - One-digit factor times two-digit factor (problems written horizontally)  |
| 4           | -0.95                 | - Adding four numbers with renaming from ones to tens and from tens to hundreds (sums of columns below 20)                             |
| 14          | -0.91                 | - Two-digit dividend; one-digit divisor; one-digit quotient; no remainder  |
| 10          | -0.87                 | - One-digit factor times two-digit factor with no carrying   |
| 9           | -0.64                 | - Subtracting a three-digit number from a four-digit number with renaming from thousands to hundreds                                   |
| 8           | -0.60                 | - Subtracting a four-digit number from a four-digit number with renaming from thousands to hundreds                                    |
| 7           | -0.59                 | - Subtracting a three-digit number from a three-digit number, zero in tens column with renaming from tens to ones and hundreds to tens |
| 6           | -0.41                 | - Subtracting a three-digit number from a three-digit number with renaming from tens to ones and hundreds to tens                      |
| 13          | -0.24                 | - Two-digit dividend; one-digit divisor; one-digit quotient; no remainder  |

Table 4.

Specific task type and item difficulty for final grade 4 measure.

| Item number | Item difficulty level | Specific task type  |
|-------------|-----------------------|---|
| 2           | -1.89                 | - Three-digit factor times one-digit factor with zero in tens column  |
| 3           | -0.28                 | - Three-digit factor times one-digit factor with horizontal alignment |
| 8           | -0.10                 | - Adding fractions with like denominators                             |
| 9           | 0.63                  | - Adding fractions with like denominators                             |
| 12          | 0.78                  | -Adding tenths, hundredths and whole number                           |
| 5           | 1.06                  | - Three-digit dividend; one-digit divisor; remainder                  |
| 7           | 1.55                  | -Two-digit dividend; one-digit divisor; two-digit quotient; remainder |
| 11          | 1.96                  | -Subtracting fractions with like denominators                         |
| 14          | 1.96                  | - Subtracting tenths from whole number                                |
| 15          | 2.67                  | - Subtracting hundredths from whole number                            |

Table 5.

Specific task type and item difficulty for final grade 5 measure.

| Item number | Item difficulty level | Specific task type  |
|-------------|-----------------------|---|
| 11          | -1.99                 | - Multiplying decimals; one-digit factor times three-digit factor               |
| 1           | -0.67                 | - Two-digit divisor; one-digit quotient   |
| 12          | -0.12                 | - Whole number divisor; no remainder  |
| 15          | 0.06                  | - Multiplying decimals; zero to be placed after decimal point                   |
| 3           | 0.30                  | - Two-digit divisor; two-digit quotient   |
| 9           | 0.37                  | - Subtracting fractions with mixed numbers                                      |
| 13          | 1.12                  | - Divisor is decimal; adding zeros in dividend required                         |
| 8           | 1.70                  | - Subtracting mixed numbers from whole number                                   |
| 10          | 2.60                  | - Subtracting fractions with different denominators, mixed numbers and reducing |
| 5           | 3.25                  | - Adding two fractions with different denominators                              |

Table 6.

Specific task type and item difficulty for final grade 6 measure.

| Item number | Item difficulty level | Specific task type  |
|-------------|-----------------------|---|
| 13          | -3.06                 | - Whole number divisor; zeros must be added to dividend after decimal point |
| 14          | -1.73                 | - Whole number divisor; zeros must be added to dividend after decimal point |
| 10          | -0.76                 | - Multiplying decimals; two digit factor times three digit factor           |
| 7           | -0.01                 | - Dividing mixed numbers by whole numbers                                   |
| 11          | 0.15                  | - Dividing decimals by whole number; quotient begins with zero              |
| 3           | 0.41                  | - Dividing fractions  |
| 15          | 0.85                  | - Whole number divisor; zeros must be added to dividend after decimal point |
| 6           | 1.15                  | - Dividing fractions by whole numbers                                       |
| 1           | 1.77                  | - Multiplying mixed numbers   |
| 12          | 2.02                  | - Dividing decimals by whole number; quotient begins with zero              |

Table 7.

Specific task type and item difficulty for final grade 7 measure.

| Item number | Item difficulty level | Specific task type  |
|-------------|-----------------------|---|
| 1           | 0.72                  | - Adding integers; two three-digit numbers  |
| 3           | 0.73                  | - Adding integers; four numbers   |
| 13          | 0.94                  | - Dividing integers: three-digit dividend; three-digit quotient   |
| 12          | 0.98                  | - Multiplying integers: three-digit factor times three-digit factor; zero in tens factor column of multiplier |
| 15          | 0.98                  | - Dividing integers: two-digit divisor; one digit quotient  |
| 6           | 1.02                  | - Subtracting integers; two-digit number from a three-digit number  |
| 4           | 1.09                  | - Adding integers; four-digit numbers   |
| 11          | 1.09                  | - Multiplying integers: three-digit factor times three-digit factor   |
| 10          | 1.18                  | - Multiplying integers: two-digit factor times three-digit factor   |
| 8           | 1.34                  | - Subtracting integers: two-digit number from a three-digit number, zero in tens column                       |

*Note.* Item difficulty levels for grade 7 measure were from Winsteps measure values.

Table 8.

Specific task type and item difficulty for final grade 8 measure.

| Item number | Item difficulty level | Specific task type  |
|-------------|-----------------------|---|
| 5           | -2.70                 | - Adding hundredths and tenths                                      |
| 3           | -1.09                 | - Three-digit factor times three-digit factor                       |
| 8           | -0.78                 | - Whole number divisor; no remainder                                |
| 15          | 0.30                  | - Four-digit dividend; two-digit divisor; three-digit quotient      |
| 14          | 0.54                  | - Multiplication with three integers                                |
| 9           | 0.74                  | - Adding three fractions with different denominators                |
| 7           | 1.05                  | - Multiplying decimals; three-digit factor times three-digit factor |
| 10          | 1.14                  | - Subtracting mixed number from whole number                        |
| 11          | 1.49                  | - Mixed number times whole number                                   |
| 12          | 1.63                  | - Dividing fractions  |

### *Discussion*

The GOM Mathematics is a set of M-CBM measures to assess computation proficiency for students in grades 3 to 8. Fifteen items per grade were developed and each item was a multiple-choice question with one correct answer and three distracters. The authors compared three different models of analyzing students' response patterns on pilot testing. The CTT model provided the narrowest (Grade 3) and the widest (Grade 5) range of p-value. However, considering that the CTT model is population dependent, the authors additionally selected IRT models for this pilot testing analysis. The Rasch model analysis found that all items, except three problematic items (Grade 3, item 1; Grade 5, item 14; Grade 7, item 7), were appropriate items for each grade level. Finally, the authors examined the estimates of item difficulty and item discrimination under the 2PL model. Based on a range of difficulty levels and a range of content coverage, for each grade 10 items out of the initial 15 items were selected.



### References

- Deno, S. L. (1985). Curriculum-based measurement: The emerging alternative. *Exceptional Children*, 52, 219-232.
- Emberson, S. E., & Reise, S.P. (2000). The new rules of measurement. *Item Response Theory for Psychologists*. Mahwah, NJ : Lawrence Erlbaum Associates.
- Shinn, M. R. (1989). *Curriculum-based measurement: Assessing special children*. New York: Guilford.
- Shinn, M. R. (Ed.). (1998). *Advanced applications of curriculum-based measurement*. New York: Guilford.
- Stecker, P. M., & Fuchs, L. S. (2000). Effecting superior achievement using curriculum-based measurement: The importance of individual progress monitoring. *Learning Disabilities Research and Practice*, 15 (3), 128-134.
- Stein, M., Silbert, J., & Carnine, D. (1997), *Designing Effective Mathematics Instruction: A direct instruction approach*. Columbus, OH: Merrill.
- Thurber, R. S., Shinn, M. R., & Smolkowski, K. (2002). What is measured in mathematics test? Construct validity of curriculum-based mathematics measures. *School Psychology Review*, 31, 498-513.
- Tindal, G., Marston, D., & Deno, S. (1983). The reliability of direct and repeated measurement (Research Report No. 109). Minneapolis, MN: University of Minnesota Institute for Research on Learning Disabilities.
- Yen, W. M. (1993). Scaling performance assessments: Strategies for managing local item dependence. *Journal of Educational Measurement*, 30, 187-213.

## Appendix A: Directions for Administration

### Project INFORM Directions for Administration

My name is \_\_\_\_\_. Today we are going to work with you in mathematics and reading. You will work on the computer to complete the tasks.

Please your very best job on the reading problems and mathematics problems. Sometimes you will be asked to read some sentences or some paragraphs. Please make sure you read every word on the sentences or paragraphs. I know it might be tempting to NOT read the sentences or paragraphs, but we really want to make sure you read all of the words. Sometimes you will be asked questions about the reading that you do, so please do your best reading.

To solve the mathematics problems, you will have scratch paper and a pencil to use.

Each of you will have a different set of tasks so it is very important to FOLLOW DIRECTIONS. Some of you might have some more stories and fewer mathematics problems or more mathematics problems and fewer stories. So it doesn't matter who finishes first.

When you finish, please raise your hand and we will excuse you.

Is everyone ready? Does anyone have any questions? [wait for questions]

When we excuse you to the computers, please find your teacher's name on the list. Then find your name on the list. **DO NOT GO ON UNTIL WE HAVE CHECKED TO MAKE SURE YOU HAVE ALL OF THE CORRECT INFORMATION.**

Are you ready? [excuse students one at a time; helper will help them get set up on the computer]

What do you do first? *Find your teacher's name, then your name.*

What do you do after you have selected your name? *Wait for the teacher.*

What do you do when you're finished? *Raise your hand.*

#### Appendix B: Estimates of item difficulty under Classical Test Theory (CTT) model

“Valid Percent” is the percentage of valid response that is the correct answer. The valid percent is the estimates of item difficulty under the CTT model. The estimates under the CTT model are “population dependent.” The “valid percent” gathered from a more skilled group is usually higher than the valid percent gathered from a less skill group.

Table B1.  
Estimates of item difficulty for grade 3.

| <b>Measure</b>       | <b>1</b> | <b>2</b> | <b>3</b> | <b>4</b> | <b>5</b> | <b>6</b> | <b>7</b> | <b>8</b> | <b>9</b> | <b>10</b> | <b>11</b> | <b>12</b> | <b>13</b> | <b>14</b> | <b>15</b> |
|----------------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-----------|-----------|-----------|-----------|-----------|-----------|
| <b>Correct</b>       | 192      | 181      | 175      | 154      | 140      | 139      | 147      | 149      | 149      | 158       | 141       | 155       | 136       | 142       | 141       |
| <b>Incorrect</b>     | 25       | 36       | 42       | 63       | 77       | 78       | 70       | 68       | 68       | 59        | 76        | 62        | 81        | 75        | 76        |
| <b>Valid</b>         | 217      | 217      | 217      | 217      | 217      | 217      | 217      | 217      | 217      | 217       | 217       | 217       | 217       | 217       | 217       |
| <b>Missing</b>       | 22       | 22       | 22       | 22       | 22       | 22       | 22       | 22       | 22       | 22        | 22        | 22        | 22        | 22        | 22        |
| <b>Valid percent</b> | .88      | .83      | .81      | .71      | .65      | .64      | .68      | .69      | .69      | .73       | .65       | .71       | .63       | .65       | .65       |

Table B2.  
Estimates of item difficulty for grade 4.

| <b>Measure</b>       | <b>1</b> | <b>2</b> | <b>3</b> | <b>4</b> | <b>5</b> | <b>6</b> | <b>7</b> | <b>8</b> | <b>9</b> | <b>10</b> | <b>11</b> | <b>12</b> | <b>13</b> | <b>14</b> | <b>15</b> |
|----------------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-----------|-----------|-----------|-----------|-----------|-----------|
| <b>Correct</b>       | 123      | 133      | 114      | 59       | 83       | 75       | 63       | 53       | 63       | 31        | 42        | 81        | 64        | 55        | 127       |
| <b>Incorrect</b>     | 47       | 37       | 56       | 111      | 87       | 95       | 107      | 117      | 107      | 139       | 128       | 89        | 10        | 89        | 43        |
| <b>Valid</b>         | 170      | 170      | 170      | 170      | 170      | 170      | 170      | 170      | 170      | 170       | 170       | 170       | 170       | 144       | 170       |
| <b>Missing</b>       | 15       | 15       | 15       | 15       | 15       | 15       | 15       | 15       | 15       | 15        | 15        | 15        | 15        | 41        | 15        |
| <b>Valid percent</b> | .72      | .78      | .67      | .35      | .49      | .44      | .37      | .31      | .37      | .23       | .25       | .48       | .38       | .38       | .25       |

Table B3.  
Estimates of item difficulty for grade 5.

| Measure       | 1   | 2   | 3   | 4   | 5   | 6   | 7   | 8   | 9   | 10  | 11  | 12  | 13  | 14  | 15  |
|---------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| Correct       | 160 | 153 | 117 | 81  | 14  | 13  | 28  | 69  | 114 | 24  | 181 | 131 | 85  | 47  | 80  |
| Incorrect     | 95  | 102 | 138 | 174 | 241 | 242 | 227 | 186 | 141 | 231 | 74  | 124 | 170 | 208 | 175 |
| Valid         | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| Missing       | 18  | 18  | 18  | 18  | 18  | 18  | 18  | 18  | 18  | 18  | 18  | 18  | 18  | 18  | 18  |
| Valid percent | .63 | .60 | .46 | .32 | .05 | .05 | .11 | .27 | .45 | .09 | .71 | .51 | .33 | .18 | .31 |

Table B4.  
Estimates of item difficulty for grade 6.

| Measure       | 1   | 2   | 3   | 4   | 5   | 6   | 7   | 8   | 9   | 10  | 11  | 12  | 13  | 14  | 15  |
|---------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| Correct       | 25  | 30  | 69  | 33  | 70  | 57  | 88  | 76  | 99  | 99  | 67  | 64  | 128 | 138 | 63  |
| Incorrect     | 141 | 136 | 97  | 133 | 96  | 109 | 78  | 90  | 67  | 67  | 99  | 102 | 38  | 28  | 103 |
| Valid         | 166 | 166 | 166 | 166 | 166 | 166 | 166 | 166 | 166 | 166 | 166 | 166 | 166 | 166 | 166 |
| Missing       | 37  | 37  | 37  | 37  | 37  | 37  | 37  | 37  | 37  | 37  | 37  | 37  | 37  | 37  | 37  |
| Valid percent | .15 | .18 | .42 | .20 | .42 | .34 | .53 | .46 | .60 | .60 | .40 | .39 | .77 | .83 | .38 |

Table B5.  
Estimates of item difficulty for grade 7.

| Measure       | 1   | 2   | 3   | 4   | 5   | 6   | 7   | 8   | 9   | 10  | 11  | 12  | 13  | 14  | 15  |
|---------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| Correct       | 114 | 96  | 98  | 78  | 55  | 63  | 83  | 48  | 78  | 93  | 79  | 84  | 83  | 91  | 115 |
| Incorrect     | 72  | 90  | 88  | 108 | 131 | 123 | 103 | 138 | 108 | 93  | 107 | 101 | 102 | 94  | 70  |
| Valid         | 186 | 186 | 186 | 186 | 186 | 186 | 186 | 186 | 186 | 186 | 186 | 185 | 185 | 185 | 185 |
| Missing       | 20  | 20  | 20  | 20  | 20  | 20  | 20  | 20  | 20  | 20  | 20  | 21  | 21  | 21  | 21  |
| Valid percent | .61 | .52 | .53 | .42 | .30 | .34 | .45 | .26 | .42 | .50 | .42 | .45 | .45 | .51 | .38 |

Table B6.  
Estimates of item difficulty for grade 8.

| Measure       | 1   | 2   | 3   | 4   | 5   | 6   | 7   | 8   | 9   | 10  | 11  | 12  | 13  | 14  | 15  |
|---------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| Correct       | 158 | 149 | 125 | 76  | 147 | 123 | 65  | 109 | 62  | 53  | 49  | 55  | 60  | 70  | 82  |
| Incorrect     | 26  | 35  | 59  | 108 | 37  | 61  | 119 | 74  | 122 | 131 | 134 | 128 | 122 | 112 | 100 |
| Valid         | 184 | 184 | 184 | 184 | 184 | 184 | 184 | 183 | 184 | 184 | 183 | 183 | 182 | 182 | 182 |
| Missing       | 28  | 28  | 28  | 28  | 28  | 28  | 28  | 29  | 28  | 28  | 29  | 29  | 30  | 30  | 30  |
| Valid percent | .86 | .81 | .68 | .41 | .80 | .67 | .35 | .60 | .34 | .29 | .27 | .30 | .33 | .38 | .45 |

## Appendix C: Estimates of Item Difficulty Under Rasch Model

Table C1.  
Estimates of item difficulty for grade 3.

| <b>Entry</b> | <b>Measure</b> | <b>Count</b> | <b>Score</b> | <b>OUT.MSQ</b> | <b>OUT.ZSTD</b> | <b>PTME</b> | <b>OBSMATCH</b> | <b>EXPMATCH</b> |
|--------------|----------------|--------------|--------------|----------------|-----------------|-------------|-----------------|-----------------|
| <b>1</b>     | 34.77          | 180          | 156          | 2.36           | 3.14            | 0.3         | 87.80           | 87.10           |
| <b>2</b>     | 40.23          | 180          | 145          | 1.48           | 1.81            | 0.39        | 80.60           | 82.10           |
| <b>3</b>     | 42.73          | 180          | 139          | 1.08           | 0.45            | 0.44        | 82.20           | 79.60           |
| <b>4</b>     | 50.17          | 180          | 118          | 1.18           | 1.28            | 0.48        | 69.40           | 74.60           |
| <b>5</b>     | 54.53          | 180          | 104          | 1.03           | 0.33            | 0.55        | 71.70           | 72.80           |
| <b>6</b>     | 54.84          | 180          | 103          | 0.78           | -2.10           | 0.66        | 82.20           | 72.70           |
| <b>7</b>     | 52.38          | 180          | 111          | 0.82           | -1.46           | 0.62        | 80.00           | 73.50           |
| <b>8</b>     | 51.76          | 180          | 113          | 0.73           | -2.28           | 0.64        | 81.10           | 73.60           |
| <b>9</b>     | 51.76          | 180          | 113          | 0.81           | -1.53           | 0.62        | 80.00           | 73.60           |
| <b>10</b>    | 48.86          | 180          | 122          | 0.89           | -0.72           | 0.56        | 77.20           | 75.20           |
| <b>11</b>    | 54.23          | 180          | 105          | 1.20           | 1.67            | 0.49        | 66.70           | 72.90           |
| <b>12</b>    | 49.84          | 180          | 119          | 1.41           | 2.60            | 0.41        | 65.60           | 74.70           |
| <b>13</b>    | 55.74          | 180          | 100          | 1.18           | 1.58            | 0.53        | 69.40           | 72.50           |
| <b>14</b>    | 53.92          | 180          | 106          | 0.77           | -2.14           | 0.64        | 77.20           | 73.00           |
| <b>15</b>    | 54.23          | 180          | 105          | 0.90           | -0.87           | 0.58        | 73.30           | 72.90           |

Table C2.  
Estimates of item difficulty for grade 4.

| Entry | Measure | Count | Score | OUT.MSQ | OUT.ZSTD | PTME | OBSMATCH | EXPMATCH |
|-------|---------|-------|-------|---------|----------|------|----------|----------|
| 1     | 34.85   | 169   | 122   | 1.21    | 1.41     | 0.3  | 75.7     | 74.7     |
| 2     | 31.18   | 169   | 132   | 0.78    | -1.24    | 0.43 | 82.2     | 79.2     |
| 3     | 37.79   | 169   | 113   | 0.87    | -1.04    | 0.44 | 74.0     | 71.3     |
| 4     | 53.93   | 169   | 58    | 1.02    | 0.19     | 0.39 | 71.0     | 71.9     |
| 5     | 46.85   | 169   | 82    | 0.92    | -1.00    | 0.46 | 69.8     | 67.2     |
| 6     | 49.14   | 169   | 74    | 1.17    | 1.86     | 0.32 | 58.6     | 67.8     |
| 7     | 52.69   | 169   | 62    | 0.92    | -0.77    | 0.43 | 67.5     | 70.6     |
| 8     | 55.86   | 169   | 52    | 0.78    | -1.87    | 0.56 | 82.2     | 73.9     |
| 9     | 52.69   | 169   | 62    | 0.94    | -0.5     | 0.48 | 73.4     | 70.6     |
| 10    | 60.91   | 169   | 38    | 1.08    | 0.52     | 0.41 | 81.7     | 79.4     |
| 11    | 59.75   | 169   | 41    | 1.10    | 0.65     | 0.39 | 79.9     | 78.2     |
| 12    | 47.42   | 169   | 80    | 1.13    | 1.51     | 0.31 | 60.4     | 67.3     |
| 13    | 52.38   | 169   | 63    | 1.12    | 1.12     | 0.39 | 72.8     | 70.3     |
| 14    | 55.21   | 169   | 54    | 1.11    | 0.91     | 0.36 | 71.6     | 73.1     |
| 15    | 59.37   | 169   | 42    | 1.13    | 0.81     | 0.27 | 69.8     | 77.8     |



Table C3.  
Estimates of item difficulty for grade 5.

| Entry | Measure | Count | Score | OUT.MSQ | OUT.ZSTD | PTME | OBSMATCH | EXPMATCH |
|-------|---------|-------|-------|---------|----------|------|----------|----------|
| 1     | 33.52   | 254   | 160   | 0.93    | -0.73    | 0.42 | 68.9     | 69.4     |
| 2     | 34.89   | 254   | 153   | 1.05    | 0.6      | 0.46 | 70.9     | 68.3     |
| 3     | 41.67   | 254   | 117   | 0.91    | -1.28    | 0.48 | 72.4     | 66.6     |
| 4     | 48.76   | 254   | 81    | 0.81    | -2.02    | 0.49 | 74.8     | 72.5     |
| 5     | 72.26   | 254   | 14    | 0.78    | -0.48    | 0.32 | 94.9     | 94.5     |
| 6     | 73.10   | 254   | 13    | 0.66    | -0.82    | 0.3  | 95.3     | 94.9     |
| 7     | 63.99   | 254   | 28    | 0.92    | -0.23    | 0.32 | 90.2     | 89.3     |
| 8     | 51.42   | 254   | 69    | 0.97    | -0.18    | 0.42 | 76.4     | 75.2     |
| 9     | 42.23   | 254   | 114   | 0.96    | -0.49    | 0.42 | 66.5     | 66.9     |
| 10    | 65.9    | 254   | 24    | 1.15    | 0.6      | 0.28 | 91.7     | 90.8     |
| 11    | 29.13   | 254   | 181   | 1.1     | 0.91     | 0.27 | 70.1     | 74.1     |
| 12    | 39.05   | 254   | 131   | 1.1     | 1.43     | 0.36 | 66.1     | 66.2     |
| 13    | 47.92   | 254   | 85    | 0.97    | -0.34    | 0.38 | 69.3     | 71.5     |
| 14    | 57.15   | 254   | 47    | 1.59    | 3.08     | 0.06 | 79.1     | 82.4     |
| 15    | 48.98   | 254   | 80    | 1.17    | 1.64     | 0.23 | 67.3     | 72.7     |

Table C4.  
Estimates of item difficulty for grade 6.

| Entry | Measure | Count | Score | OUT.MSQ | OUT.ZSTD | PTME | OBSMATCH | EXPMATCH |
|-------|---------|-------|-------|---------|----------|------|----------|----------|
| 1     | 67.33   | 163   | 24    | 0.84    | -0.65    | 0.38 | 84.70    | 85.90    |
| 2     | 64.79   | 163   | 29    | 0.83    | -0.86    | 0.43 | 84.70    | 83.20    |
| 3     | 51.06   | 163   | 68    | 0.97    | -0.32    | 0.40 | 69.30    | 66.30    |
| 4     | 63.41   | 163   | 32    | 0.97    | -0.08    | 0.37 | 81.60    | 81.60    |
| 5     | 50.77   | 163   | 69    | 1.09    | 1.09     | 0.31 | 63.80    | 66.20    |
| 6     | 54.68   | 163   | 56    | 1.12    | 1.16     | 0.29 | 66.30    | 70.10    |
| 7     | 45.64   | 163   | 87    | 0.93    | -0.86    | 0.42 | 64.40    | 65.10    |
| 8     | 49.05   | 163   | 75    | 1.08    | 1.02     | 0.33 | 63.80    | 65.20    |
| 9     | 42.47   | 163   | 98    | 0.95    | -0.55    | 0.40 | 71.20    | 67.10    |
| 10    | 42.47   | 163   | 98    | 0.96    | -0.39    | 0.39 | 67.50    | 67.10    |
| 11    | 51.65   | 163   | 66    | 0.94    | -0.70    | 0.40 | 64.40    | 66.60    |
| 12    | 52.54   | 163   | 63    | 0.98    | -0.23    | 0.39 | 68.10    | 67.60    |
| 13    | 32.86   | 163   | 127   | 1.88    | 4.00     | 0.18 | 76.70    | 78.20    |
| 14    | 28.44   | 163   | 137   | 0.80    | -0.87    | 0.42 | 85.30    | 84.10    |
| 15    | 52.84   | 163   | 62    | 1.01    | 0.15     | 0.35 | 65.00    | 68.00    |

Table C5.  
Estimates of item difficulty for grade 7.

| Entry | Measure | Count | Score | OUT.MSQ | OUT.ZSTD | PTME | OBSMATCH | EXPMA<br>TCH |
|-------|---------|-------|-------|---------|----------|------|----------|--------------|
| 1     | 39.89   | 178   | 107   | 0.72    | -2       | 0.57 | 79.8     | 71.1         |
| 2     | 45.27   | 178   | 89    | 0.68    | -2.84    | 0.64 | 82       | 71           |
| 3     | 44.67   | 178   | 91    | 0.73    | -2.28    | 0.61 | 77.5     | 70.9         |
| 4     | 50.78   | 178   | 71    | 1.09    | 0.74     | 0.5  | 68.5     | 73.9         |
| 5     | 58.76   | 178   | 48    | 1.18    | 0.99     | 0.57 | 84.3     | 79.9         |
| 6     | 55.79   | 178   | 56    | 1.02    | 0.18     | 0.56 | 81.5     | 77.8         |
| 7     | 49.21   | 178   | 76    | 1.63    | 4.29     | 0.33 | 60.1     | 72.8         |
| 8     | 61.61   | 178   | 41    | 1.34    | 1.49     | 0.51 | 80.3     | 81.8         |
| 9     | 50.78   | 178   | 71    | 0.9     | -0.76    | 0.56 | 76.4     | 73.9         |
| 10    | 46.17   | 178   | 86    | 1.18    | 1.4      | 0.47 | 69.7     | 71.3         |
| 11    | 50.46   | 178   | 72    | 1.09    | 0.74     | 0.52 | 74.7     | 73.7         |
| 12    | 48.72   | 177   | 77    | 0.98    | -0.11    | 0.53 | 71.2     | 72.4         |
| 13    | 49.03   | 177   | 76    | 0.94    | -0.41    | 0.54 | 74       | 72.7         |
| 14    | 45.67   | 177   | 87    | 1       | 0.08     | 0.52 | 70.6     | 71           |
| 15    | 53.22   | 177   | 63    | 0.98    | -0.08    | 0.55 | 78       | 75.9         |

Table C6.  
Estimates of item difficulty for grade 8.

| <b>Entry</b> | <b>Measure</b> | <b>Count</b> | <b>Score</b> | <b>OUT.MSQ</b> | <b>OUT.ZSTD</b> | <b>PTME</b> | <b>OBSMATCH</b> | <b>EXPMATCH</b> |
|--------------|----------------|--------------|--------------|----------------|-----------------|-------------|-----------------|-----------------|
| <b>1</b>     | 29.37          | 183          | 157          | 1.34           | 1.29            | 0.26        | 86.3            | 86              |
| <b>2</b>     | 33.37          | 183          | 148          | 1.03           | 0.22            | 0.31        | 80.9            | 81.5            |
| <b>3</b>     | 41.45          | 183          | 124          | 1.00           | 0.05            | 0.38        | 72.7            | 71.5            |
| <b>4</b>     | 54.73          | 183          | 75           | 1.03           | 0.35            | 0.41        | 69.4            | 69.3            |
| <b>5</b>     | 34.15          | 183          | 146          | 0.86           | -0.70           | 0.35        | 79.8            | 80.6            |
| <b>6</b>     | 42.04          | 183          | 122          | 0.84           | -1.38           | 0.48        | 77              | 71              |
| <b>7</b>     | 57.82          | 183          | 64           | 1.05           | 0.46            | 0.37        | 68.3            | 71.9            |
| <b>8</b>     | 45.77          | 182          | 108          | 1.17           | 1.66            | 0.32        | 64.8            | 68.3            |
| <b>9</b>     | 58.69          | 183          | 61           | 0.86           | -1.31           | 0.48        | 73.2            | 72.6            |
| <b>10</b>    | 61.46          | 183          | 52           | 0.86           | -1.04           | 0.49        | 77              | 75.4            |
| <b>11</b>    | 62.60          | 182          | 48           | 1.23           | 1.52            | 0.3         | 73.1            | 76.5            |
| <b>12</b>    | 60.65          | 182          | 54           | 1.28           | 2.02            | 0.29        | 72              | 74.7            |
| <b>13</b>    | 59.01          | 181          | 59           | 0.96           | -0.30           | 0.42        | 74.6            | 73              |
| <b>14</b>    | 56.09          | 181          | 69           | 0.87           | -1.36           | 0.51        | 74.6            | 70.5            |
| <b>15</b>    | 52.79          | 181          | 81           | 0.98           | -0.18           | 0.44        | 71.8            | 67.9            |

## Appendix D: The Scores Files for Grades 3-8 Mathematics Measures under the 2PL model

Table D1.  
The score files for grade 3.

| Total items | Number of correct items | Proportion correct | Number of cases | Scale scores* |         | Standard errors of scale score * |         |
|-------------|-------------------------|--------------------|-----------------|---------------|---------|----------------------------------|---------|
|             |                         |                    |                 | Minimum       | Maximum | Minimum                          | Maximum |
| 15          | 15                      | 100                | 36              | 1.32          | 1.32    | 0.67                             | 0.67    |
| 15          | 14                      | 93.33              | 27              | 0.51          | 1.01    | 0.40                             | 0.60    |
| 15          | 13                      | 86.67              | 20              | 0.14          | 0.65    | 0.39                             | 0.46    |
| 15          | 12                      | 80                 | 27              | -0.27         | 0.48    | 0.37                             | 0.47    |
| 15          | 11                      | 73.33              | 14              | -0.35         | 0.28    | 0.30                             | 0.47    |
| 15          | 10                      | 66.67              | 19              | -0.49         | -0.25   | 0.13                             | 0.39    |
| 15          | 9                       | 60                 | 8               | -0.57         | -0.40   | 0.14                             | 0.30    |
| 15          | 8                       | 53.33              | 16              | -0.73         | -0.45   | 0.14                             | 0.42    |
| 15          | 7                       | 46.67              | 10              | -1.20         | -0.49   | 0.18                             | 0.46    |
| 15          | 6                       | 40                 | 12              | -1.35         | -0.52   | 0.24                             | 0.45    |
| 15          | 5                       | 33.33              | 13              | -1.42         | -1.06   | 0.24                             | 0.44    |
| 15          | 4                       | 26.67              | 7               | -1.51         | -1.37   | 0.24                             | 0.34    |
| 15          | 3                       | 20                 | 5               | -1.68         | -1.34   | 0.25                             | 0.45    |
| 15          | 2                       | 13.33              | 1               | -1.56         | -1.56   | 0.38                             | 0.38    |
| 15          | 1                       | 6.67               | 1               | -2.14         | -2.14   | 0.53                             | 0.53    |
| 15          | 0                       | 0                  | 1               | -2.51         | -2.51   | 0.57                             | 0.57    |

Table D2.  
The score files for grade 4.

| Total items | Number of correct items | Proportion correct | Number of cases | Scale scores* |         | Standard errors of scale score * |         |
|-------------|-------------------------|--------------------|-----------------|---------------|---------|----------------------------------|---------|
|             |                         |                    |                 | Minimum       | Maximum | Minimum                          | Maximum |
| 14          | 14                      | 100                | 1               | 2.80          | 2.80    | .67                              | .67     |
| 14          | 13                      | 92.86              | 1               | 2.10          | 2.10    | .61                              | .61     |
| 14          | 12                      | 85.71              | 3               | 1.85          | 2.31    | .58                              | .63     |
| 14          | 11                      | 78.57              | 8               | 1.65          | 2.04    | .55                              | .61     |
| 14          | 10                      | 71.43              | 8               | -.46          | 1.78    | .17                              | .57     |
| 14          | 9                       | 64.29              | 11              | -.48          | 1.57    | .14                              | .53     |
| 14          | 8                       | 57.14              | 18              | -.49          | 1.37    | .15                              | .52     |
| 14          | 7                       | 50                 | 20              | -.51          | 1.22    | .14                              | .52     |
| 14          | 6                       | 42.86              | 24              | -.54          | 1.13    | .16                              | .52     |
| 14          | 5                       | 35.71              | 32              | -.61          | .88     | .15                              | .49     |
| 14          | 4                       | 28.57              | 15              | -.70          | -.47    | .14                              | .44     |
| 14          | 3                       | 21.43              | 17              | -.85          | .54     | .14                              | .54     |
| 14          | 2                       | 14.29              | 10              | -1.06         | -.51    | .18                              | .64     |
| 14          | 1                       | 7.14               | 2               | -1.31         | -.53    | .23                              | .72     |
| 14          | 0                       | 0                  | 0               | --            | --      | --                               | --      |

*Note.* \* Scale scores and standard errors of scale scores vary depending on which questions are answered correctly. To show the range, the authors report the maximum and minimum of the scale scores and standard errors of scale scores.

Table D3.  
The score files for grade 5.

| Total items | Number of correct items | Proportion correct | Number of cases | Scale scores* |         | Standard errors of scale score * |         |
|-------------|-------------------------|--------------------|-----------------|---------------|---------|----------------------------------|---------|
|             |                         |                    |                 | Minimum       | Maximum | Minimum                          | Maximum |
| 14          | 14                      | 100                | 0               | --            | --      | --                               | --      |
| 14          | 13                      | 92.86              | 1               | 2.75          | 2.75    | .58                              | .58     |
| 14          | 12                      | 85.71              | 1               | 2.74          | 2.74    | .58                              | .58     |
| 14          | 11                      | 78.57              | 1               | 1.91          | 1.91    | .56                              | .56     |
| 14          | 10                      | 71.43              | 5               | 1.37          | 2.06    | .56                              | .56     |
| 14          | 9                       | 64.29              | 8               | 1.04          | 1.83    | .56                              | .59     |
| 14          | 8                       | 57.14              | 22              | .76           | 1.73    | .56                              | .61     |
| 14          | 7                       | 50                 | 19              | .47           | 1.28    | .57                              | .62     |
| 14          | 6                       | 42.86              | 30              | .12           | .89     | .60                              | .64     |
| 14          | 5                       | 35.71              | 54              | -.29          | .63     | .61                              | .67     |
| 14          | 4                       | 28.57              | 36              | -.63          | .37     | .62                              | .69     |
| 14          | 3                       | 21.43              | 44              | -1.00         | -.38    | .67                              | .71     |
| 14          | 2                       | 14.29              | 25              | -1.30         | -.79    | .70                              | .73     |
| 14          | 1                       | 7.14               | 6               | -1.51         | -1.32   | .74                              | .75     |
| 14          | 0                       | 0                  | 2               | -1.71         | 999.00  | .77                              | .77     |

Table D4.  
The score files for grade 6.

| Total items | Number of correct items | Proportion correct | Number of cases | Scale scores* |         | Standard errors of scale score * |         |
|-------------|-------------------------|--------------------|-----------------|---------------|---------|----------------------------------|---------|
|             |                         |                    |                 | Minimum       | Maximum | Minimum                          | Maximum |
| 15          | 15                      | 100                | 1               | 2.65          | 2.65    | 0.68                             | 0.68    |
| 15          | 14                      | 93.33              | 1               | 2.43          | 2.43    | 0.66                             | 0.66    |
| 15          | 13                      | 86.67              | 2               | 1.8           | 1.89    | 0.63                             | 0.64    |
| 15          | 12                      | 80                 | 3               | 1.32          | 1.88    | 0.61                             | 0.64    |
| 15          | 11                      | 73.33              | 6               | 1.18          | 1.54    | 0.61                             | 0.62    |
| 15          | 10                      | 66.67              | 5               | 0.92          | 0.98    | 0.61                             | 0.61    |
| 15          | 9                       | 60                 | 14              | 0.57          | 0.93    | 0.60                             | 0.61    |
| 15          | 8                       | 53.33              | 27              | 0.18          | 0.76    | 0.60                             | 0.61    |
| 15          | 7                       | 46.67              | 27              | -0.12         | 0.46    | 0.60                             | 0.62    |
| 15          | 6                       | 40                 | 26              | -0.56         | 0.22    | 0.61                             | 0.62    |
| 15          | 5                       | 33.33              | 22              | -0.87         | -0.25   | 0.62                             | 0.64    |
| 15          | 4                       | 26.67              | 14              | -1.26         | -0.58   | 0.62                             | 0.66    |
| 15          | 3                       | 20                 | 14              | -1.57         | -0.86   | 0.64                             | 0.67    |
| 15          | 2                       | 13.33              | 2               | -1.83         | -1.83   | 0.69                             | 0.69    |
| 15          | 1                       | 6.67               | 0               | --            | --      | --                               | --      |
| 15          | 0                       | 0                  | 1               | -2.27         | -2.27   | 0.73                             | 0.73    |

*Note.* \* Scale scores and standard errors of scale scores vary depending on which questions are answered correctly. To show the range, the authors report the maximum and minimum of the scale scores and standard errors of scale scores.



Table D5.  
The scores files for grade 8.

| Total items | Number of correct items | Proportion correct | Number of cases | Scale scores* |         | Standard errors of scale score * |         |
|-------------|-------------------------|--------------------|-----------------|---------------|---------|----------------------------------|---------|
|             |                         |                    |                 | Minimum       | Maximum | Minimum                          | Maximum |
| 15          | 15                      | 100                | 1               | 2.34          | 2.34    | .70                              | .70     |
| 15          | 14                      | 93.33              | 1               | 1.94          | 1.94    | .67                              | .67     |
| 15          | 13                      | 86.67              | 5               | 1.70          | 1.82    | .64                              | .65     |
| 15          | 12                      | 80                 | 10              | 1.03          | 1.46    | .61                              | .63     |
| 15          | 11                      | 73.33              | 13              | .90           | 1.26    | .60                              | .62     |
| 15          | 10                      | 66.67              | 14              | .51           | 1.02    | .58                              | .61     |
| 15          | 9                       | 60                 | 13              | .33           | .66     | .58                              | .59     |
| 15          | 8                       | 53.33              | 30              | -.02          | .81     | .59                              | .71     |
| 15          | 7                       | 46.67              | 28              | -.45          | .00     | .60                              | .60     |
| 15          | 6                       | 40                 | 22              | -.60          | .02     | .60                              | .68     |
| 15          | 5                       | 33.33              | 26              | -.98          | -.59    | .61                              | .63     |
| 15          | 4                       | 26.67              | 11              | -1.23         | -.95    | .63                              | .65     |
| 15          | 3                       | 20                 | 7               | -1.52         | -1.24   | .65                              | .66     |
| 15          | 2                       | 13.33              | 3               | -1.80         | -1.69   | .67                              | .68     |
| 15          | 1                       | 6.67               | 0               | --            | --      | --                               | --      |
| 15          | 0                       | 0                  | 0               | --            | --      | --                               | --      |

*Note.* \* Scale scores and standard errors of scale scores vary depending on which questions are answered correctly. To show the range, the authors report the maximum and minimum of the scale scores and standard errors of scale

## Appendix E: The Parameter files of Grades 3-8 measures under the 2PL model

Table E1.  
The parameter files of grade 3.

|         | Intercept | Intercept<br>SE | Slope   | Slope<br>SE | Difficulty | Difficulty<br>SE |
|---------|-----------|-----------------|---------|-------------|------------|------------------|
| Item 01 | 1.32085   | 0.15205         | 0.56668 | 0.11908     | -2.33083   | 0.49993          |
| Item 02 | 1.09815   | 0.13606         | 0.54736 | 0.12459     | -2.00626   | 0.44097          |
| Item 03 | 1.03764   | 0.15229         | 0.76334 | 0.15331     | -1.35933   | 0.2732           |
| Item 04 | 0.7214    | 0.12941         | 0.75728 | 0.13905     | -0.95262   | 0.20902          |
| Item 05 | 0.51843   | 0.13371         | 0.89424 | 0.15578     | -0.57974   | 0.1558           |
| Item 06 | 0.66304   | 0.20019         | 1.63523 | 0.29128     | -0.40548   | 0.1223           |
| Item 07 | 0.97314   | 0.21427         | 1.65698 | 0.2729      | -0.5873    | 0.13171          |
| Item 08 | 0.94397   | 0.21173         | 1.57452 | 0.29188     | -0.59953   | 0.12758          |
| Item 09 | 0.80838   | 0.1779          | 1.25344 | 0.23129     | -0.64492   | 0.14284          |
| Item 10 | 0.87152   | 0.16979         | 0.99932 | 0.18525     | -0.87211   | 0.17376          |
| Item 11 | 0.47678   | 0.11886         | 0.60958 | 0.1215      | -0.78214   | 0.22823          |
| Item 12 | 0.55606   | 0.10585         | 0.45377 | 0.10171     | -1.22543   | 0.30967          |
| Item 13 | 0.18503   | 0.12927         | 0.75663 | 0.14633     | -0.24454   | 0.1737           |
| Item 14 | 1.31942   | 0.20773         | 1.45443 | 0.24384     | -0.90716   | 0.14583          |
| Item 15 | 0.25947   | 0.13081         | 0.69926 | 0.16353     | -0.37106   | 0.18126          |

Table E2.  
The parameter files of grade 4.

|                | Intercept | Intercept<br>SE | Slope   | Slope<br>SE | Difficulty | Difficulty<br>SE |
|----------------|-----------|-----------------|---------|-------------|------------|------------------|
| <b>Item 01</b> | 0.41071   | 0.136           | 0.36721 | 0.08893     | -1.11851   | 0.44231          |
| <b>Item 02</b> | 0.6962    | 0.15218         | 0.36749 | 0.10739     | -1.89452   | 0.61422          |
| <b>Item 03</b> | 0.09613   | 0.13737         | 0.34409 | 0.09492     | -0.27938   | 0.38624          |
| <b>Item 04</b> | -0.75267  | 0.12988         | 0.36321 | 0.08789     | 2.07227    | 0.59177          |
| <b>Item 05</b> | -0.53276  | 0.14384         | 0.50387 | 0.11494     | 1.05733    | 0.35204          |
| <b>Item 06</b> | -0.45006  | 0.11952         | 0.31598 | 0.08015     | 1.42432    | 0.50495          |
| <b>Item 07</b> | -0.73975  | 0.14538         | 0.47586 | 0.10677     | 1.55456    | 0.42516          |
| <b>Item 08</b> | 0.73354   | 1.94312         | 7.17478 | 3.10544     | -0.10224   | 0.18208          |
| <b>Item 09</b> | -1.44045  | 0.52675         | 2.29396 | 0.5518      | 0.62793    | 0.16943          |
| <b>Item 10</b> | --        | --              | --      | --          | --         | --               |
| <b>Item 11</b> | -1.97132  | 0.26263         | 1.00376 | 0.15251     | 1.96393    | 0.30997          |
| <b>Item 12</b> | -0.28866  | 0.12007         | 0.36886 | 0.09097     | 0.78255    | 0.37739          |
| <b>Item 13</b> | -0.72806  | 0.126           | 0.34521 | 0.08892     | 2.10904    | 0.64094          |
| <b>Item 14</b> | -0.87283  | 0.13876         | 0.44559 | 0.09956     | 1.95882    | 0.46528          |
| <b>Item 15</b> | -1.10449  | 0.14746         | 0.41304 | 0.09605     | 2.67411    | 0.67534          |

Table E3.  
The parameter files of grade 5.

|         | Intercept | Intercept<br>SE | Slope   | Slope<br>SE | Difficulty | Difficulty<br>SE |
|---------|-----------|-----------------|---------|-------------|------------|------------------|
| Item 01 | 0.35347   | 0.0973          | 0.53034 | 0.10892     | -0.66651   | 0.2038           |
| Item 02 | 0.29714   | 0.09709         | 0.54826 | 0.11098     | -0.54197   | 0.19012          |
| Item 03 | -0.13423  | 0.08724         | 0.44245 | 0.10451     | 0.30339    | 0.20663          |
| Item 04 | -0.60464  | 0.11078         | 0.60001 | 0.13423     | 1.00772    | 0.22542          |
| Item 05 | -2.39772  | 0.29547         | 0.73777 | 0.21226     | 3.24996    | 0.72685          |
| Item 06 | -2.39477  | 0.42077         | 1.09871 | 0.3513      | 2.17962    | 0.43306          |
| Item 07 | -1.52745  | 0.18008         | 0.70451 | 0.16514     | 2.16809    | 0.42182          |
| Item 08 | -0.78331  | 0.10342         | 0.46144 | 0.10675     | 1.69752    | 0.39121          |
| Item 09 | -0.16838  | 0.09047         | 0.44947 | 0.10085     | 0.37462    | 0.22117          |
| Item 10 | -1.56645  | 0.1703          | 0.60189 | 0.14253     | 2.60254    | 0.58349          |
| Item 11 | 0.52011   | 0.08783         | 0.26093 | 0.06887     | -1.99325   | 0.58791          |
| Item 12 | 0.04089   | 0.08083         | 0.32766 | 0.07905     | -0.12478   | 0.24673          |
| Item 13 | -0.51183  | 0.09633         | 0.45718 | 0.10122     | 1.11954    | 0.29568          |
| Item 14 | --        | --              | --      | --          | --         | --               |
| Item 15 | -0.01316  | 0.08071         | 0.23173 | 0.06092     | 0.05679    | 0.3484           |

Table E4.  
The parameter files of grade 6.

|         | Intercept | Intercept<br>SE | Slope   | Slope<br>SE | Difficulty | Difficulty<br>SE |
|---------|-----------|-----------------|---------|-------------|------------|------------------|
| Item 01 | -1.25614  | 0.24615         | 0.70966 | 0.18138     | 1.77005    | 0.40976          |
| Item 02 | -1.20315  | 0.22619         | 0.6623  | 0.17494     | 1.81662    | 0.41074          |
| Item 03 | -0.20064  | 0.12548         | 0.49535 | 0.11062     | 0.40504    | 0.24944          |
| Item 04 | -1.06479  | 0.15863         | 0.46791 | 0.11751     | 2.27561    | 0.57521          |
| Item 05 | -0.21761  | 0.11484         | 0.3686  | 0.09153     | 0.59038    | 0.33317          |
| Item 06 | -0.38075  | 0.10989         | 0.33158 | 0.08267     | 1.14829    | 0.43513          |
| Item 07 | 0.00729   | 0.12947         | 0.53906 | 0.13025     | -0.01352   | 0.22214          |
| Item 08 | -0.11564  | 0.1043          | 0.22611 | 0.06251     | 0.51142    | 0.48583          |
| Item 09 | 0.15145   | 0.14269         | 0.63349 | 0.15439     | -0.23906   | 0.20346          |
| Item 10 | 0.30581   | 0.11685         | 0.40462 | 0.10907     | -0.75579   | 0.30019          |
| Item 11 | -0.07535  | 0.14463         | 0.50592 | 0.13123     | 0.14895    | 0.28058          |
| Item 12 | -0.68266  | 0.11784         | 0.33756 | 0.0958      | 2.02236    | 0.65214          |
| Item 13 | 0.86338   | 0.11738         | 0.28237 | 0.07567     | -3.05765   | 0.85455          |
| Item 14 | 1.31993   | 0.18917         | 0.76385 | 0.19961     | -1.728     | 0.33243          |
| Item 15 | -0.33634  | 0.11595         | 0.39504 | 0.09802     | 0.85142    | 0.33422          |

Table E5.  
The parameter files of grade 8.

|         | Intercept | Intercept<br>SE | Slope   | Slope<br>SE | Difficulty | Difficulty<br>SE |
|---------|-----------|-----------------|---------|-------------|------------|------------------|
| Item 01 | 1.19771   | 0.14507         | 0.42647 | 0.11297     | -2.80842   | 0.71473          |
| Item 02 | 1.014     | 0.13548         | 0.41374 | 0.1116      | -2.45084   | 0.62493          |
| Item 03 | 0.5102    | 0.11237         | 0.47019 | 0.10833     | -1.08512   | 0.29642          |
| Item 04 | -0.26075  | 0.10501         | 0.50252 | 0.10982     | 0.51887    | 0.2293           |
| Item 05 | 0.99841   | 0.13056         | 0.36949 | 0.11073     | -2.70221   | 0.74609          |
| Item 06 | 0.38505   | 0.13072         | 0.60228 | 0.1441      | -0.63932   | 0.22635          |
| Item 07 | -0.3426   | 0.09597         | 0.32573 | 0.08419     | 1.0518     | 0.38252          |
| Item 08 | 0.27114   | 0.10071         | 0.34979 | 0.08532     | -0.77516   | 0.32236          |
| Item 09 | -0.44838  | 0.11535         | 0.6091  | 0.13668     | 0.73614    | 0.22074          |
| Item 10 | -0.62203  | 0.12543         | 0.54622 | 0.12706     | 1.13882    | 0.29229          |
| Item 11 | -0.57898  | 0.11135         | 0.38818 | 0.09394     | 1.49151    | 0.42777          |
| Item 12 | -0.49994  | 0.10275         | 0.3075  | 0.07868     | 1.62578    | 0.49535          |
| Item 13 | -0.4976   | 0.11245         | 0.48159 | 0.11209     | 1.03323    | 0.30542          |
| Item 14 | -0.37167  | 0.11869         | 0.68265 | 0.15157     | 0.54447    | 0.19474          |
| Item 15 | -0.16708  | 0.11076         | 0.55067 | 0.12159     | 0.30341    | 0.21159          |

## Appendix F: Item analysis of problematic items

Grade 3, Item 1:

$$\begin{array}{r} 483 \\ + 371 \\ \hline \end{array}$$

Table F1.

Item analysis for item 1 in grade 3.

|         | Number | Percent | Average Measures | Standard Error Mean | Outfit Mean Square |
|---------|--------|---------|------------------|---------------------|--------------------|
| A 7154  | 9      | 4       | 41.68            | 5.53                | 0.8                |
| C 753   | 9      | 4       | 52.92            | 5.70                | 3.3                |
| D 112   | 7      | 3       | 55.81            | 7.78                | 3.6                |
| B* 854  | 192    | 88      | 65.40            | 1.14                | 1.0                |
| Missing | 22     | 7       |                  |                     |                    |

Grade 5, Item 14:

$$.2 \overline{)14.26}$$

Table F2.

Item analysis for item 14 in grade 5.

|         | Number | Percent | Average Measures | Standard Error Mean | Outfit Mean Square |
|---------|--------|---------|------------------|---------------------|--------------------|
| B 70.3  | 40     | 16      | 37.12            | 1.49                | 0.9                |
| A 7.03  | 46     | 18      | 39.81            | 1.48                | 1.6                |
| C 7.13  | 122    | 48      | 40.12            | 0.92                | 1.3                |
| D* 71.3 | 47     | 18      | 40.93            | 1.28                | 1.7                |
| Missing | 18     | 7       |                  |                     |                    |

Grade 7, Item 7:

$$(-8000) - (-4264) =$$

Table F3.

Item analysis for item 7 in grade 7.

|          | Number | Percent | Average<br>Measures | Standard<br>Error<br>Mean | Outfit<br>Mean<br>Square |
|----------|--------|---------|---------------------|---------------------------|--------------------------|
| B -3736  | 29     | 16      | 43.15               | 1.65                      | 0.6                      |
| A 3736   | 40     | 22      | 47.71               | 1.36                      | 1.0                      |
| C 12264  | 50     | 27      | 50.71               | 1.27                      | 1.4                      |
| D*-12264 | 65     | 35      | 55.81               | 1.31                      | 1.0                      |
| Missing  | 28     | 13      |                     |                           |                          |